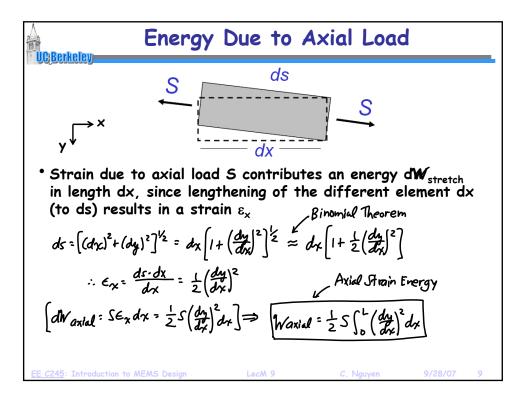
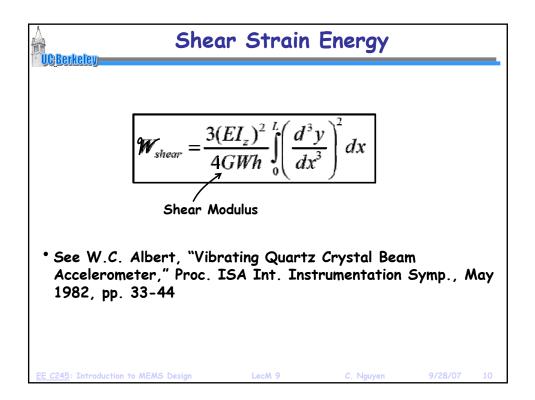
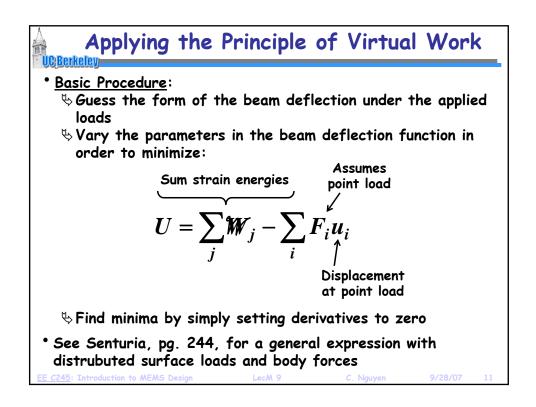
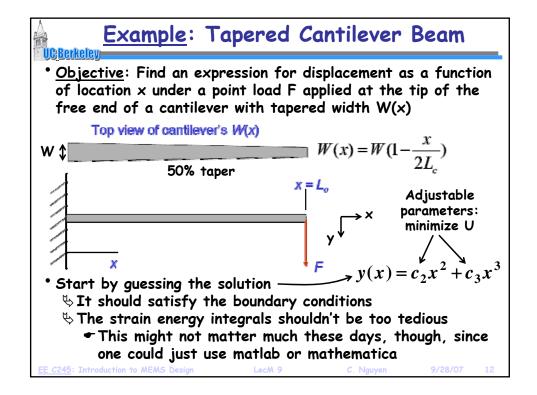


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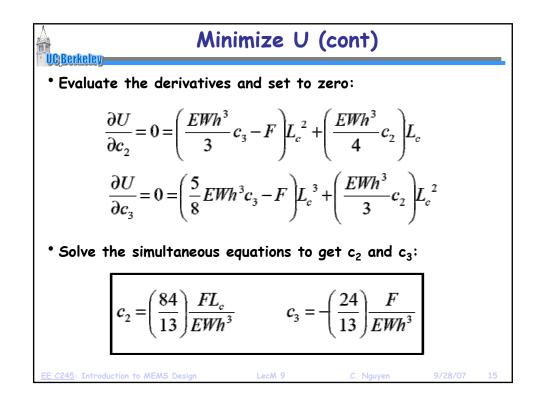








Find  $c_2$  and  $c_3$  That Minimize U • Minimize U  $\rightarrow$  basically, find the  $c_2$  and  $c_3$  that brings U closest to zero (which is what it would be if we had guessed correctly) • The  $c_2$  and  $c_3$  that minimize U are the ones for which the partial derivatives of U with respective to them are zero:  $\frac{\partial U}{\partial c_2} = 0 \qquad \frac{\partial U}{\partial c_3} = 0$ • Proceed:  $\psi$  First, evaluate the integral to get an expression for U:  $U = EWh^3 \left\{ \frac{5c_3^2}{16} L_c^3 + \frac{c_2c_3}{3} L_c^2 + \frac{c_2^2}{8} L_c \right\} - F(c_2L_c^2 + c_3L_c^3)$ EE C245: Introduction to MEMS Design



The Virtual Work-Derived Solution (Control of the solution:  $y(x) = \left(\frac{24F}{13EWh^3}\right) \left(\frac{7}{2}L_c - x\right) x^2$ • Solve for tip deflection and obtain the spring constant:  $y(L_c) = \left(\frac{24F}{13EWh^3}\right) \left(\frac{5}{2}L_c^3 - k_c = F/y(L_c) = \left(\frac{13EWh^3}{60L_c^3}\right)$ • Compare with previous solution for constant-width cantilever beam (using Euler theory):  $y(L_c) = \left(\frac{4F}{EWh^3}\right) L_c^3 \longrightarrow 13\% \text{ smaller than tapered-width case}$ 

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