

Anisotropic Wet Etching

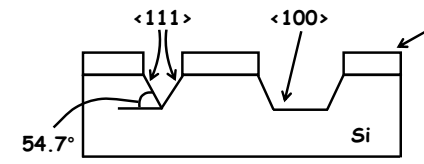
Anisotropic etches also available for single crystal Si:

- Orientation-dependent etching: $\langle 111 \rangle$ -plane more densely packed than $\langle 100 \rangle$ -plane
 - Faster E.R.
 - Slower E.R.
- ...in some solvents
- One such solvent: KOH + isopropyl alcohol
(e.g., 23.4 wt% KOH, 13.3 wt% isopropyl alcohol, 63 wt% H₂O)
- $\Rightarrow \text{E.R.}_{\langle 100 \rangle} = 100 \times \text{E.R.}_{\langle 111 \rangle}$

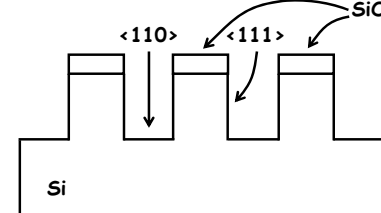
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Anisotropic Wet Etching (cont.)

Can get the following:



(on a $\langle 100 \rangle$ - wafer)

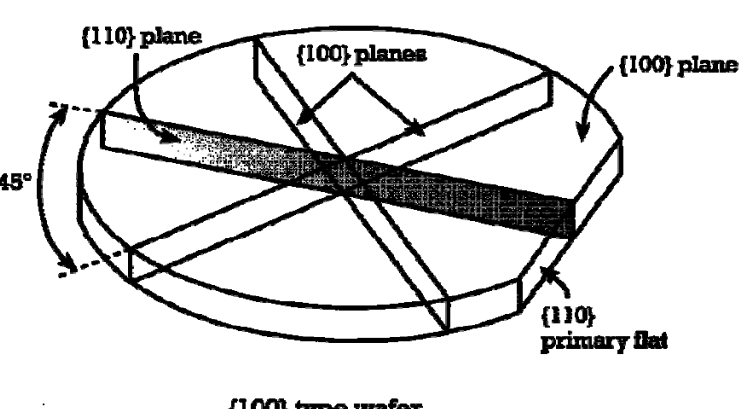


(on a $\langle 110 \rangle$ - wafer)

\Rightarrow Quite anisotropic!

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Silicon Wafers



$\{110\}$ plane

$\{100\}$ planes

$\{100\}$ plane

45°

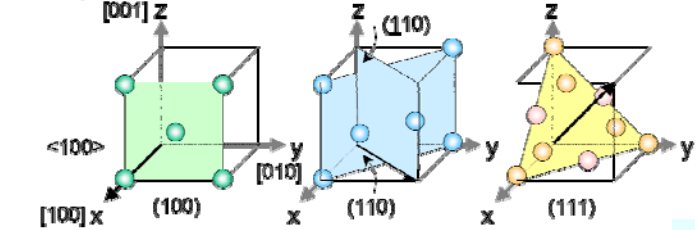
$\{110\}$ primary flat

$\{100\}$ type wafer

[Maluf]

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Silicon Crystallography



$[001]$ z

$\langle 100 \rangle$

$[100]$ x

(100)

$[010]$ y

(110)

$[110]$ z

(111)

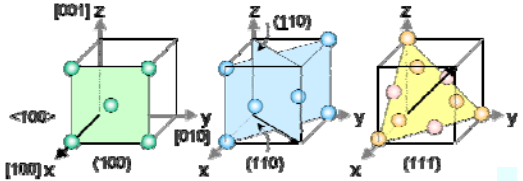
$[111]$

Miller Indices (h k l):

- Planes
 - Reciprocal of plane intercepts with axes
 - e.g., for (110), intercepts: (x,y,z) = (1,1, ∞); reciprocals: (1,1,0) \rightarrow (110)
 - (unique), {family}
- Directions
 - One endpoint of vector @ origin
 - [unique], \langle family \rangle

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Determining Angles Between Planes



• The angle between vectors $[abc]$ and $[xyz]$ is given by:


$$ax + by + cz = |(a, b, c)| \cdot |(x, y, z)| \cdot \cos \theta$$

$$\theta_{(a,b,c),(x,y,z)} = \cos^{-1} \left[\frac{ax + by + cz}{|(a, b, c)| \cdot |(x, y, z)|} \right]$$

- For $\{100\}$ and $\{110\} \rightarrow 45^\circ$
- For $\{100\}$ and $\{111\} \rightarrow 54.74^\circ$
- For $\{110\}$ and $\{111\} \rightarrow 35.26^\circ, 90^\circ, \text{ and } 144.74^\circ$

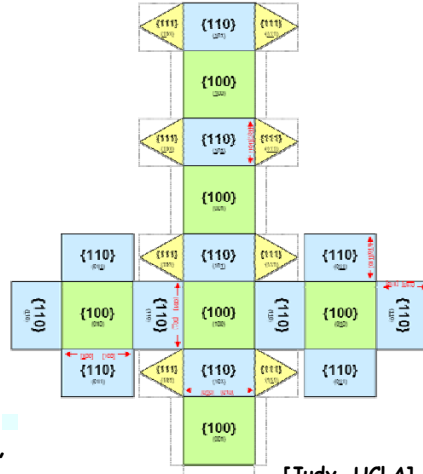
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Silicon Crystal Origami



Judy

- Silicon fold-up cube
- Adapted from Profs. Kris Pister and Jack Judy
- Print onto transparency
- Assemble inside out
- Visualize crystal plane orientations, intersections, and directions



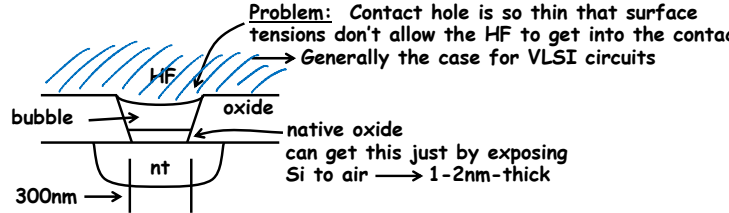
[Judy, UCLA]

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Wet Etching SiO_2

$$\text{SiO}_2 + 6\text{HF} \rightarrow \text{H}_2 + \text{SiF}_6 + 2\text{H}_2\text{O}$$

Generally used to clear out residual oxides from contacts



Problem: Contact hole is so thin that surface tensions don't allow the HF to get into the contact
→ Generally the case for VLSI circuits

native oxide can get this just by exposing Si to air → 1-2nm-thick

Solution: add a surfactant (e.g., Triton X) to the BHF before the contact clear etch

- Improves the ability of HF to wet the surface (hence, get into the contact)
- Suppresses the formation of etch by-products, which otherwise can block further reaction if by-products get caught in the contact

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More Wet Etch Chemistries

- Wet etching silicon nitride
 - Use hot phosphoric acid: 85% phosphoric acid @ 180°C
 - Etch rate ~ 10 nm/min (quite slow)
 - Problem:** PR lifted during such etching
 - Solution:** use SiO_2 as an etch mask (E.R. ~2.5 nm/min)
 - A hassle → dry etch processes more common than wet
- Wet etching aluminum
 - Typical etch solution composition:

H_2PO_4	HNO_3	CH_3COOH	H_2O
(1) Forms Al_2O_3 (aluminum oxide)			
(2) Dissolves the Al_2O_3			
 - Problem:** H_2 gas bubbles adhere firmly to the surface → delay the etch → need a 10-50% overetch time
 - Solution:** mechanical agitation, periodic removal of wafers from etching solution

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Wet Etch Rates (f/ K. Williams)

[illegible]

Notation: — not performed; W—wet performed, but known to Work (2–100 Å/min); F—frost performed, but known to be Fast (2–10 Å/min); P—some of film peeled during etch or when raised; A—film was visibly attacked and roughened; C—etch marks all of 4–4 inch width for the transparent film and half of the width for single-crystal silicon and the metals.

Film Etch Chemistries

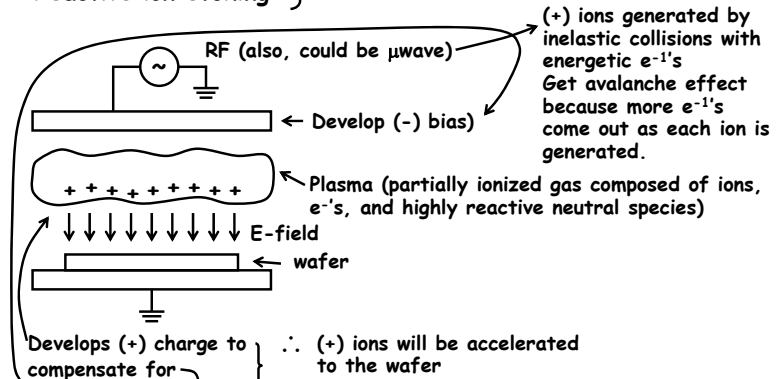
- For some popular films:

Material	Wet etchant	Etch rate [nm/min]	Dry etchant	Etch rate [nm/min]
Polysilicon	$\text{HNO}_3\text{:H}_2\text{O}\text{:NH}_4\text{F}$	120-600	$\text{SF}_6 + \text{He}$	170-920
Silicon nitride	H_3PO_4	5	SF_6	150-250
Silicon dioxide	HF	20-2000	$\text{CHF}_3 + \text{O}_2$	50-150
Aluminum	$\text{H}_3\text{PO}_4\text{:HNO}_3\text{:CH}_3\text{COOH}$	660	$\text{Cl}_2 + \text{SiCl}_4$	100-150
Photoresist	Acetone	>4000	O_2	35-3500
Gold	KI	40	n/a	n/a

Dry Etching

Dry Etching

- Physical sputtering
 - Plasma etching
 - Reactive ion etching
- } All based upon plasma processes.



Physical Sputtering (Ion Milling)

- Bombard substrate w/ energetic ions → etching via physical momentum transfer
- Give ions energy and directionality using E-fields
- Highly directional → very anisotropic

Steep vertical wall

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Problems With Ion Milling

- PR or other masking material etched at almost the same rate as the film to be etched → very poor selectivity!
- Ejected species not inherently volatile → get redeposition → non-uniform etch → grass!

- Because of these problems, ion milling is not used often (very rare)

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Plasma Etching

- Plasma (gas glow discharge) creates reactive species that chemically react w/ the film in question
- Result:** much better selectivity, but get an isotropic etch

Plasma Etching Mechanism:

- Reactive species generated in a plasma.
- Reactive species diffuse to the surface of material to be etched.
- Species adsorbed on the surface.
- Chemical reaction.
- By-product desorbed from surface.
- Desorbed species diffuse into the bulk of the gas

← MOST IMPORTANT STEP! (determines whether plasma etching is possible or not.)

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Ex: Polysilicon Etching w/ CF_4 and O_2

$$\text{CF}_4 \xrightarrow{\text{plasma}} \text{CF}_4^+ + \text{CF}_3^+ + \text{CF}_2^+ + \text{CF}^+ + \text{F}^+ + \text{F}^0 + \text{CF}_2^+ + \dots$$

Neutral radical (highly reactive!)

$$\text{e}^- + \text{CF}_4 \rightarrow \text{CF}_3 + \text{F} + \text{e}^-$$

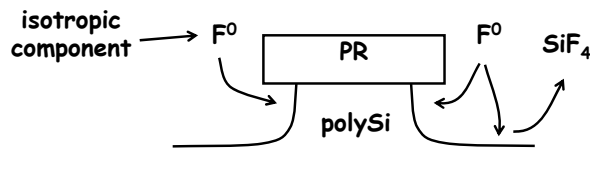
$\text{SiCF}_6, \text{SiF}_4$ ← both volatile ∴ dry etching is possible.

- F^0 is the dominant reactant → but it can't be given a direction → thus, get isotropic etch!

isotropic component → F^0

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Ex: Polysilicon Etching w/ CF_4 and O_2



Problems:

1. Isotropic etching
2. Formation of polymer because of C in CF_4
 - \rightarrow **Solution:** add O_2 to remove the polymer (but note that this reduces the selectivity, $S_{\text{poly/PR}}$)

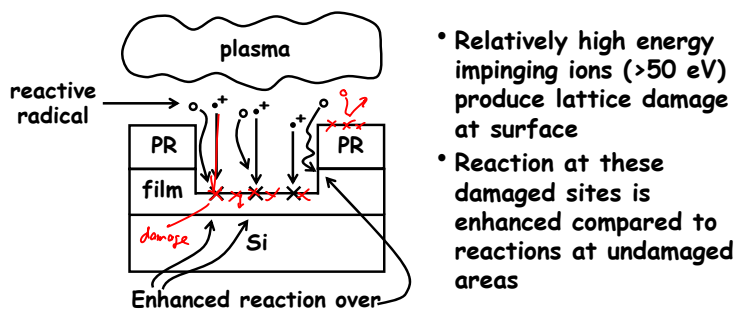
Solution:

- \rightarrow Use Reactive Ion Etching (RIE)

Reactive Ion Etching (RIE)

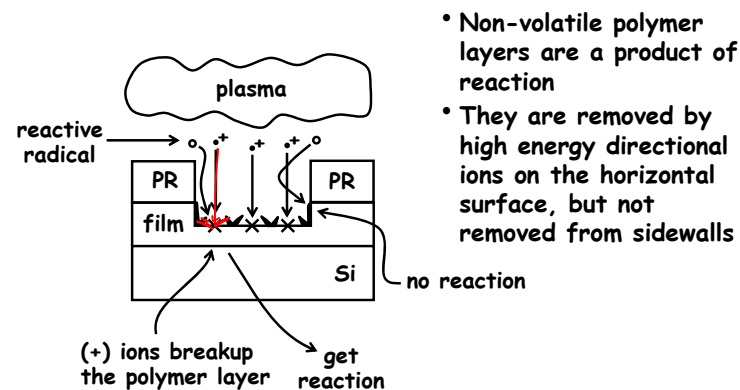
- Use ion bombardment to aid and enhance reactive etching in a particular direction
 - \rightarrow **Result:** directional, anisotropic etching!
- RIE is somewhat of a misnomer
 - \rightarrow It's not ions that react ... rather, it's still the neutral species that dominate reaction
 - \rightarrow Ions just enhance reaction of these neutral radicals in a specific direction
- Two principle postulated mechanisms behind RIE
 1. Surface damage mechanism
 2. Surface inhibitor mechanism

RIE: Surface Damage Mechanism



Result: E.R. at surface \gg E.R. on sidewalls

RIE: Surface Inhibitor Mechanism

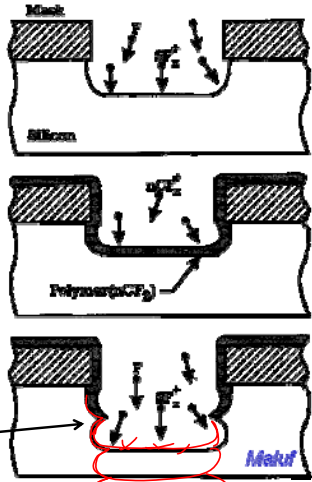


Result: E.R. @ surface \gg E.R. on sidewalls

Deep Reactive-Ion Etching (DRIE)

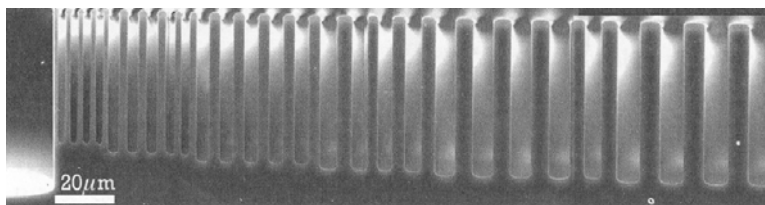
The Bosch process:

- Inductively-coupled plasma
- Etch Rate: 1.5-4 $\mu\text{m}/\text{min}$
- Two main cycles in the etch:
 - Etch cycle (5-15 s): SF_6 (SF_x^+) etches Si
 - Deposition cycle: (5-15 s): C_4F_8 deposits fluorocarbon protective polymer $(\text{CF}_2)_n$
- Etch mask selectivity:
 - $\text{SiO}_2 \sim 200:1$
 - Photoresist $\sim 100:1$
- Issue: finite sidewall roughness
 - scalloping < 50 nm
- Sidewall angle: $90^\circ \pm 2^\circ$

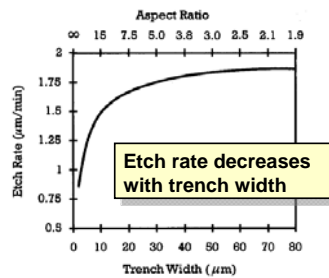


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DRIE Issues: Etch Rate Variance



- Etch rate is diffusion-limited and drops for narrow trenches
 - Adjust mask layout to eliminate large disparities
 - Adjust process parameters (slow down the etch rate to that governed by the slowest feature)



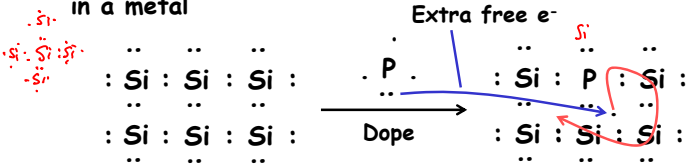
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Semiconductor Doping

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Doping of Semiconductors

- Semiconductors are not intrinsically conductive
- To make them conductive, replace silicon atoms in the lattice with dopant atoms that have valence bands with fewer or more e^- 's than the 4 of Si
- If more e^- 's, then the dopant is a donor: P, As
 - The extra e^- is effectively released from the bonded atoms to join a cloud of free e^- 's, free to move like e^- 's in a metal



- The larger the # of donor atoms, the larger the # of free e^- 's \rightarrow the higher the conductivity

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Doping of Semiconductors (cont.)

• Conductivity Equation:

$$\sigma = q\mu_n n + q\mu_p p$$

Labels for the equation:
 - σ : conductivity
 - q : charge magnitude on an electron
 - μ_n : electron mobility
 - n : electron density
 - μ_p : hole mobility
 - p : hole density

• If fewer e^- 's, then the dopant is an acceptor: B

Diagram showing the doping process:
 Left: Three Silicon (Si) atoms with four valence electrons each.
 Middle: A Boron (B) atom with three valence electrons.
 Right: The Boron atom is incorporated into the Silicon lattice, creating a hole (indicated by a red circle and arrow).
 Label: "Dope"

↳ Lack of an e^- = hole = h^+
 ↳ When e^- 's move into h^+ 's, the h^+ 's effectively move in the opposite direction → a h^+ is a mobile (+) charge carrier

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Ion Implantation

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Ion Implantation

• Method by which dopants can be introduced in silicon to make the silicon conductive, and for transistor devices, to form, e.g., pn-junctions, source/drain junctions, ...

The basic process:

Diagram illustrating the ion implantation process:
 - **Control current & time to control the dose.** (indicated by arrows to the B⁺ ions)
 - **Charged dopant accelerated to high energy by an E-Field (e.g., 100 keV)** (indicated by arrows to the B⁺ ions)
 - **Masking material (could be PR, could be oxide, etc.)** (indicated by a box on the Si surface)
 - **Depth determined by energy & type of dopant** (indicated by an 'x' on the Si surface)
 - **Result of I/I** (indicated by a downward arrow)

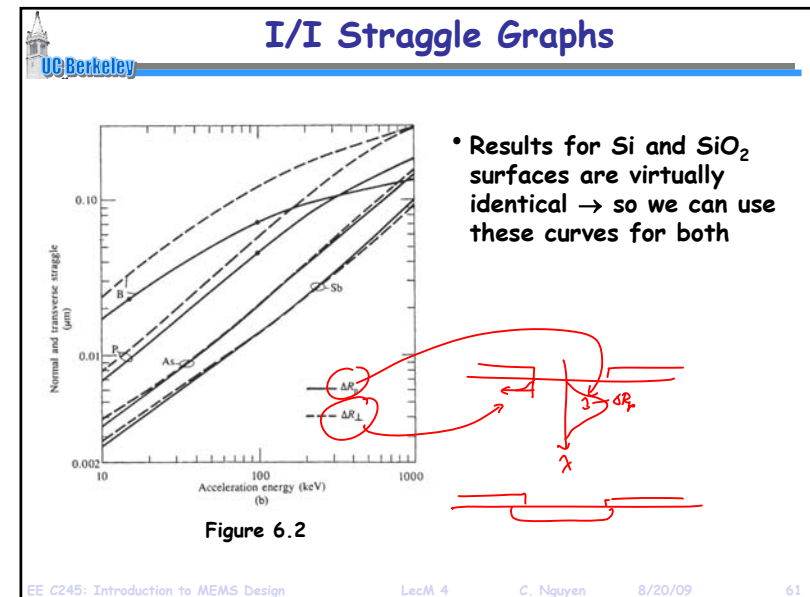
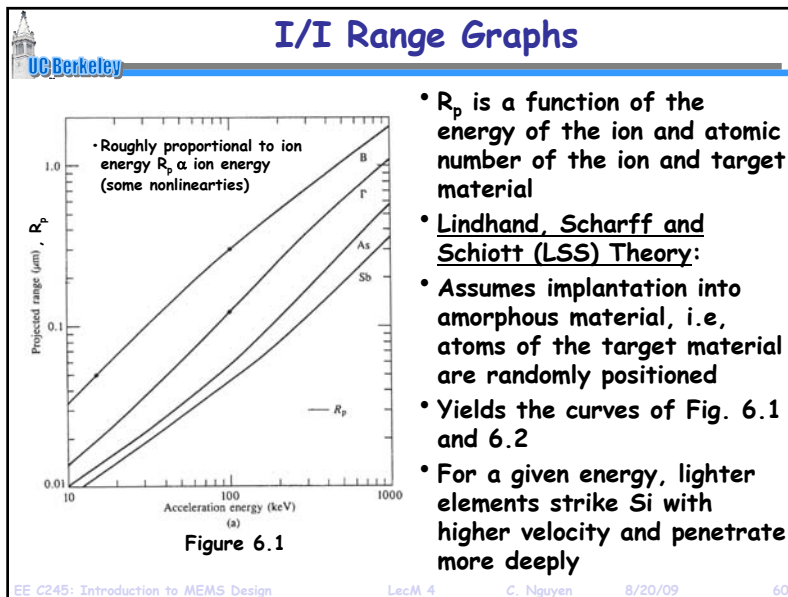
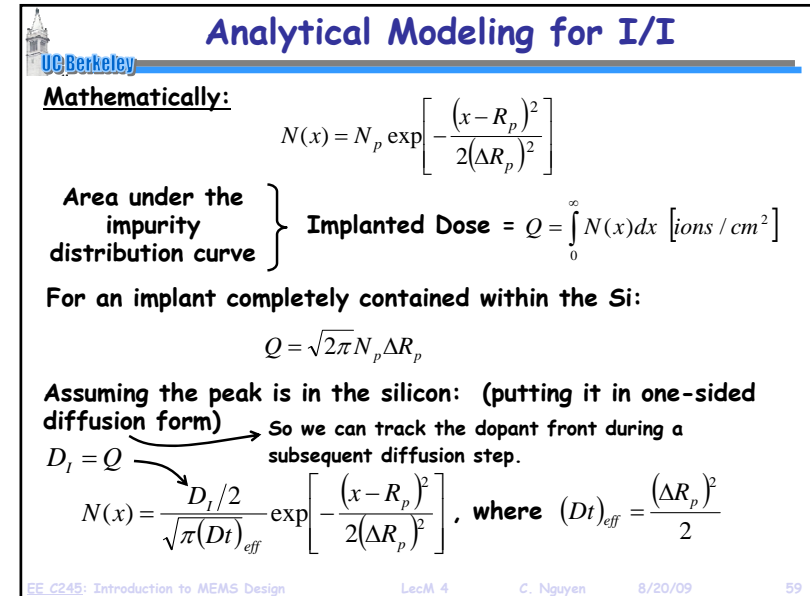
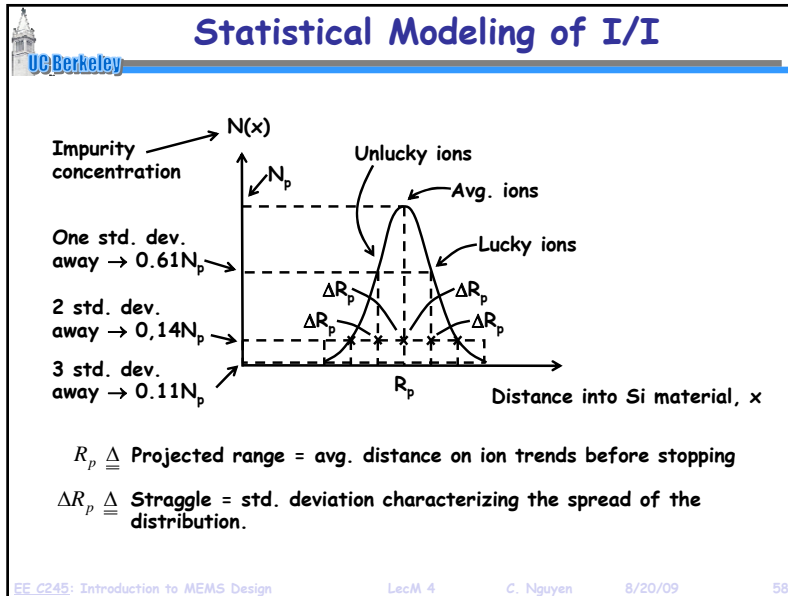
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Ion Implantation (cont.)

Result of I/I

Diagram illustrating the result of ion implantation:
 - **Damage → Si layer at top becomes amorphous** (indicated by a downward arrow)
 - **B not in the lattice, so it's not electrically active.** (indicated by a B atom outside the lattice)
 - **Ion collides with atoms and interacts with e^- 's in the lattice → all of which slow it down and eventually stop it.** (indicated by a B atom in the lattice)
 - **High Temperature Anneal (also, usually do a drive-in diffusion) (800-1200°C)** (indicated by a downward arrow)
 - **Now B in the lattice & electrically active! (serves as dopant)** (indicated by a B atom in the lattice)
 - **This is a statistical process → implanted impurity profile can be approximated by a Gaussian distribution.** (indicated by a downward arrow)

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Diffusion

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Diffusion in Silicon

- Movement of dopants within the silicon at high temperatures
- Three mechanisms: (in Si)

(a)

(b)

(c)

Substitutional Diffusion

- Impurity moves along vacancies in the lattice
- Substitutes for a Si-atom in the lattice

Interstitialcy Diffusion

- Impurity atom replaces a Si atom in the lattice
- Si atom displaced to an interstitial site

Interstitial Diffusion

- Impurity atoms jump from one interstitial site to another
- Get rapid diffusion
 - ↳ Hard to control
 - ↳ Impurity not in lattice so not electrically active

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Diffusion in Polysilicon

- In polysilicon, still get diffusion into the crystals, but get more and faster diffusion through grain boundaries
- **Result:** overall faster diffusion than in silicon

Fast diffusion through grain boundaries Regular diffusion into crystals

- In effect, larger surface area allows much faster volumetric diffusion

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Basic Process for Selective Doping

1. Introduce dopants (introduce a fixed dose Q of dopants)
 - (i) Ion implantation
 - (ii) Predeposition
2. Drive in dopants to the desired depth
 - ↳ High temperature $> 900^\circ\text{C}$ in N_2 or N_2/O_2

• **Result:**

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Predeposition

- Furnace-tube system using solid, liquid, or gaseous dopant sources
- Used to introduce a controlled amount of dopants
 - Unfortunately, not very well controlled
 - Dose (Q) range: $10^{13} - 10^{16} \pm 20\%$
 - For ref: w/ ion implantation: $10^{11} - 10^{16} \pm 1\%$ (larger range & more accurate)
- Example:** Boron predeposition

Predeposition Temp: 800-1100°C

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Ex: Boron Predeposition

- Basic Procedure:**
 - Deposit B_2O_3 glass
 - B diffuses from $B_2O_3 \rightarrow Si$
- Difficult to control dose Q, because it's heavily dependent on partial pressure of B_2H_6 gas flow
 - this is difficult to control itself
 - get only 10% uniformity

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Ex: Boron Predeposition (cont.)

For better uniformity, use solid source:

Reactions:

$$B_2H_6 + 3O_2 \rightarrow 3H_2O + B_2O_3$$

$$Si + O_2 \rightarrow SiO_2$$

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General Comments on Predeposition

- Higher doses only: $Q = 10^{13} - 10^{16} \text{ cm}^{-2}$ (I/I is $10^{11} - 10^{16}$)
- Dose not well controlled: $\pm 20\%$ (I/I can get $\pm 1\%$)
- Uniformity is not good
 - $\pm 10\%$ w/ gas source
 - $\pm 2\%$ w/ solid source
- Max. conc. possible limited by solid solubility
 - Limited to $\sim 10^{20} \text{ cm}^{-3}$
 - No limit for I/I \rightarrow you force it in here!
- For these reasons, I/I is usually the preferred method for introduction of dopants in transistor devices
- But I/I is not necessarily the best choice for MEMS
 - I/I cannot dope the underside of a suspended beam
 - I/I yields one-sided doping \rightarrow introduces unbalanced stress \rightarrow warping of structures
 - I/I can do physical damage \rightarrow problem if annealing is not permitted
- Thus, predeposition is often preferred when doping MEMS

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Diffusion Modeling

Modeling $N(x)$

⇒ Dopants from points of high conc. move to points of low conc. w/ flux J
⇒ Question: What's $N(x,t)$?
? fn of time

Fick's Law of Diffusion - (1st law)

$$J(x,t) = -D \frac{\partial N(x,t)}{\partial x} \quad (1)$$
 ↑
 Flux [$\#/\text{cm}^2 \cdot \text{s}$] Diffusion Coefficient

Continuity Equation for Particle Flux -
 General form: $\frac{\partial N(x,t)}{\partial t} = -\nabla \cdot \vec{J}$
 ↑
 rate of increase of conc. w/ time negative of the divergence of particle flux

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Diffusion Modeling (cont.)

⇒ We're interested for now in the one-dimensional form:

$$\frac{\partial N(x,t)}{\partial t} = -\frac{\partial J}{\partial x}$$

[$\frac{\partial}{\partial x}$ (1) and substitute (2) in (1)] ⇒ $\frac{\partial N(x,t)}{\partial t} = D \frac{\partial^2 N(x,t)}{\partial x^2}$ [Fick's 2nd Law of Diffusion in 1-D]

Solutions: → dependent upon boundary conditions
 ↳ use variable separation or Laplace Xform techniques

Case 1: Predeposition → constant source diffusion: surface concentration stays the same during the diffusion
 $t_1 < t_2 < t_3$
 $(D_1 t_1 < D_2 t_2 < D_3 t_3)$
 high T

surface conc. stays constant
 background conc. N_B
 x , distance f/ the surface

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Diffusion Modeling (Predeposition)

⇒ if plotted on a linear scale, would look like this:

⇒ **Boundary Condition:**
 (i) $N(0,t) = N_0$
 (ii) $N(\infty,t) = 0$

$$N(x,t) = N_0 \left[1 - \frac{1}{\sqrt{\pi}} \int_0^{\frac{x}{2\sqrt{Dt}}} e^{-y^2} dy \right]$$

$N(x,t) = N_0 \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right)$ ⇒ again, complementary error function (read tables or graph)

Dose, $Q \triangleq$ total # of impurity atoms per unit area in the Si
 = area under the curve
 $Q = \int_0^\infty N(x,t) dx \Rightarrow Q(t) = N_0 \frac{2\sqrt{Dt}}{\sqrt{\pi}} \text{ cm}^{-2}$

$2\sqrt{Dt} \triangleq$ characteristic diffusion length

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Diffusion Modeling (Limited Source)

Case 2: Drive-in → limited source diffusion, i.e., constant dose Q

Boundary Condition:
 (i) $N(\infty,t) = 0$
 (ii) $\frac{\partial N(x,t)}{\partial x} \Big|_{x=0} = 0$

Why? Constant Dose:
 $\int_0^\infty N(x,t) dx = Q \leftarrow \text{const.}$

⇒ This is equivalent to saying that there's no flux going out of the Si, i.e.,
 and that's what this says!

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Diffusion Modeling (Limited Source)

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Usually make delta fun. approx.: $N(x,0) = Q \delta(x)$
 \Rightarrow we can do this, because for sufficiently long diffusion times, no matter what the original shape of the dopant distribution, the diffused distribution will be the same

Get Gaussian Distribution: $N(x,t) = \frac{Q}{\sqrt{\pi Dt}} \exp\left[-\frac{x^2}{2Dt}\right]$ corresponds to a half Gaussian in this Equation

When the starting conc. profile is completely contained in the Si, then $Q = \frac{D_t}{2} = \text{half the implant dose}$

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Two-Step Diffusion

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- Two step diffusion procedure:
 - Step 1: predeposition (i.e., constant source diffusion)
 - Step 2: drive-in diffusion (i.e., limited source diffusion)
- For processes where there is both a predeposition and a drive-in diffusion, the final profile type (i.e., complementary error function or Gaussian) is determined by which has the much greater Dt product:
 - $(Dt)_{\text{predep}} \gg (Dt)_{\text{drive-in}} \Rightarrow$ impurity profile is complementary error function
 - $(Dt)_{\text{drive-in}} \gg (Dt)_{\text{predep}} \Rightarrow$ impurity profile is Gaussian (which is usually the case)

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Successive Diffusions

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- For actual processes, the junction/diffusion formation is only one of many high temperature steps, each of which contributes to the final junction profile
- Typical overall process:
 - Selective doping
 - Implant \rightarrow effective $(Dt)_1 = (\Delta R_p)^2/2$ (Gaussian)
 - Drive-in/activation $\rightarrow D_2 t_2$
 - Other high temperature steps
 - (eg., oxidation, reflow, deposition) $\rightarrow D_3 t_3, D_4 t_4, \dots$
 - Each has their own Dt product
 - Then, to find the final profile, use

$$(Dt)_{\text{tot}} = \sum_i D_i t_i$$

in the Gaussian distribution expression.

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The Diffusion Coefficient

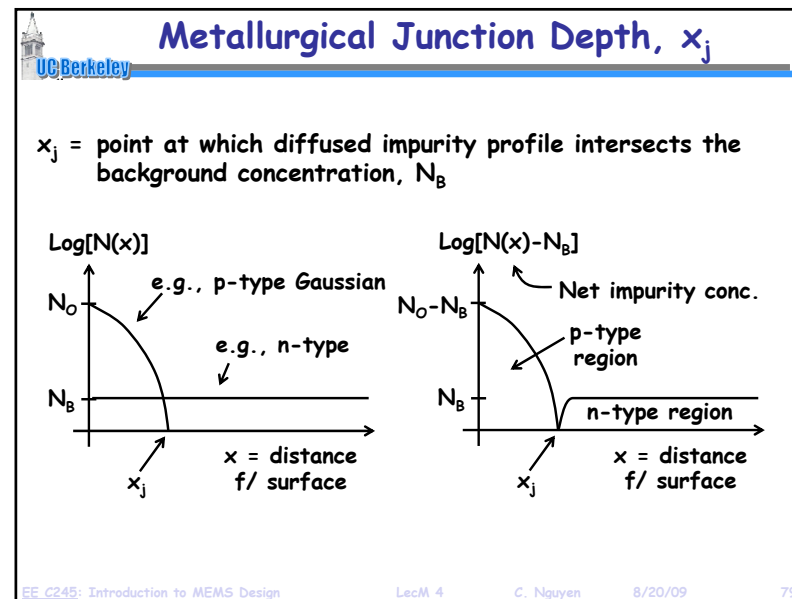
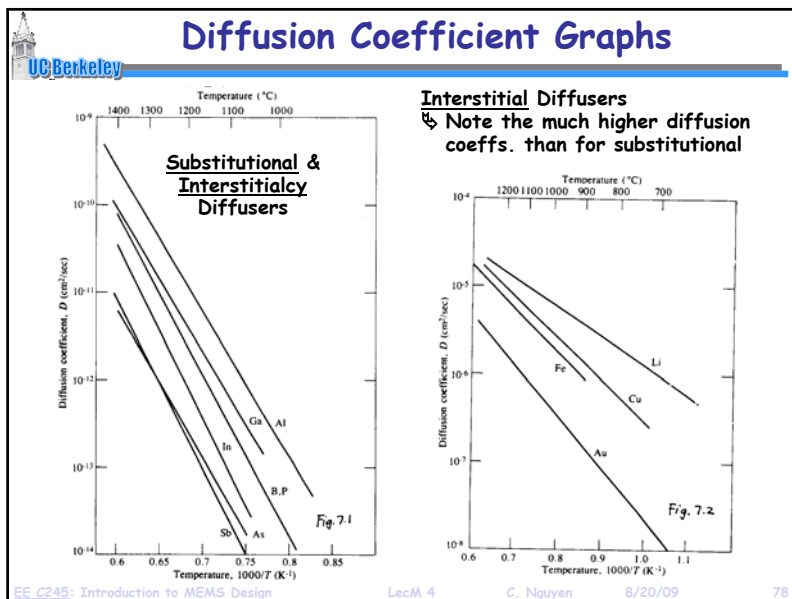
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$$D = D_o \exp\left(-\frac{E_A}{kT}\right) \quad (\text{as usual, an Arrhenius relationship})$$

Table 4.1 Typical Diffusion Coefficient Values for a Number of Impurities.

Element	$D_o(\text{cm}^2/\text{sec})$	$E_A(\text{eV})$
B	10.5	3.69
Al	8.00	3.47
Ga	3.60	3.51
In	16.5	3.90
P	10.5	3.69
As	0.32	3.56
Sb	5.60	3.95

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Expressions for x_j

- Assuming a Gaussian dopant profile: (the most common case)

$$N(x_j, t) = N_o \exp\left[-\left(\frac{x_j}{2\sqrt{Dt}}\right)^2\right] = N_B \rightarrow x_j = 2\sqrt{Dt \ln\left(\frac{N_o}{N_B}\right)}$$

- For a complementary error function profile:

$$N(x_j, t) = N_o \operatorname{erfc}\left(\frac{x_j}{2\sqrt{Dt}}\right) = N_B \rightarrow x_j = 2\sqrt{Dt} \operatorname{erfc}^{-1}\left(\frac{N_B}{N_o}\right)$$

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Sheet Resistance

- Sheet resistance provides a simple way to determine the resistance of a given conductive trace by merely counting the number of effective squares
- Definition:**

ohms per square

$$R = \frac{\rho L}{A} = \left(\frac{\rho}{t}\right) \frac{L}{w} = R_s \left(\frac{L}{w}\right)$$

(A = tw) sheet resistance # unit squares of material in the resistor

Uniformly doped material w/ resistivity $\rho = \frac{1}{\sigma}$

$\sigma = \text{conductivity} = q(\mu_n n + \mu_p p)$

e.g.,

total $R = R_s(\# \text{ squares}) = R_s \cdot 5$

$\therefore R = R_s \times S$

- What if the trace is non-uniform? (e.g., a corner, contains a contact, etc.)

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Squares From Non-Uniform Traces

Diagram 1: A square with side length $3W$ and a central square of side length W . The equivalent square is 0.65 squares.

Diagram 2: A square with side length W and a central square of side length W . The equivalent square is 0.56 squares.

Diagram 3: A square with side length W and a central square of side length $W/2$. The equivalent square is 0.14 squares.

Diagram 4: A square with side length $2W$ and a central square of side length W . The equivalent square is 0.35 squares.

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Sheet Resistance of a Diffused Junction

• For diffused layers:

Majority carrier mobility

Net impurity concentration

Effective resistivity

Sheet resistance

$$R_s = \frac{\rho}{x_j} = \left[\int_0^{x_j} \sigma(x) dx \right]^{-1} = \left[\int_0^{x_j} q \mu N(x) dx \right]^{-1}$$

[extrinsic material]

• This expression neglects depletion of carriers near the junction, $x_j \rightarrow$ thus, this gives a slightly lower value of resistance than actual

• Above expression was evaluated by Irvin and is plotted in "Irvin's curves" on next few slides

• Illuminates the dependence of R_s on x_j , N_0 (the surface concentration), and N_B (the substrate background conc.)

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Irvin's Curves (for n-type diffusion)

Example. p-type

Given:

$N_B = 3 \times 10^{16} \text{ cm}^{-3}$

$N_0 = 1.1 \times 10^{18} \text{ cm}^{-3}$ (n-type Gaussian)

$x_j = 2.77 \text{ } \mu\text{m}$

Can determine these given known predep. and drive conditions

Determine the R_s .

Using Fig. 7.7:

$R_s x_j = 470 \text{ } \Omega \cdot \mu\text{m}$

$\therefore R_s = \frac{470}{2.77} = 170 \text{ } \Omega/\square$

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Irvin's Curves (for p-type diffusion)

Example. n-type

Given:

$N_B = 3 \times 10^{16} \text{ cm}^{-3}$

$N_0 = 1.1 \times 10^{18} \text{ cm}^{-3}$ (p-type Gaussian)

$x_j = 2.77 \text{ } \mu\text{m}$

Can determine these given known predep. and drive conditions

Determine the R_s .

Using Fig. 7.9:

$R_s x_j = 800 \text{ } \Omega \cdot \text{cm}$

$\therefore R_s = \frac{800}{2.77} = 289 \text{ } \Omega/\square$

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