EE 245: Introduction to MEMS
Module 15: Gyros, Noise & MDS



EE C245 - ME C218 Introduction to MEMS Design Fall 2012

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Lecture Module 15: Gyros, Noise, & MDS

EE C245: Introduction to MEMS Design

.ecM 15

C. Nguyen

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Lecture Outline

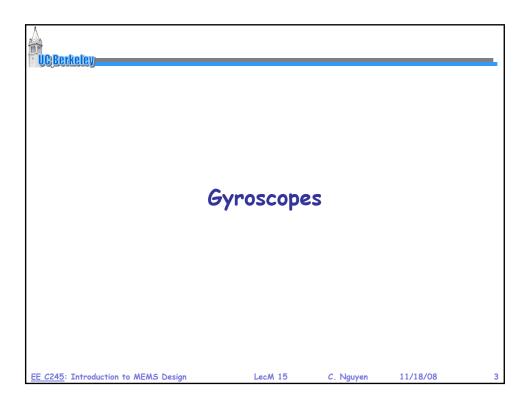
- Reading: Senturia, Chpt. 14, Chpt. 16, Chpt. 21
- Lecture Topics:
 - **⇔** Gyroscopes
 - Syro Circuit Modeling
 - ♦ Minimum Detectable Signal (MDS)
 - 🕶 Noise
 - ◆ Angle Random Walk (ARW)

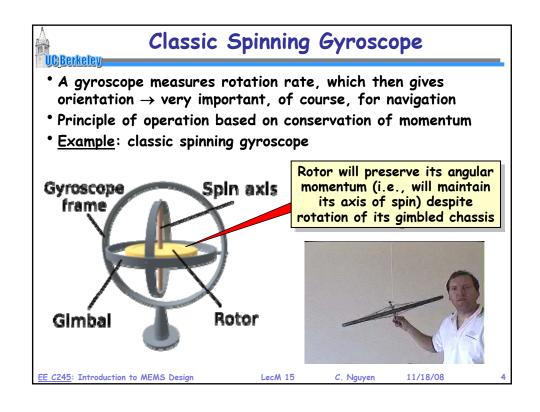
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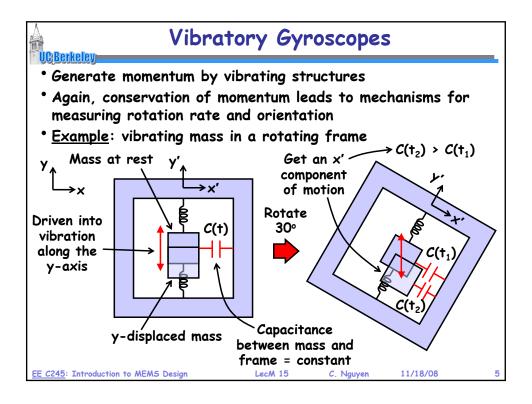
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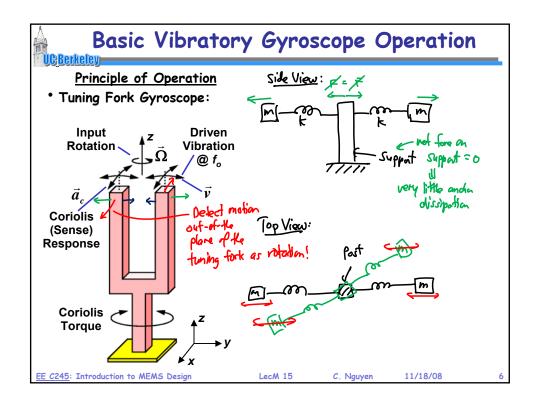
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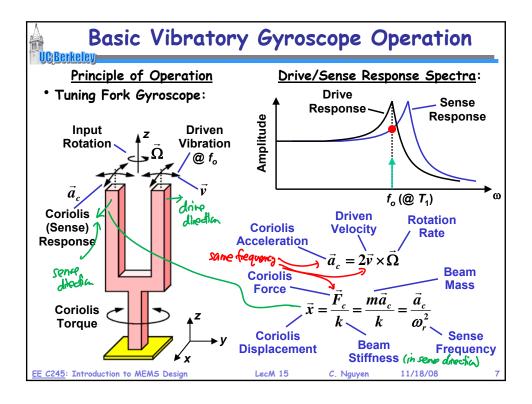
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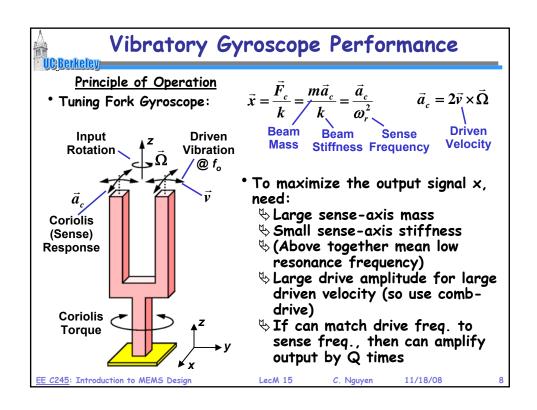


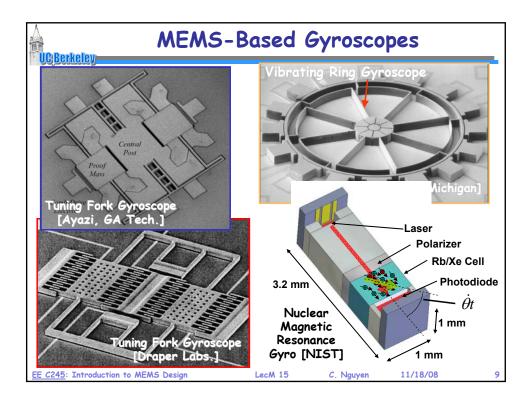


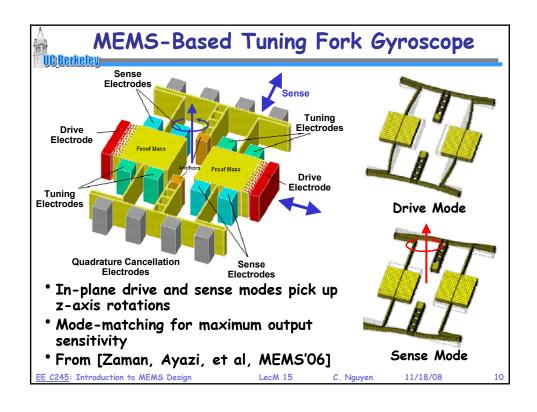


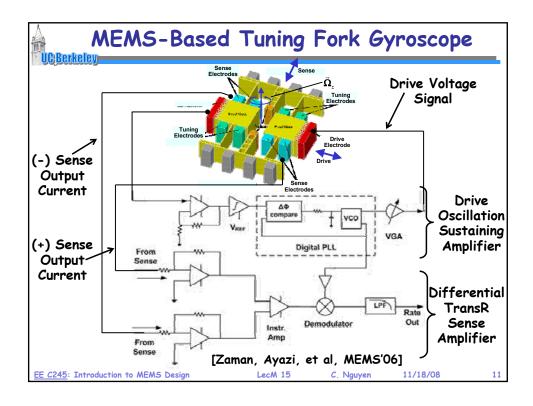


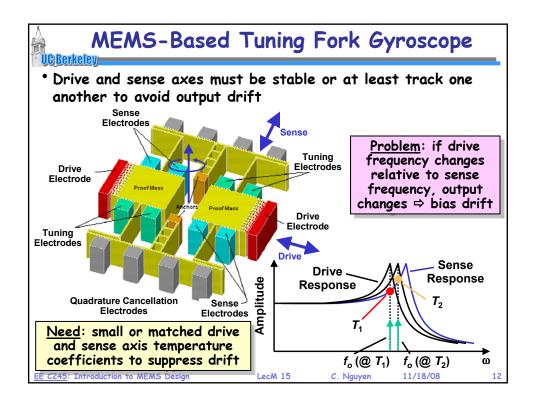


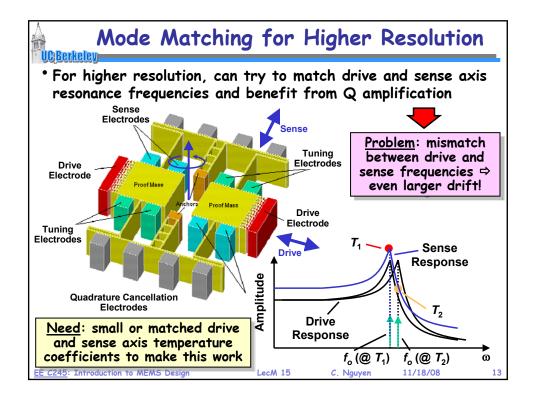


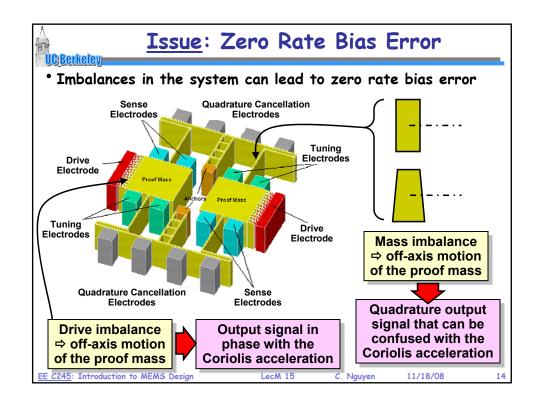


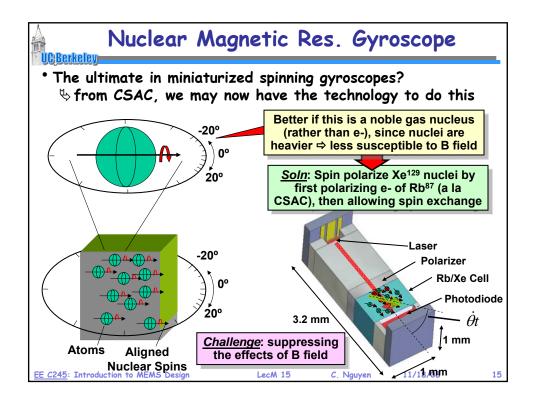


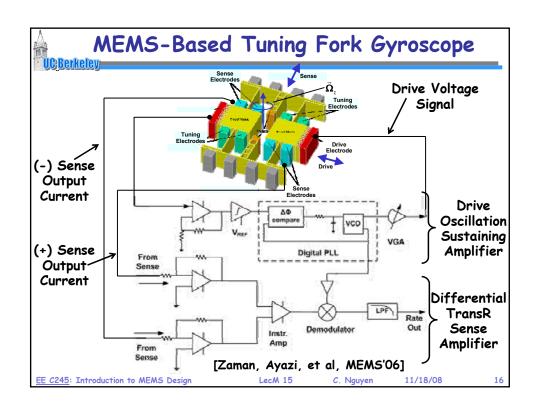


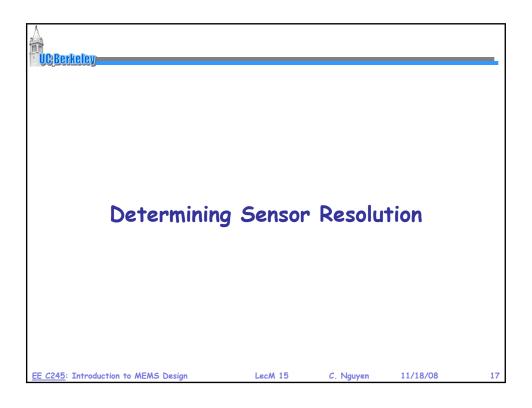


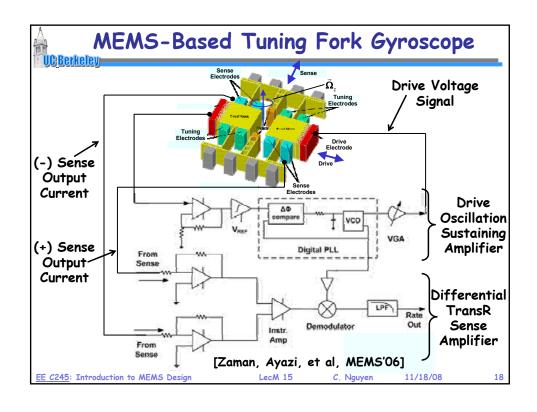


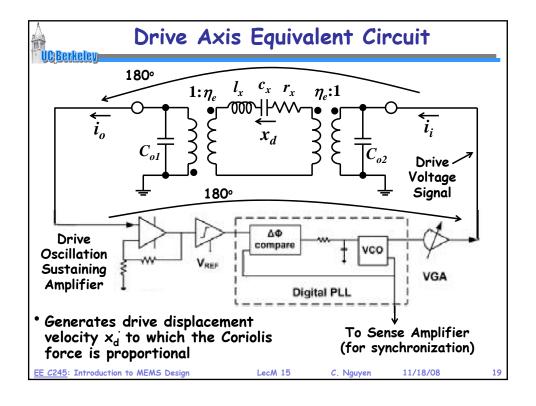


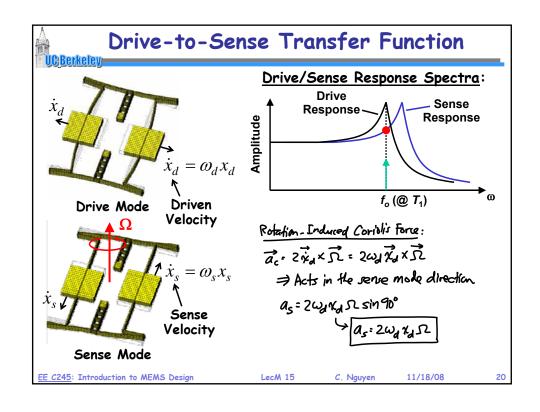




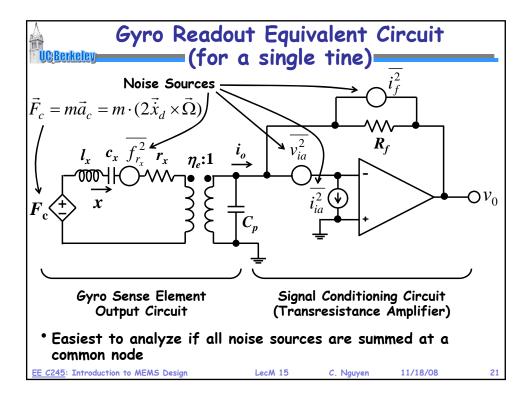


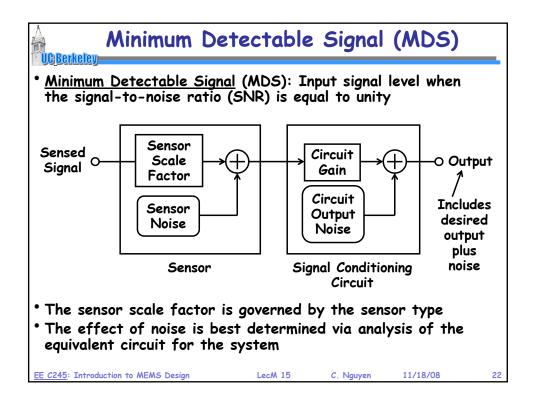




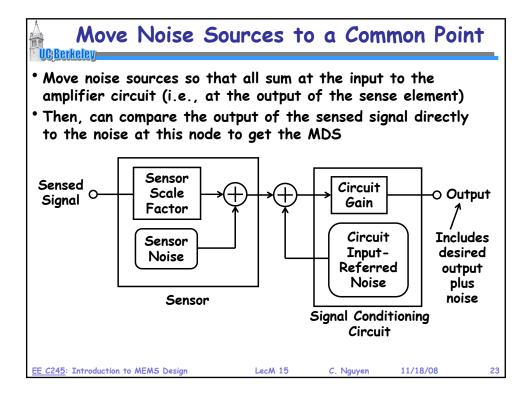


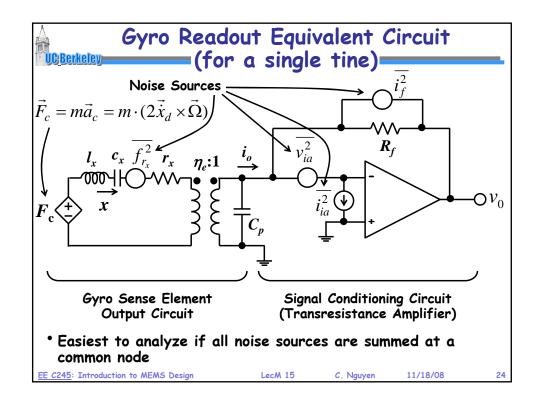
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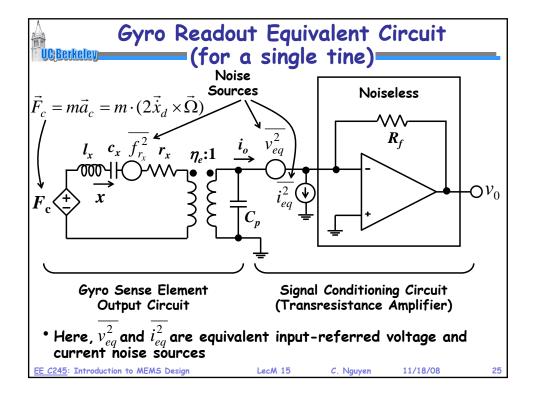


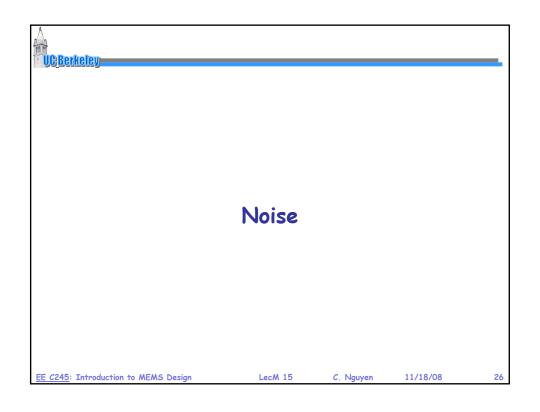


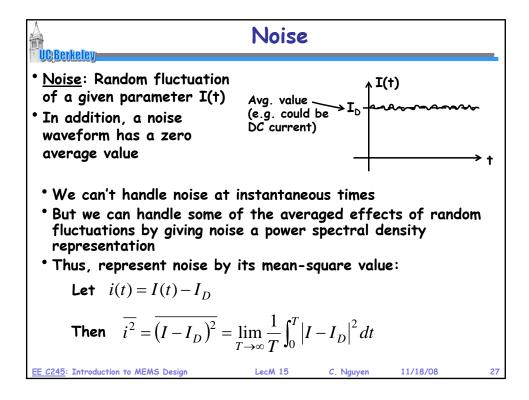
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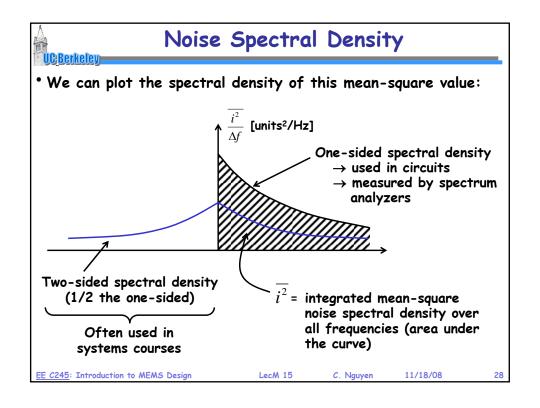


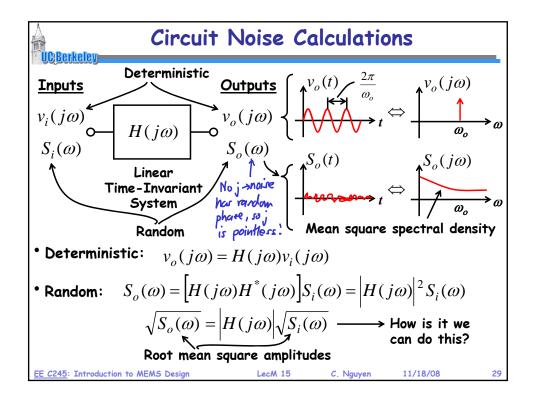


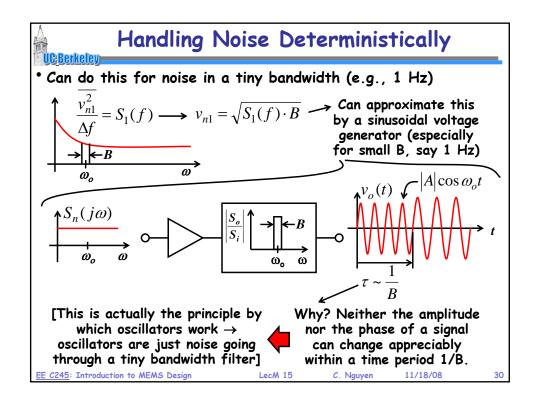


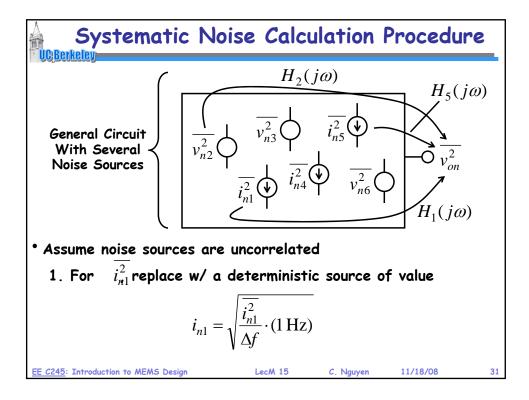


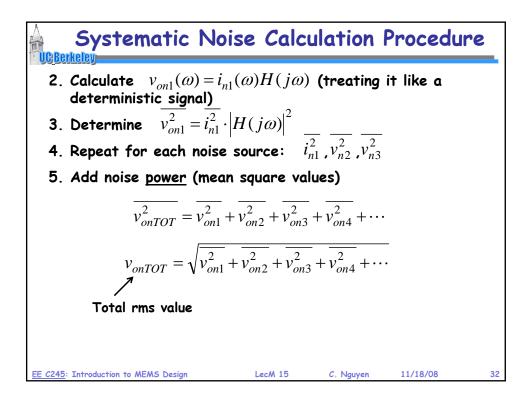


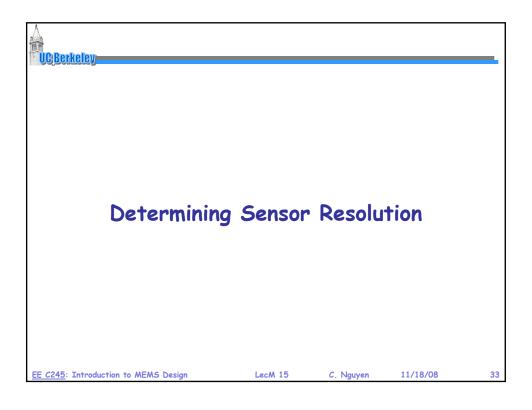


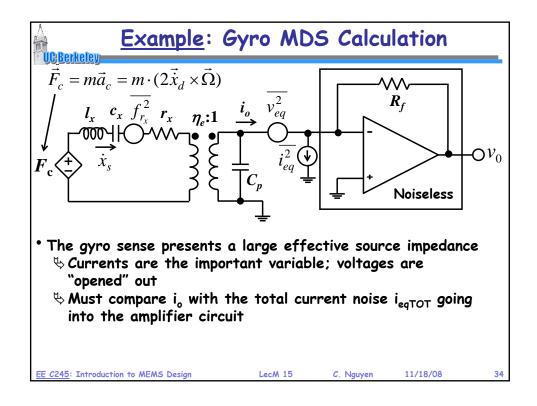


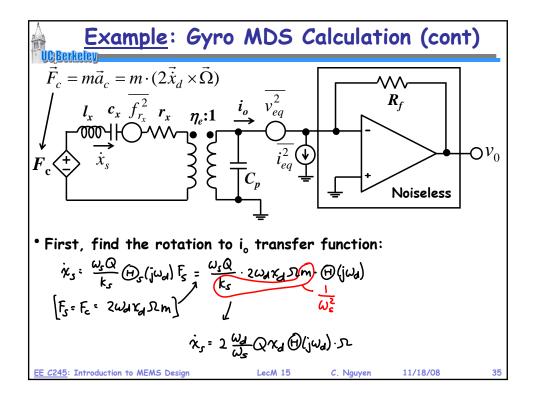


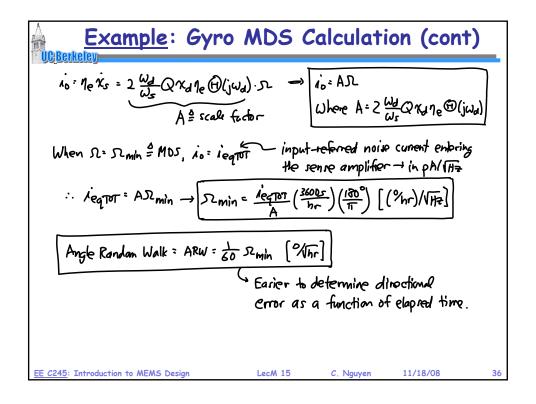


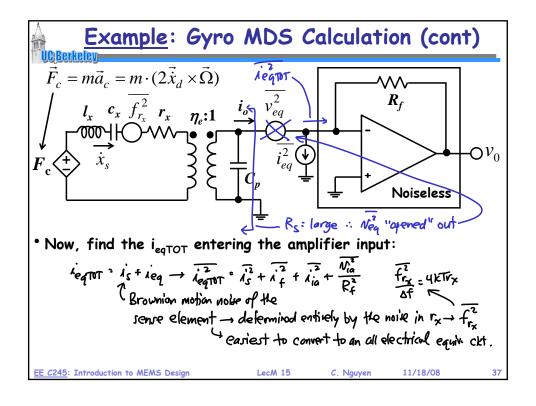


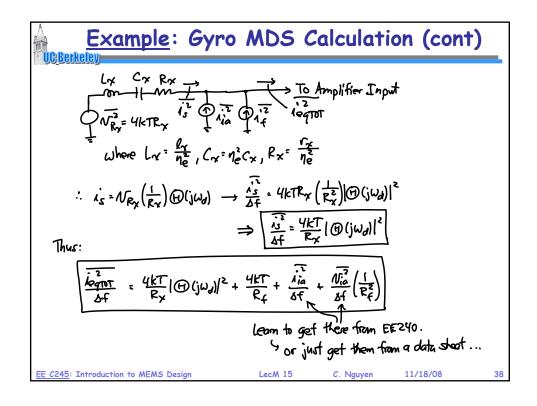


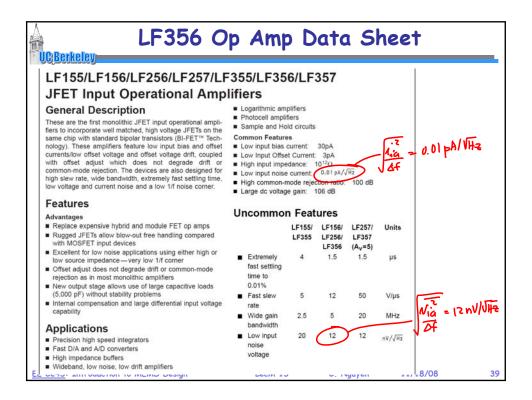


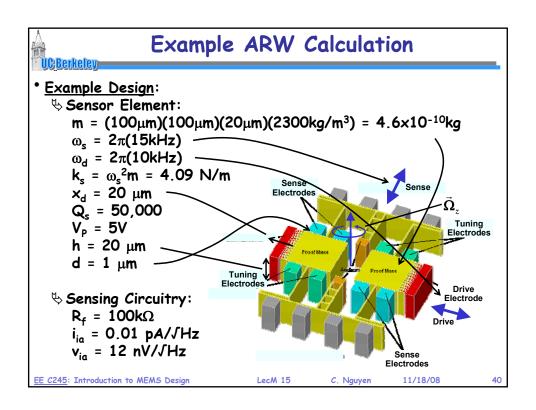












Example ARW Calculation (cont)

Get rotation rate to output current scale factor:

$$A = 2 \frac{\omega_d}{\omega_s} Q_s \chi_d \eta_e | \Theta(j\omega_d) | = 2 \frac{(0k)}{13k} (50k) (20\mu)(5)(25006_0)(0.00024) = 2.83 \times 10^{-12} C$$

$$\Theta(j\omega_d) = \frac{(j\omega_d)(\omega_s/\omega_s)}{-\omega_d^2 + j\omega_d\omega_s + \omega_s^2} = \frac{j(10k)(15k)/(50k)}{(15k)^2 - (10k)^2 + j(10k)(16k)} = \frac{j(3k)}{1.25 \times 10^{-8} + j(3k)}$$

$$\Rightarrow | \Theta(j\omega_d) | = \frac{3k}{\sqrt{(1.25 \times 10^{-8})^2 + (3k)^2}} = 0.000024$$

$$\frac{3k}{\sqrt{(1.25 \times 10^{-8})^2 + (3k)^2}} = 0.000024$$

Example ARW Calculation (cont)

$$\begin{bmatrix}
R_{Y} = \frac{\omega_{SM}}{Q_{y}^{2}} = \frac{2\pi I(1SK)(46x10^{-10})}{(50k)(8.83\pi 10^{-8})^{2}} = 110.6k\Omega
\end{bmatrix}$$

$$\frac{\lambda_{eqToT}}{Af} = \frac{(1.66\times10^{-20})}{(110.6k)}(0.000024)^{2} + \frac{(1.66\times10^{-20})}{1M} + \frac{(0.01p)^{2}}{(10.6k)}(0.01p)^{2} + \frac{(12n)^{2}}{(1M1)^{2}}$$
Senor element noise
Insignificant
$$\frac{\lambda_{eqToT}}{Af} = 1.68x10^{-26}A^{2}/Hz \rightarrow \lambda_{eqToT} = \frac{\lambda_{eqToT}}{Af} = 1.30x10^{-13}ANHz$$

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And finally:
$$\frac{\lambda_{eqToT}}{A} = \frac{\lambda_{eqToT}}{A} = \frac{\lambda_{$$

What if
$$\omega_{d} = \omega_{s}$$
?

If $\omega_{d} = \omega_{s} = 1.5KH^{2}$, then $|\mathbb{P}[j\omega_{d}]| = 1$ and

$$A = 2 \frac{\omega_{d}}{\omega_{s}} \mathcal{Q}_{s} \mathcal{K}_{d} \eta_{e} |\mathbb{P}[j\omega_{d}]| = 2 \mathcal{Q}_{s} \mathcal{K}_{d} \eta_{e} = 2(50K)(20\mu)(5)(200066) = 1.77 \times 10^{-7} \text{C}$$

$$\frac{\lambda_{eqTDT}}{\Delta f} = \frac{(1.66 \times 10^{-20})(1)^{2} + \frac{(1.66 \times 10^{-20})}{1M} + \frac{(0.61)^{2}}{(1M)^{2}} + \frac{(12h)^{2}}{(1M)^{2}}$$

Now, the senser element dominates!

$$\frac{\lambda_{eqTDT}}{\Delta f} = 1.67 \times 10^{-25} A^{2}/Hz \longrightarrow \lambda_{eqTDT} = \frac{\lambda_{eqTDT}}{\Delta f} = 4.08 \times 10^{-13} A/NHz$$

$$\therefore \mathcal{N}_{min} = \frac{\lambda_{eqTDT}}{A} \left(\frac{3600s}{hr}\right) \left(\frac{180^{\circ}}{1T}\right) = \frac{4.08 \times 10^{-13}}{(.77 \times 10^{-7})} (3600) \left(\frac{180^{\circ}}{1T}\right) = 0.476 \left(\frac{9}{hr}\right)/NHz$$

And finally:

$$ARW = \frac{1}{60} \mathcal{N}_{min} = \frac{1}{60} (0.476) = 0.0079 \frac{9}{Nhr} = ARW \Rightarrow 0.0036 = 0.0036 = 0.0079 \frac{9}{Nhr} = ARW \Rightarrow 0.0036 = 0.$$