


## EE C247B - ME C218 Introduction to MEMS Design Spring 2014

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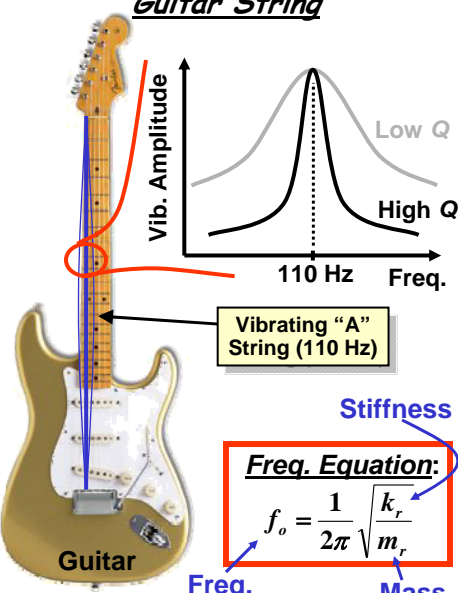
Lecture Module 2: Benefits of Scaling

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### Basic Concept: Scaling Guitar Strings

**Guitar String**



Vib. Amplitude

Low Q

High Q

110 Hz

Freq.

Vibrating "A" String (110 Hz)

**Freq. Equation:**

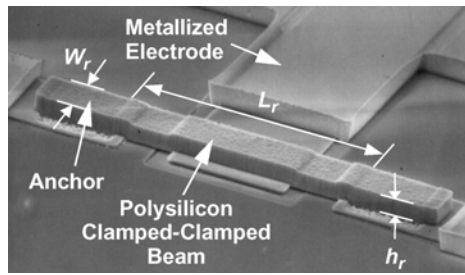
$$f_o = \frac{1}{2\pi} \sqrt{\frac{k_r}{m_r}}$$

Stiffness  $k_r$

Mass  $m_r$

Freq.

**$\mu$ Mechanical Resonator**



Metallized Electrode

Anchor

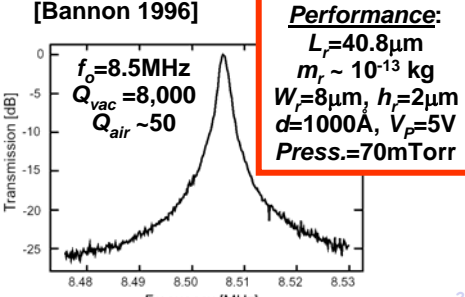
Polysilicon Clamped-Clamped Beam

$h_r$

[Bannon 1996]

Performance:

- $L_r = 40.8 \mu\text{m}$
- $m_r \sim 10^{-13} \text{ kg}$
- $W_r = 8 \mu\text{m}, h_r = 2 \mu\text{m}$
- $d = 1000 \text{ \AA}, V_p = 5 \text{ V}$
- Press. = 70 mTorr



Transmission [dB]

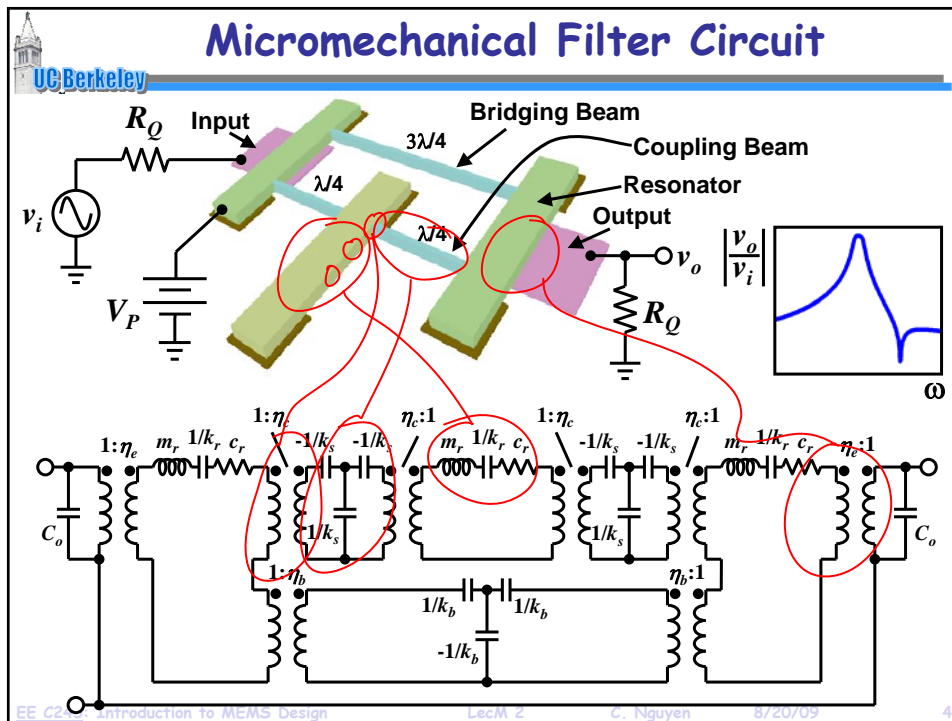
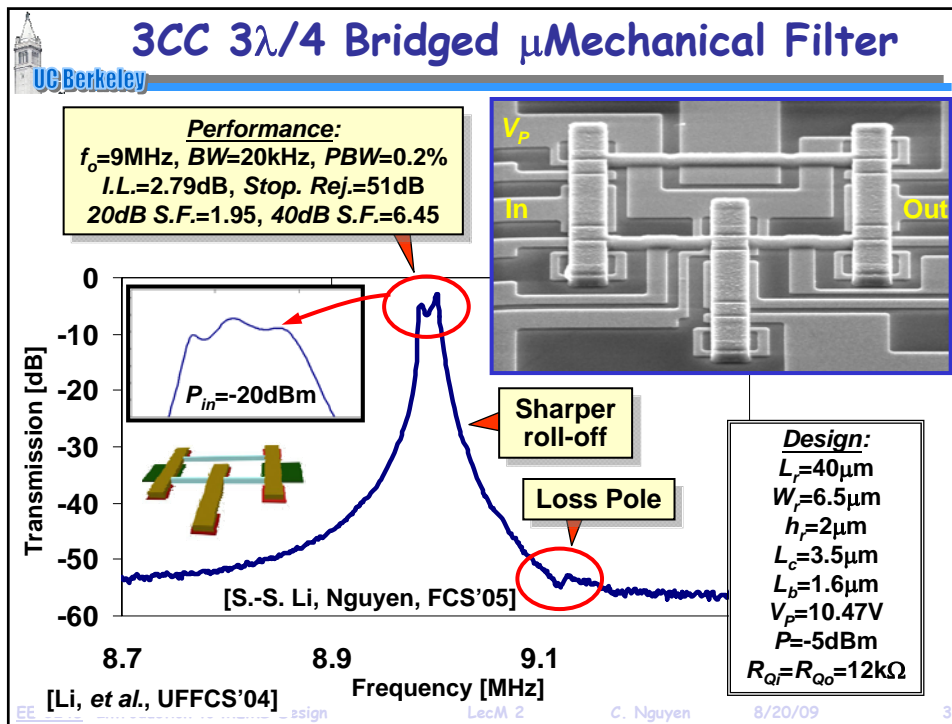
Frequency [MHz]

$f_o = 8.5 \text{ MHz}$

$Q_{vac} = 8,000$

$Q_{air} \sim 50$

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**1.51-GHz,  $Q=11,555$  Nanocrystalline Diamond Disk  $\mu$ Mechanical Resonator**

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- Impedance-mismatched stem for reduced anchor dissipation
- Operated in the 2<sup>nd</sup> radial-contour mode
- $Q \sim 11,555$  (vacuum);  $Q \sim 10,100$  (air)
- Below: 20  $\mu\text{m}$  diameter disk

**Design/Performance:**  
 $R=10\mu\text{m}$ ,  $t=2.2\mu\text{m}$ ,  $d=800\text{\AA}$ ,  $V_p=7\text{V}$   
 $f_o=1.51\text{ GHz}$  (2<sup>nd</sup> mode),  $Q=11,555$

Mixed Amplitude [dB]

Frequency [MHz]

$f_o = 1.51\text{ GHz}$   
 $Q = 11,555$  (vac)  
 $Q = 10,100$  (air)

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**163-MHz Differential Disk-Array Filter**

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Com. Array Couplers

Filter Coupler

Port1  $v_{i+}$

Port3  $v_{o+}$

Port2  $v_{i-}$

Port4  $v_{o-}$

Diff. Array Couplers

$V_p$

$\lambda/2$ ,  $\lambda/4$ ,  $\lambda$

[Li, Nguyen Trans'07]

### Linear MEMS in Wireless Comms

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High Q and good linearity of micromechanical resonators

➔

Filters for front-end frequency selection

**Micromechanical Bandpass Filter**

Transmission [dB]

Frequency [MHz]

Antenna Diplexer From TX RF BPF LNA Mixer I LPF AGC A/D Mixer Q LPF AGC A/D RXRF LO RF PLL Xstal Osc

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### Miniaturization of RF Front Ends

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RF Power Amplifier

Diplexer

897.5±17.5MHz RF SAW Filter

925-960MHz RF SAW Filter

Dual-Band Zero-IF Transistor Chip

1805-1880MHz RF SAW Filter

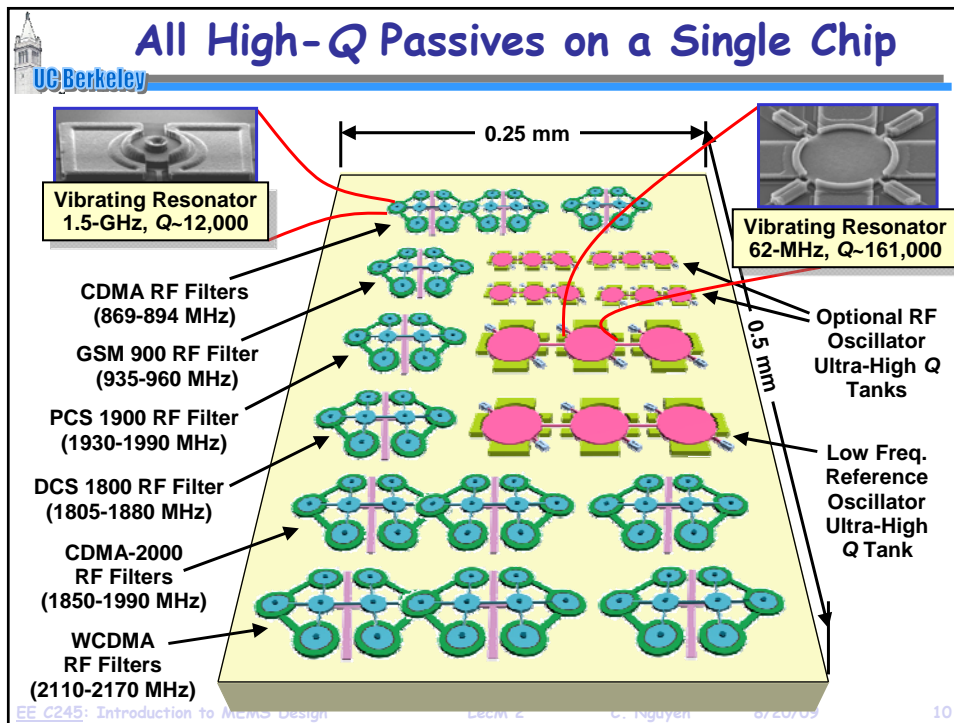
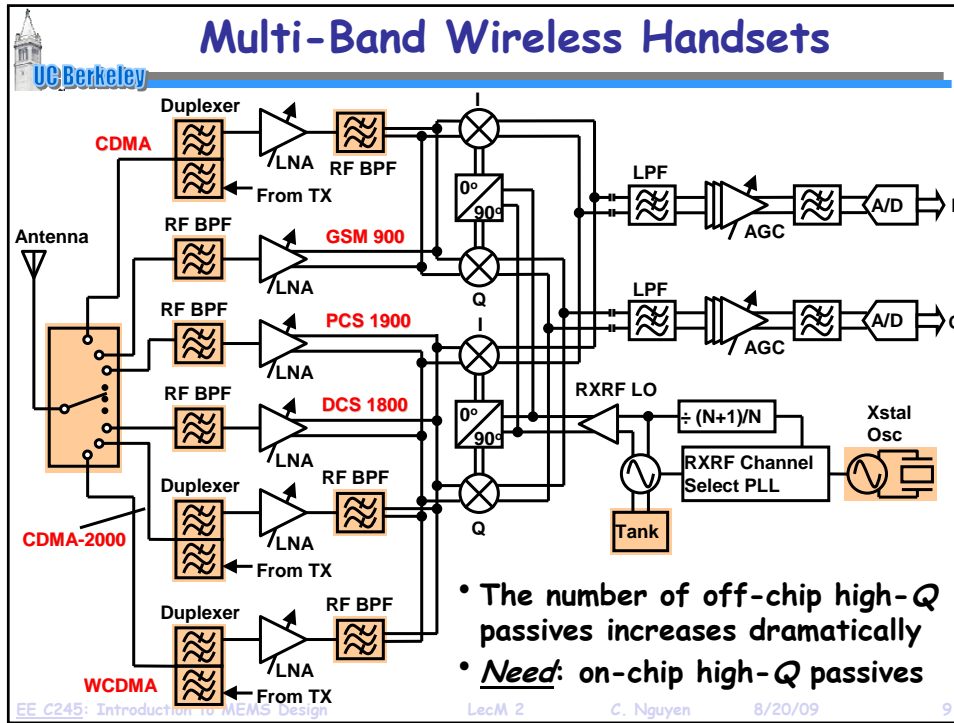
3420-3840MHz VCO

26-MHz Xstal Oscillator

**Problem: high-Q passives pose a bottleneck against miniaturization**

Antenna Diplexer From TX RF BPF LNA Mixer I LPF AGC A/D Mixer Q LPF AGC A/D RXRF LO RF PLL Xstal Osc

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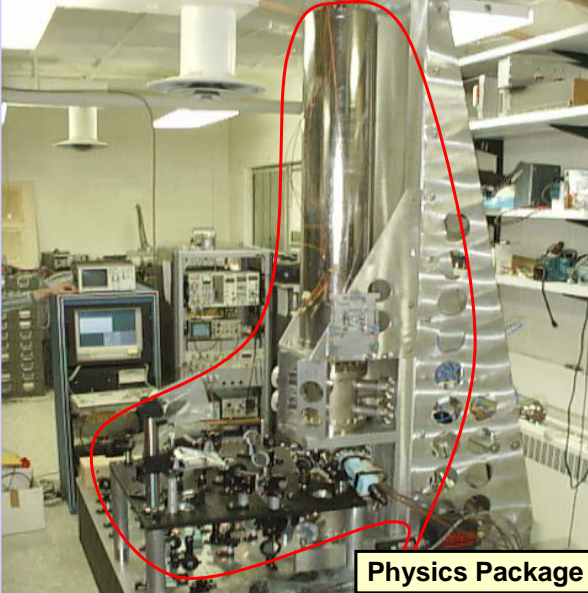
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## Chip-Scale Atomic Clocks (CSAC)

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## NIST F1 Fountain Atomic Clock



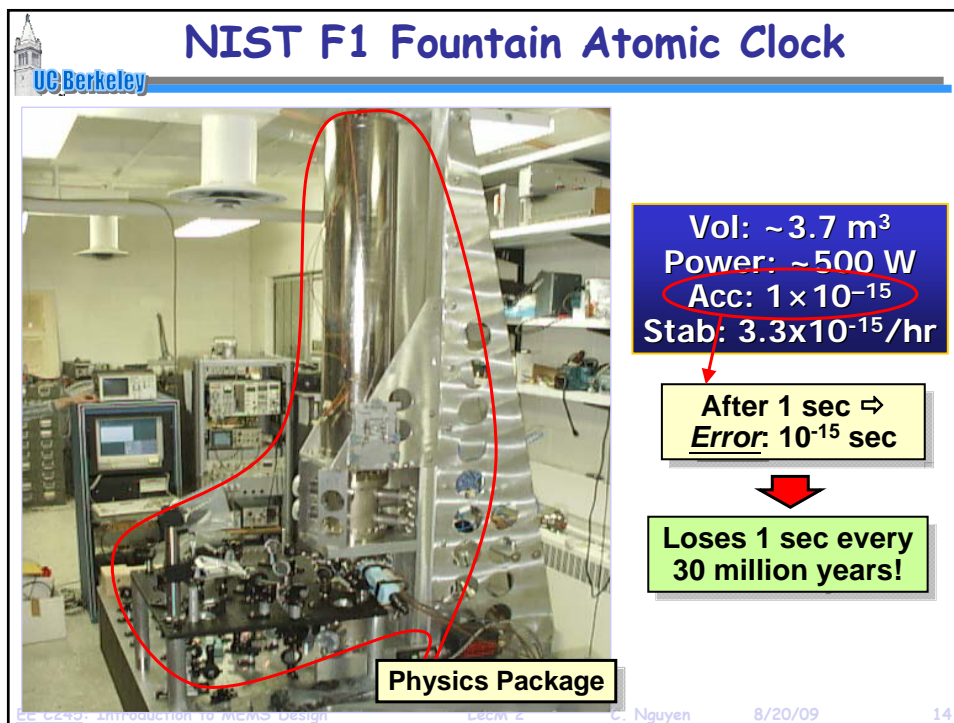
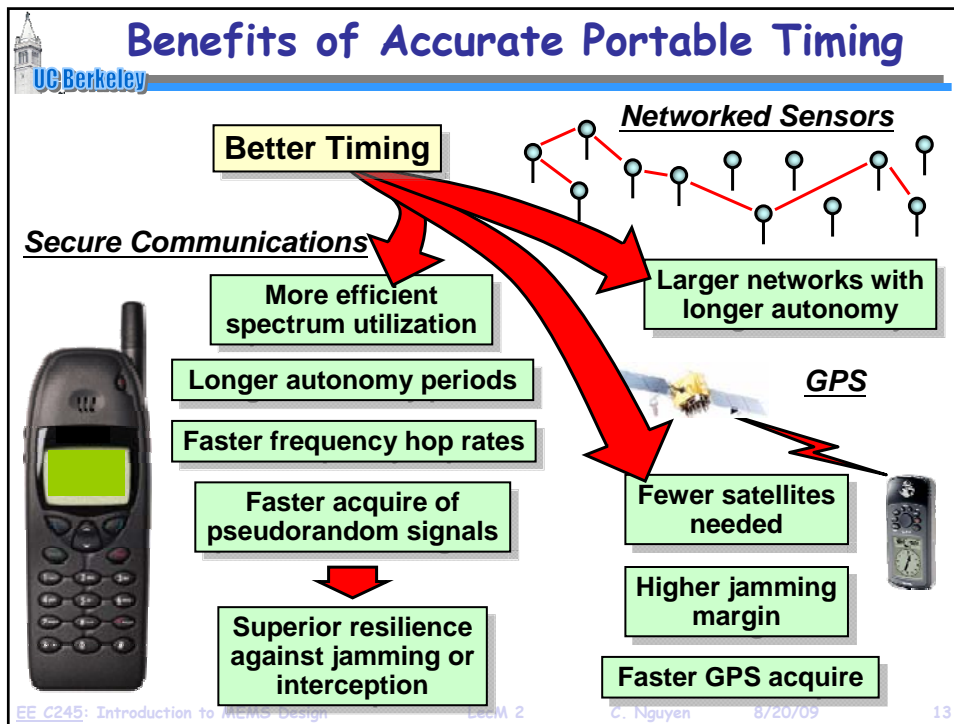
Vol:  $\sim 3.7 \text{ m}^3$   
Power:  $\sim 500 \text{ W}$   
Acc:  $1 \times 10^{-15}$   
Stab:  $3.3 \times 10^{-15} / \text{hr}$

After 1 sec  $\Rightarrow$   
Error:  $10^{-15}$  sec

Loses 1 sec every  
30 million years!

Physics Package

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### 1<sup>st</sup> Chip-Scale Atomic Physics Package

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**Total Volume:** 9.5 mm<sup>3</sup>

**Cell Interior Vol:** 0.6 mm<sup>3</sup>

**Stability:** 2.4 x 10<sup>-10</sup> @ 1s

**Power Cons:** 75 mW

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### Tiny Physics Package Performance

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**Dime**

**NIST's Chip-Scale Atomic Physics Package**

**Open Loop Resonance:**

**Q = 1.3x10<sup>6</sup>**

**7.1 kHz**

**Contrast: 0.91%**

**Sufficient to meet CSAC program goals**

- **Experimental Conditions:**
- Cs D<sub>2</sub> Excitation
- External (large) Magnetic Shielding
- External Electronics & LO
- Cell Temperature: ~80 °C
- Cell Heater Power: 69 mW
- Laser Current/Voltage: 2mA / 2V
- RF Laser Mod Power: 70μW

**Stability Measurement:**

**Allan Deviation,  $\sigma_y$**

**Integration Time,  $\tau$  [s]**

**Cs (D<sub>2</sub>)**

**Rb (D<sub>1</sub>)**

**Drift Issue**

**CSAC Goal**

**1 hour**

**1 day**

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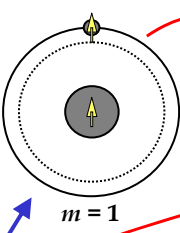


### Atomic Clock Fundamentals

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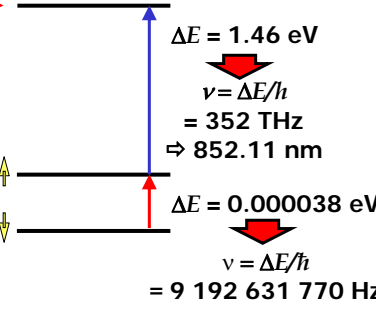
- Frequency determined by an atomic transition energy

**Excite e- to the next orbital**



$m = 1$

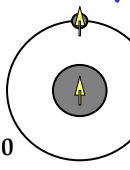
**Energy Band Diagram**



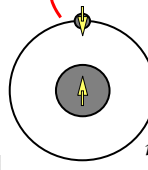
$\Delta E = 1.46 \text{ eV}$   
 $\nu = \Delta E/h = 352 \text{ THz}$   
 $\Rightarrow 852.11 \text{ nm}$

$\Delta E = 0.000038 \text{ eV}$   
 $\nu = \Delta E/h = 9\,192\,631\,770 \text{ Hz}$

$m = 0$   
 $f = 4$



**Opposite e- spins**



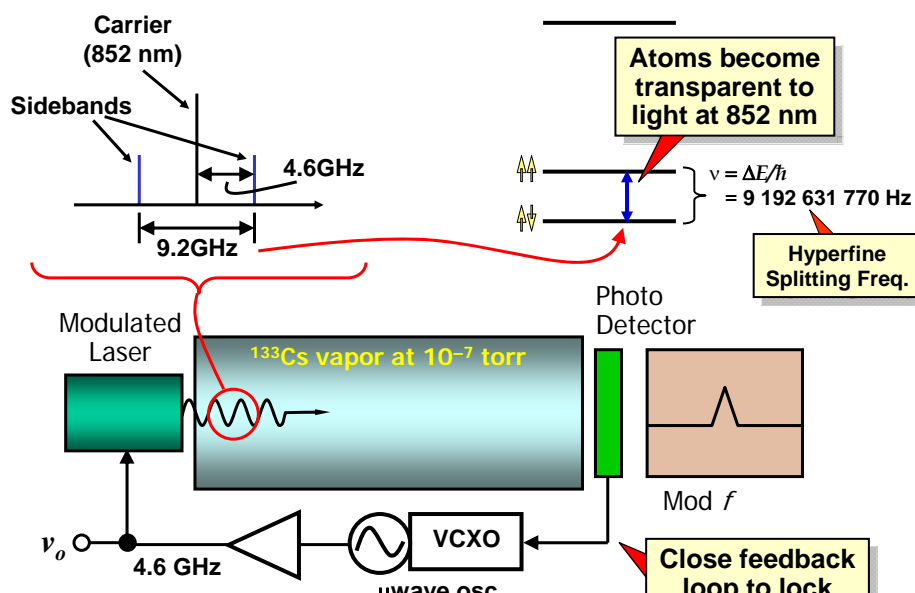
$m = 0$   
 $f = 3$

$^{133}\text{Cs}$

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### Miniature Atomic Clock Design

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**Carrier (852 nm)**  
**Sidebands**  
 4.6GHz  
 9.2GHz

**Atoms become transparent to light at 852 nm**

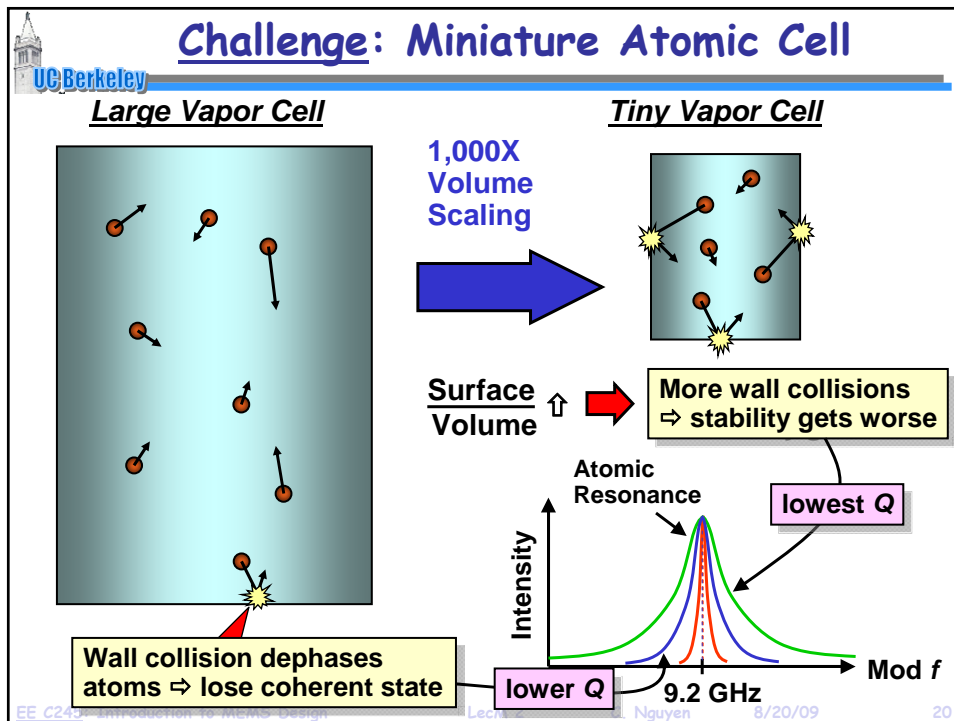
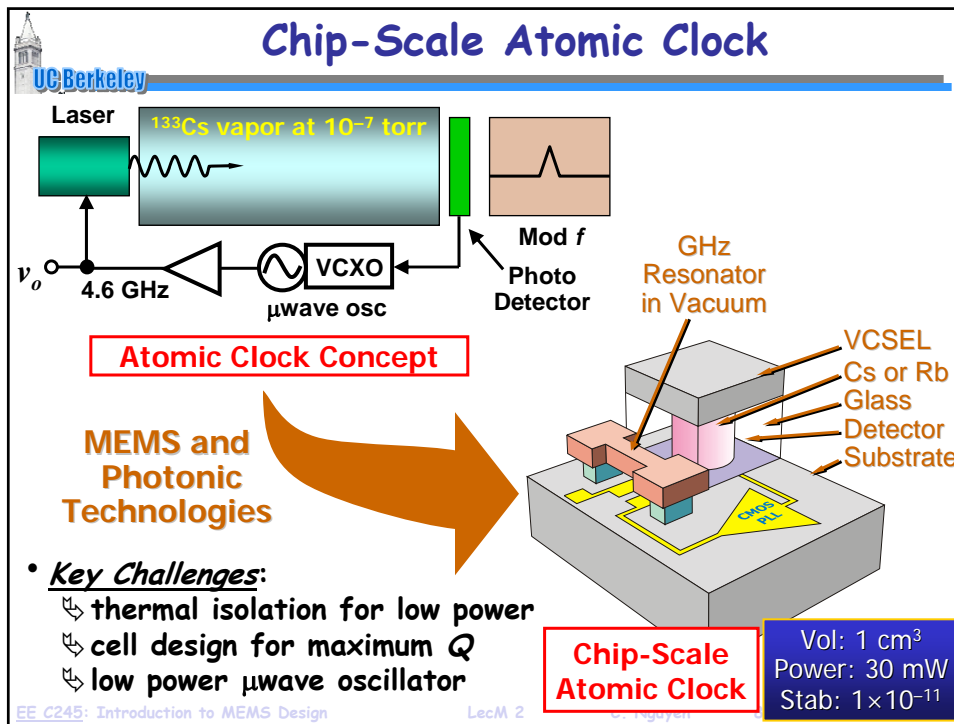
$\nu = \Delta E/h = 9\,192\,631\,770 \text{ Hz}$   
**Hyperfine Splitting Freq.**

**Modulated Laser**  
 $^{133}\text{Cs vapor at } 10^{-7} \text{ torr}$   
**Photo Detector**

$\nu_o$     4.6 GHz    **VCXO**     $\mu\text{wave osc}$

**Close feedback loop to lock**

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**Challenge: Miniature Atomic Cell**

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Large Vapor Cell

1,000X  
Volume  
Scaling

➔

Tiny Vapor Cell

Buffer Gas

**Soln:** Add a buffer gas

➔ Lower the mean free path of the atomic vapor

Atomic Resonance

Intensity

Mod  $f$

9.2 GHz

Return to higher Q

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**Chip-Scale Atomic Clock**

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**Atomic Clock Concept**

VCSEL  
Cs or Rb  
Glass  
Detector  
Substrate

**MEMS and Photonic Technologies**

- **Key Challenges:**
  - ↳ thermal isolation for low power
  - ↳ cell design for maximum Q
  - ↳ low power  $\mu$ wave oscillator

**Chip-Scale Atomic Clock**

Vol: 1 cm<sup>3</sup>  
Power: 30 mW  
Stab: 1 × 10<sup>-11</sup>

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