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| Oxidation Modeling (cont.)  |                                |
|---|--------------------------------|
| Find an expression for $X_{OX}(t)$ : oxidizing  | flux                           |
| Rate of change of oxide $\left\{ = \frac{dX_{OX}}{dt} = \frac{J}{M} = \frac{DN_O}{X_{OX} + M} \right\}$   | $\frac{dM}{D/k_s}$ (3)         |
| # of molecules of oxidizing<br>species incorporated into a<br>unit volume of oxide $\begin{cases} = 2.2 \times 10^{22} cm^{-3} \\ = 4.4 \times 10^{22} cm^{-3} \end{cases}$ | for $O_2$<br>for $H_2O$        |
| Solve (3) for $X_{OX}(t)$ : [Initial condition $X_{OX}(t=0)$  | $\mathbf{D}) = X_i \mathbf{J}$ |
| $\frac{dX_{OX}}{dt} = \frac{DN_O/M}{X_{OX} + D/k_s}  \text{ar} \int_{X_i}^{X_{OX}} \left(X_{OX} + \frac{D}{k_s}\right) dX_{OX} = \int_0^t \frac{1}{2} \frac{dX_{OX}}{dt}$   | $\frac{DN_o}{M} dt$            |
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| UCBerkeley       | Oxide Thickness Versus Time   |
|------------------|---|
| <u>Result</u> :  |   |
| addit<br>( to ga | tional time required $f$ time required to grow $X_i$<br>o from $X_i \rightarrow X_{OY}$ $f$ [X = initial oxide thickness] |
| X <sub>OX</sub>  | $(t) = \frac{A}{2} \left\{ \left[ 1 + \frac{4B}{A^2} (t + \tau) \right]^{\frac{1}{2}} - 1 \right\}$                       |
| where            | $A = \frac{2D}{k_s} \qquad \qquad \tau = \frac{X_i^2}{B} + \frac{X_i}{(B/A)}$   |
|                  | $B = \frac{2DN_o}{M} \qquad D = D_o \exp\left(-\frac{E_A}{kT}\right)$   |
|                  | i.e., D governed by an Arrhenius relationship $\rightarrow$ temperature dependent   |
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| Table 6–2                          | Rate constants describing (111) silicon oxidation kinetics at 1 Atm total pressure. For the corresponding values for (100) silicon, all C2 values should be divided by 1.68. |  |  |
|------------------------------------|--|--|--|
| Ambient                            | B  | B/A  |  |
| Dry O <sub>2</sub>                 | $C_1 = 7.72 \times 10^2 \mu \mathrm{m}^2 \mathrm{hr}^{-1}$   | $C_2 = 6.23 \times 10^6 \mu\mathrm{m}\mathrm{hr}^{-1}$ |  |
|                                    | $E_1 = 1.23 \text{ eV}$  | $E_2 = 2.0  \mathrm{eV}$                               |  |
| Wet O <sub>2</sub>                 | $C_1 = 2.14 \times 10^2 \mu \mathrm{m}^2 \mathrm{hr}^{-1}$   | $C_2 = 8.95 \times 10^7 \mu\mathrm{m}\mathrm{hr}^{-1}$ |  |
|                                    | $E_1 = 0.71 \text{ eV}$  | $E_2 = 2.05 \text{ eV}$                                |  |
| H <sub>2</sub> O                   | $C_1 = 3.86 \times 10^2 \mu \mathrm{m}^2 \mathrm{hr}^{-1}$   | $C_2 = 1.63 \times 10^8 \mu\mathrm{m}\mathrm{hr}^{-1}$ |  |
|                                    | $E_1 = 0.78 \mathrm{eV}$   | $E_2 = 2.05  \mathrm{eV}$                              |  |
| ve theor<br>1 in prac<br>2ather, ( | ry is great but usually,<br>tice, since measured dat<br>oxidation growth charts o  | the equations are i<br>a is available<br>are used      |  |

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