Module 12: Capacitive Transducers



EE C247B - ME C218 Introduction to MEMS Design Spring 2015

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<u>Lecture Module 12</u>: Capacitive Transducers

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Lecture Outline

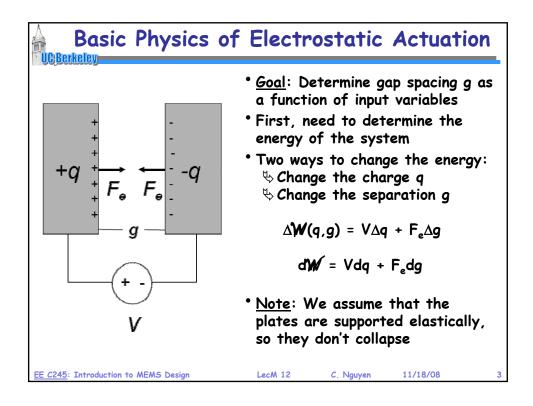
- Reading: Senturia, Chpt. 5, Chpt. 6
- Lecture Topics:
 - ♥ Energy Conserving Transducers
 - Charge Control
 - ◆ Voltage Control
 - Parallel-Plate Capacitive Transducers
 - Linearizing Capacitive Actuators
 - Electrical Stiffness
 - - ◆ 1st Order Analysis
 - ◆ 2nd Order Analysis

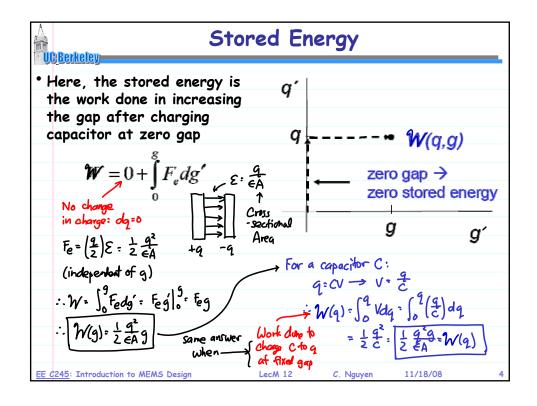
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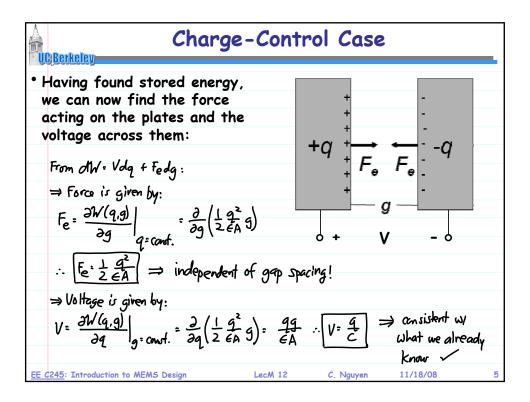
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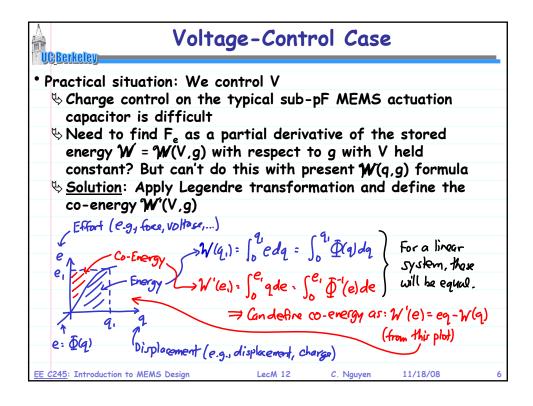
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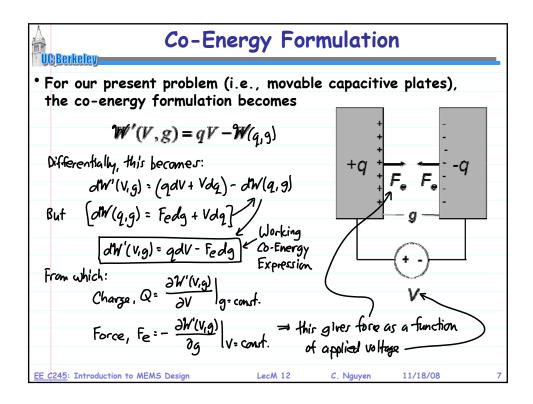
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Electrostatic Force (Voltage Control)

• Find co-energy in terms of voltage (w) gap held constant)

$$\mathcal{W}' = \int_{0}^{v} q(g, V') dV' = \int_{0}^{v} \left(\varepsilon \frac{A}{g} \right) V' dV' = \frac{1}{2} \left(\frac{\varepsilon A}{g} \right) V^{2} = \frac{1}{2} C V^{2}$$
(as expected)

 Variation of co-energy with respect to gap yields electrostatic force:

$$F_{v} = -\frac{\partial W'(V,g)}{\partial g}\bigg|_{V} = -\frac{1}{2} \left(-\frac{\varepsilon A}{g^{2}}\right) V^{2} = \frac{1}{2} \frac{C}{g} V^{2}$$
strong function of gap!

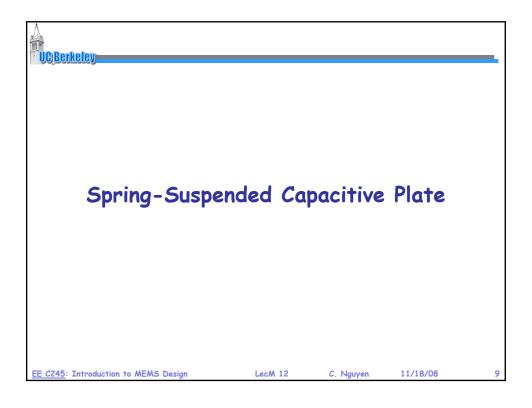
 Variation of co-energy with respect to voltage yields charge:

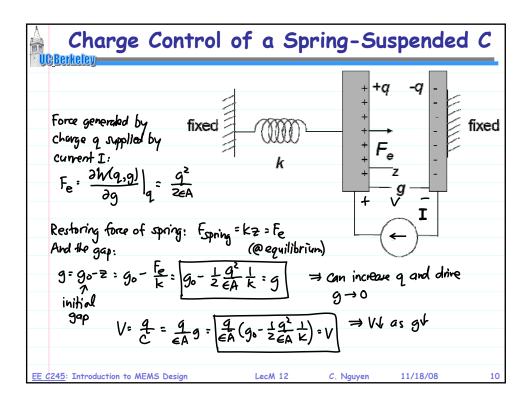
$$q = \frac{\partial W'(V,g)}{\partial V}\Big|_{g} = \left(\frac{\varepsilon A}{g}\right)V = CV$$
 as expected

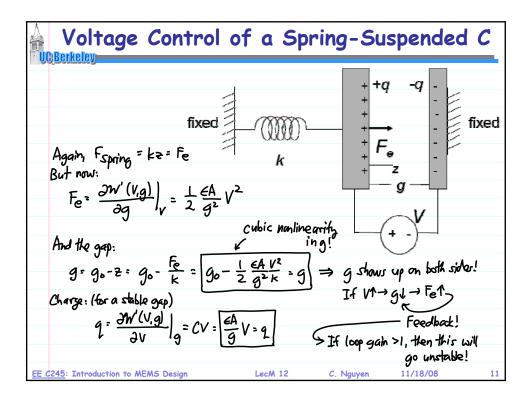
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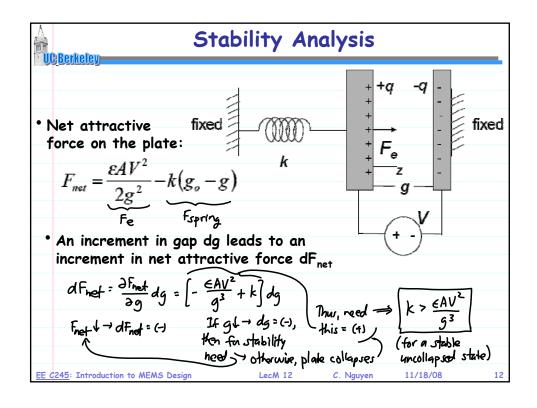
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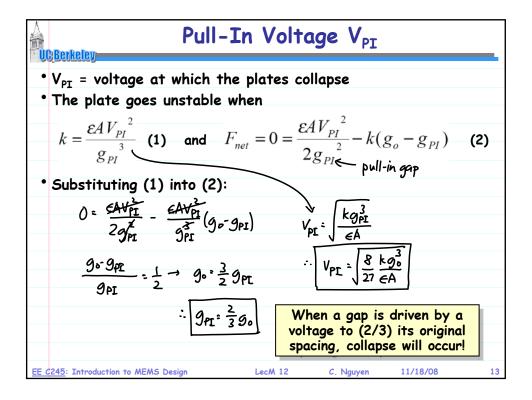
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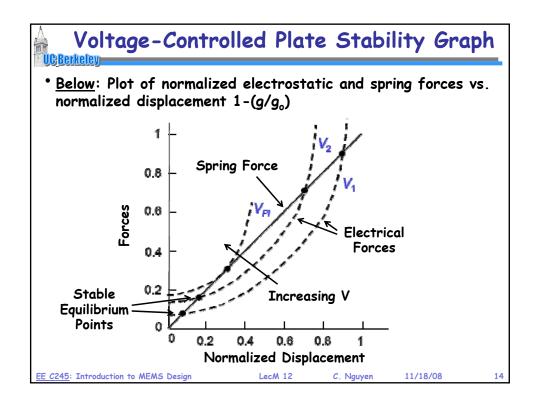












Module 12: Capacitive Transducers

Advantages of Electrostatic Actuators

- Easy to manufacture in micromachining processes, since conductors and air gaps are all that's needed → low cost!
- Energy conserving \rightarrow only parasitic energy loss through I²R losses in conductors and interconnects
- Variety of geometries available that allow tailoring of the relationships between voltage, force, and displacement
- Electrostatic forces can become very large when dimensions shrink \rightarrow electrostatics scales well!
- Same capacitive structures can be used for both drive and sense of velocity or displacement
- Simplicity of transducer greatly reduces mechanical energy losses, allowing the highest Q's for resonant structures

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Problems With Electrostatic Actuators

- * Nonlinear voltage-to-force transfer function
- Relatively weak compared with other transducers (e.g., piezoelectric), but things get better as dimensions scale

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