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EE C247B – ME C218
Introduction to MEMS Design
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Lecture Module 9: Energy Methods

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Lecture Outline

- Reading: Senturia, Chpt. 10
- Lecture Topics:
  - ⌦ Energy Methods
    - ☛ Virtual Work
    - ☛ Energy Formulations
    - ☛ Tapered Beam Example

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Energy Methods

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More General Geometries

- Euler-Bernoulli beam theory works well for simple geometries
- But how can we handle more complicated ones?
- Example: tapered cantilever beam
- Objective: Find an expression for displacement as a function of location x under a point load F applied at the tip of the free end of a cantilever with tapered width W(x)

Top view of cantilever's W(x)

$$W(x) = W(1 - \frac{x}{2L_c})$$

50% taper

$x = L_c$

Solution: Use Principle of Virtual Work

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- In an energy-conserving system (i.e., elastic materials), the energy stored in a body due to the quasi-static (i.e., slow) action of surface and body forces is equal to the work done by these forces …

- Implication: if we can formulate **stored energy** as a function of the deformation of a mechanical object, then we can determine how an object responds to a force by determining the shape the object must take in order to **minimize** the **difference U** between the stored energy and the work done by the forces:

U = Stored Energy - Work Done

- Key idea: we don't have to reach U = 0 to produce a very useful, approximate *analytical* result for load-deflection

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