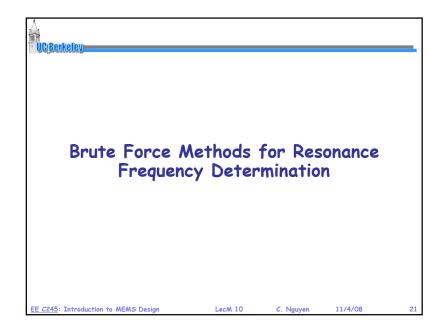
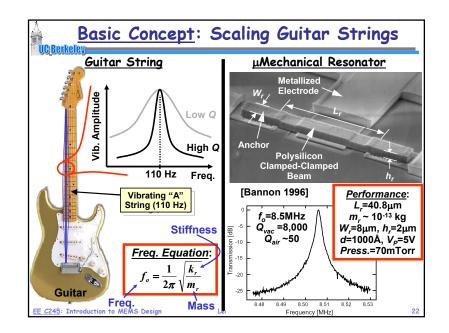
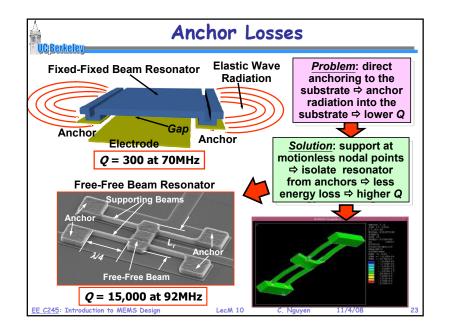
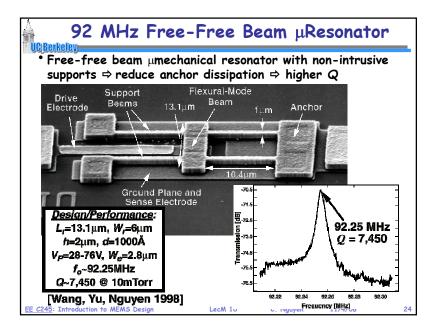
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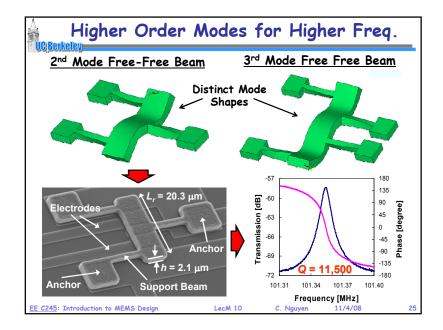


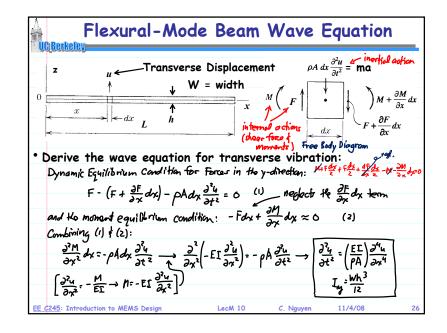


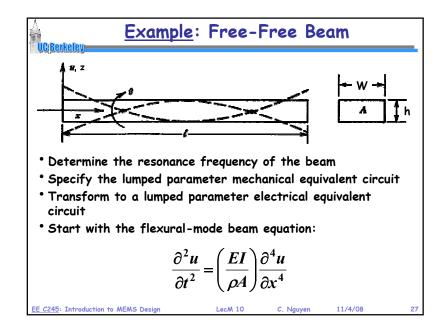
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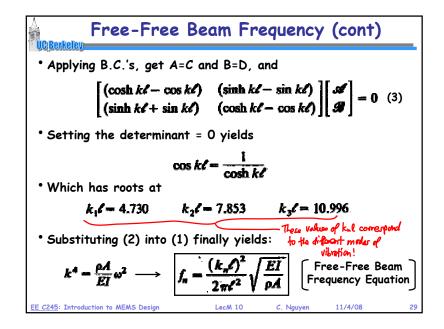




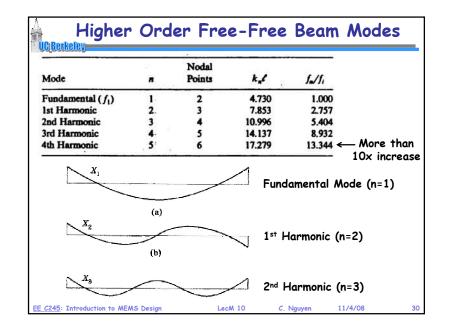
Gerkeley	ee-Free I	Beam Frequency	
• Substitute u = ($u_1 e^{j \omega t}$ into the	wave equation:	
	$\frac{\partial^4 u}{\partial x^4} = \left(u \right)^4$	$r^2 \frac{\rho A}{EI} \bigg) u$	(1)
• This is a 4 th ord	der differenti	al equation with solution:	
u(x) = st co Giver - * <u>Boundary Condit</u>	sh kx + <i>St</i> sinl to mole shape duri <u>rions</u> :	a kx + & cos kx + Ø sin kx ng resonance vibation.	(2)
	At $x = \ell$		
$\frac{\partial^2 u}{\partial x^2} = 0$ $\frac{\partial^3 u}{\partial x^3} = 0$	$\frac{\partial^2 u}{\partial x^2} = 0$ $\frac{\partial^3 u}{\partial x^3} = 0$	M = 0 (Bending moment) $\frac{\partial M}{\partial x} = 0$ (Shearing force))
dx ³ EE C245: Introduction to MEMS I		dx ecM 10 C. Nguyen 11/4/08	28

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Mode Shape Expression				
• The mode shape express fact that A=C and B=D	ion can be obtained by using the into (2), yielding			
$u_x = \mathscr{R}\left[\left(\frac{\mathscr{A}}{\mathscr{B}}\right)(\cosh kx + \cos kx) + (\sinh kx + \sin kx)\right]$				
 Get the amplitude ratio by expanding (3) [the matrix] and solving, which yields 				
$\frac{\mathcal{A}}{\mathcal{A}} = \frac{\sin kl - \sinh kl}{\cosh kl - \cos kl}$				
 Then just substitute the roots for each mode to get the expression for mode shape 				
	Fundamental Mode (n=1)			
[Substitute k ₁ = 4.730]				
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