

# EE C247B - ME C218 Introduction to MEMS Design Spring 2016

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Lecture Module 12: Capacitive Transducers

EE C245: Introduction to MEMS Design

LecM 12

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## UC Berkeley,

### Lecture Outline

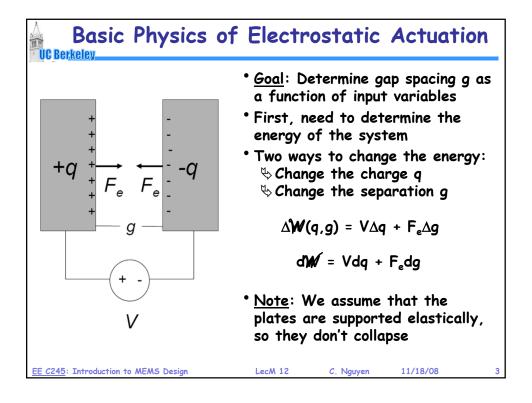
- \* Reading: Senturia, Chpt. 5, Chpt. 6
- Lecture Topics:
  - \$ Energy Conserving Transducers
    - ◆ Charge Control
    - ◆ Voltage Control
  - ♦ Parallel-Plate Capacitive Transducers
    - Linearizing Capacitive Actuators
    - Electrical Stiffness
  - - ◆ 1<sup>st</sup> Order Analysis
    - ◆ 2<sup>nd</sup> Order Analysis

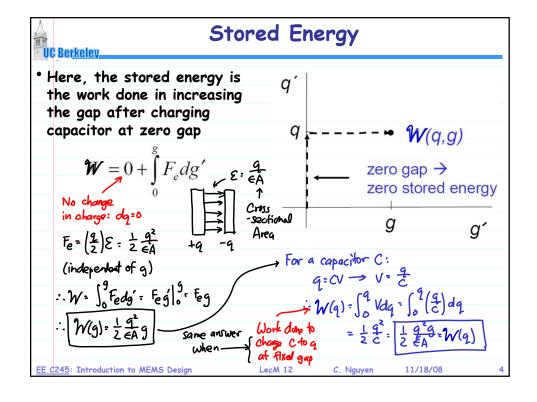
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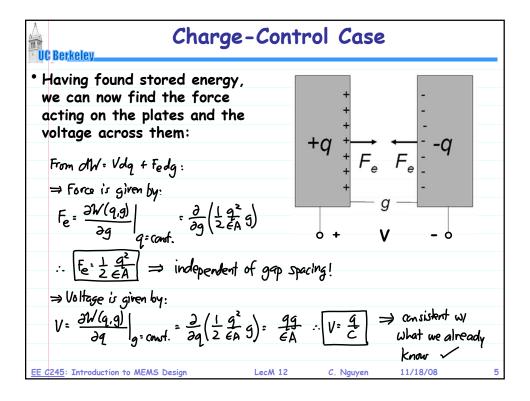
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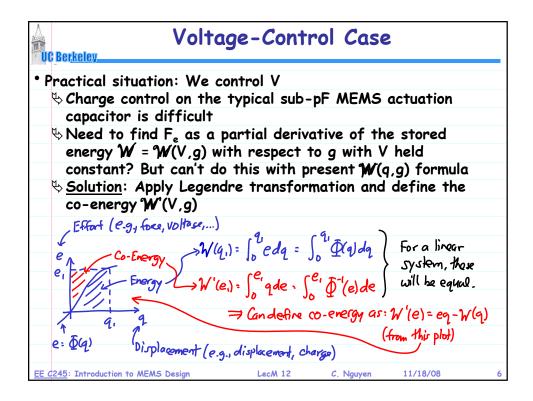
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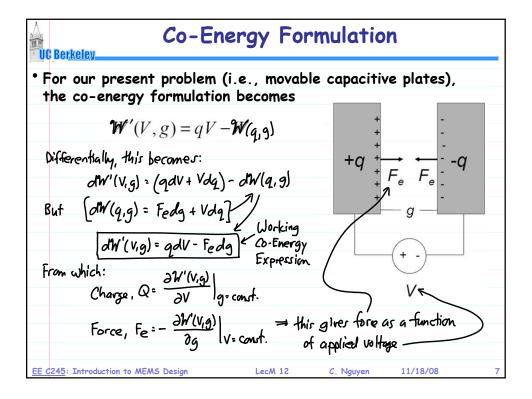
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## Electrostatic Force (Voltage Control)

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• Find co-energy in terms of voltage (w) gap held constant)

$$\mathbf{W}' = \int_{0}^{V} q(g, V') dV' = \int_{0}^{V} \left( \varepsilon \frac{A}{g} \right) V' dV' = \frac{1}{2} \left( \frac{\varepsilon A}{g} \right) V^{2} = \frac{1}{2} CV^{2}$$
(as expected)

 Variation of co-energy with respect to gap yields electrostatic force:

$$F_e = -\frac{\partial W'(V,g)}{\partial g}\bigg|_V = -\frac{1}{2} \left(-\frac{\varepsilon A}{g^2}\right) V^2 = \frac{1}{2} \frac{C}{g} V^2$$
strong function of gap

 Variation of co-energy with respect to voltage yields charge:

$$q = \frac{\partial W'(V,g)}{\partial V}\Big|_{\sigma} = \left(\frac{\varepsilon A}{g}\right)V = CV$$
 as expected

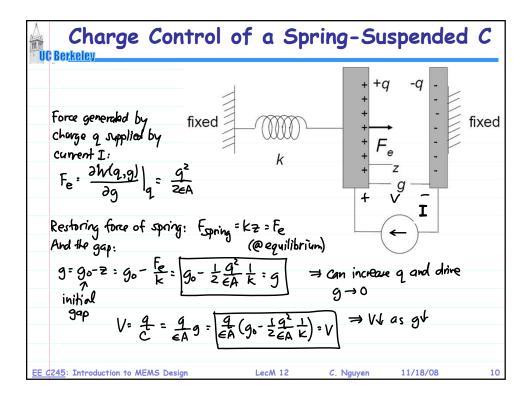
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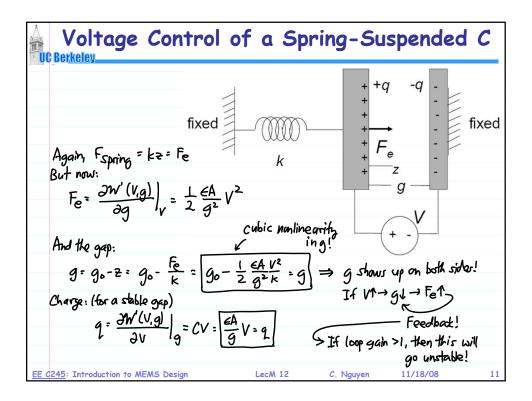
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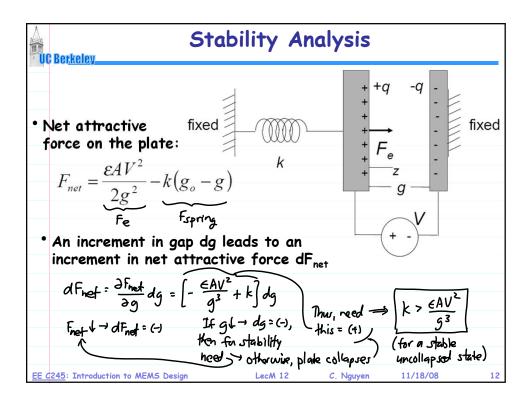
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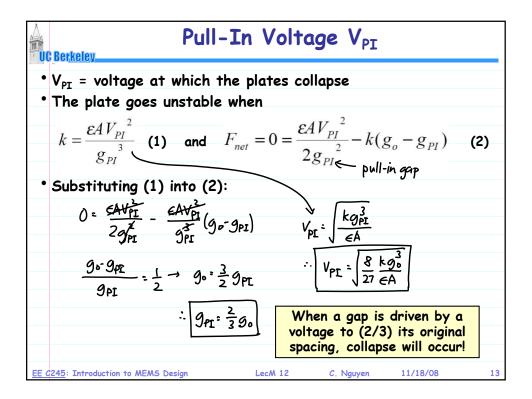
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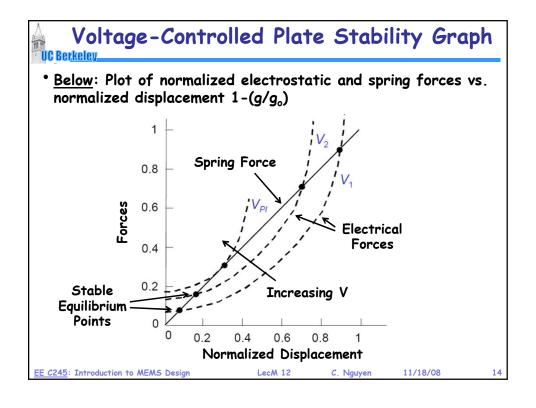












# Advantages of Electrostatic Actuators

- Easy to manufacture in micromachining processes, since conductors and air gaps are all that's needed → low cost!
- Energy conserving  $\rightarrow$  only parasitic energy loss through I<sup>2</sup>R losses in conductors and interconnects
- Variety of geometries available that allow tailoring of the relationships between voltage, force, and displacement
- Electrostatic forces can become very large when dimensions shrink  $\rightarrow$  electrostatics scales well!
- Same capacitive structures can be used for both drive and sense of velocity or displacement
- Simplicity of transducer greatly reduces mechanical energy losses, allowing the highest Q's for resonant structures

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# Problems With Electrostatic Actuators

- Nonlinear voltage-to-force transfer function
- Relatively weak compared with other transducers (e.g., piezoelectric), but things get better as dimensions scale

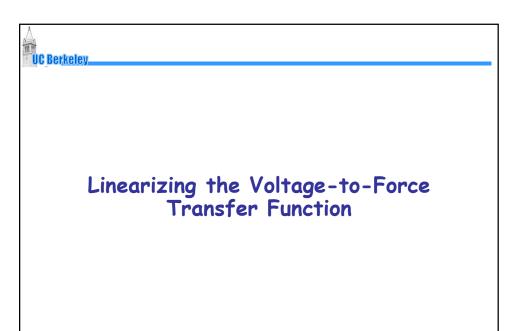
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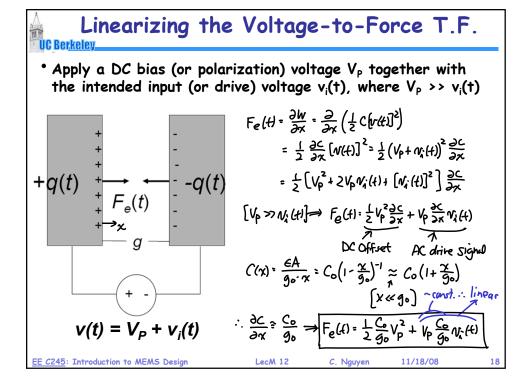
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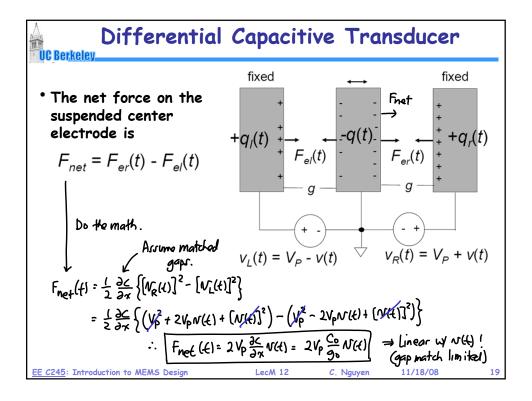
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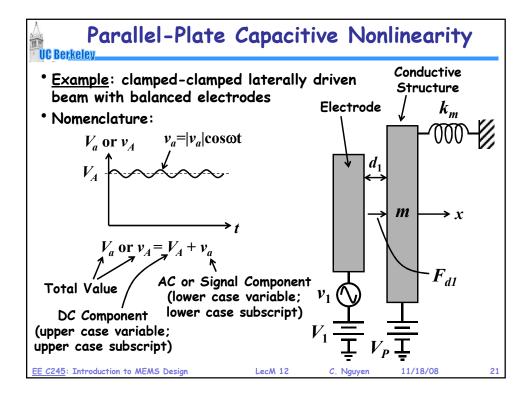
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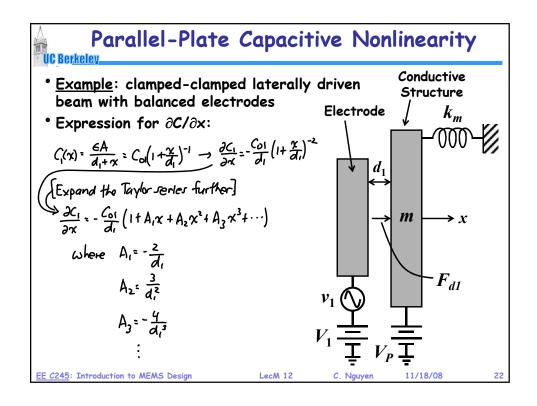
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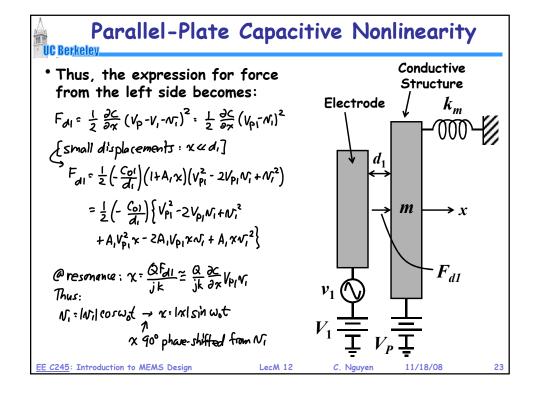




Remaining Nonlinearity (Electrical Stiffness)









• Retaining only terms at the drive frequency:

$$F_{d1}|_{\omega_o} = V_{P1} \frac{C_{o1}}{d_1} |v_1| \cos \omega_o t + V_{P1}^2 \frac{C_{o1}}{d_1^2} |x| \sin \omega_o t$$

Drive force arising from the input excitation voltage at the frequency of this voltage

Proportional to displacement

90° phase-shifted from drive, so in phase with displacement

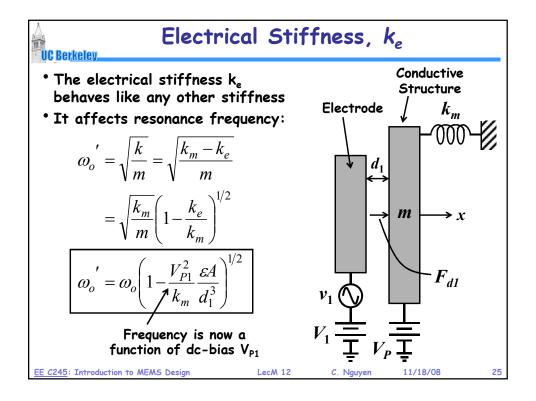
- These two together mean that this force acts against the spring restoring force!
  - ♦ A negative spring constant
  - Since it derives from  $V_P$ , we call it the electrical stiffness, given by:

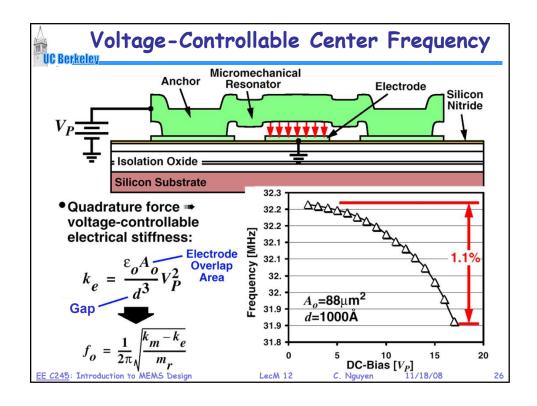
$$k_e = V_{P1}^2 \frac{C_{o1}}{d_1^2} = V_{P1}^2 \frac{\varepsilon A}{d_1^3}$$

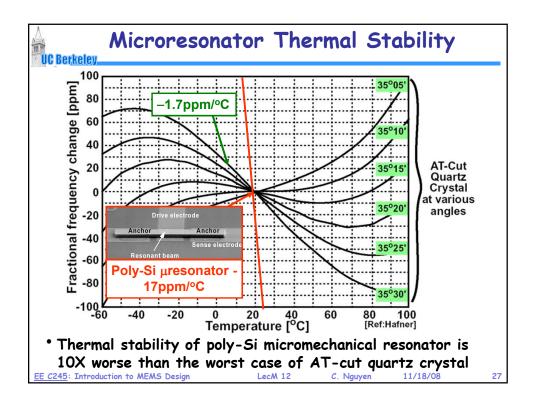
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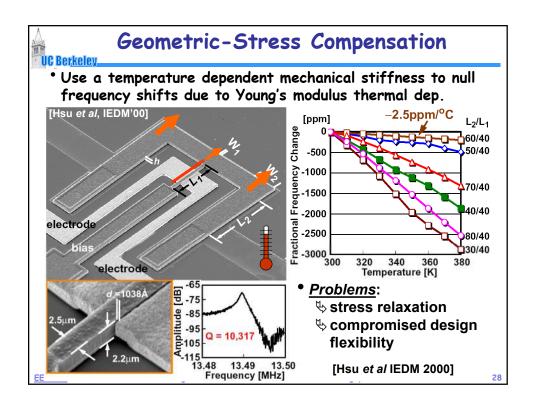
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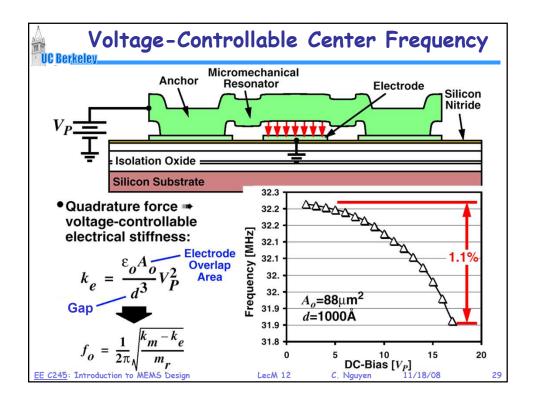
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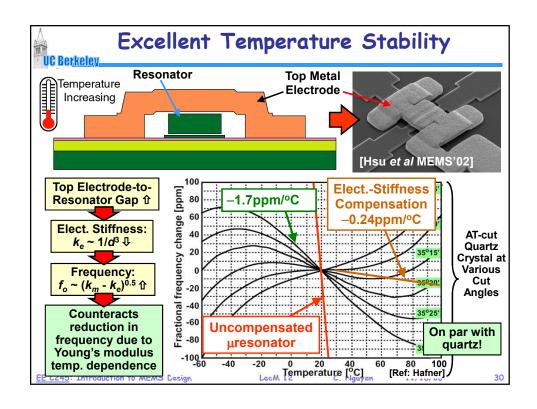


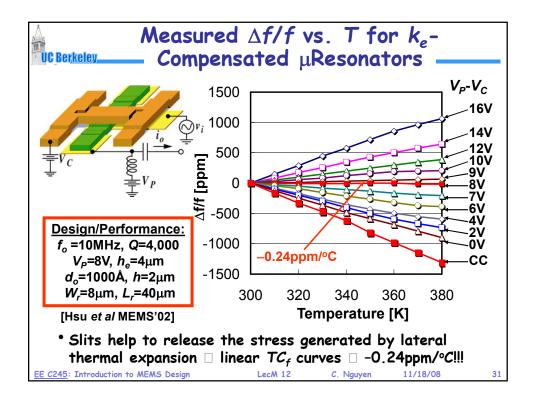


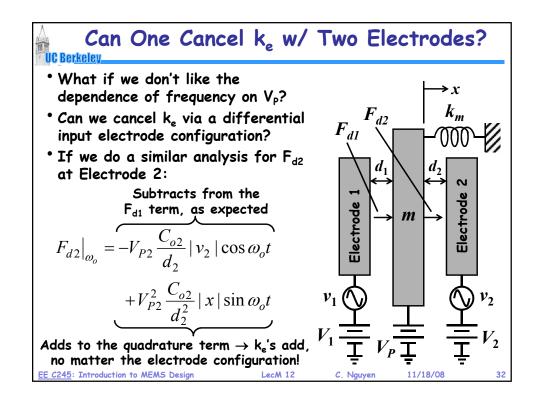


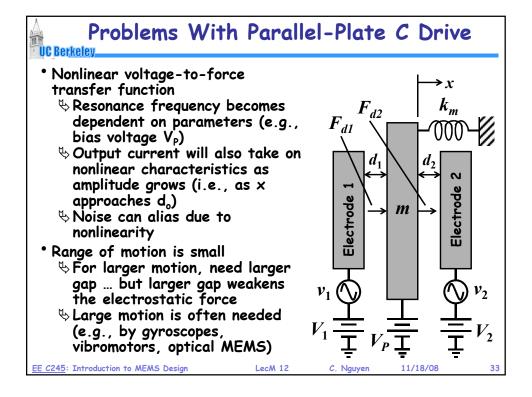












Electrostatic Comb Drive

Electrostatic Comb Drive

