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MEMS Material Properties

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Material Properties for MEMS

Material	Density, ρ , Kg/m ³	Modulus, E, GPa	E/ρ GN/kg-m
Silicon	2330	165	72
Silicon Oxide	2200	73	36
Silicon Nitride	3300	304	92
Nickel	8900	207	23
Aluminum	2710	69	25
Aluminum Oxide	3970	393	99
Silicon Carbide	3300	430	130
Diamond	3510	1035	295

Units: (m/s)²
↓
 $\sqrt{E/\rho}$ is acoustic velocity

[Mark Spearing, MIT]

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Young's Modulus Versus Density

Lines of constant acoustic velocity

[Ashby, Mechanics of Materials, Pergamon, 1992]

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Yield Strength

- Definition:** the stress at which a material experiences significant plastic deformation (defined at 0.2% offset pt.)
- Below the yield point:** material deforms elastically → returns to its original shape when the applied stress is removed
- Beyond the yield point:** some fraction of the deformation is permanent and non-reversible

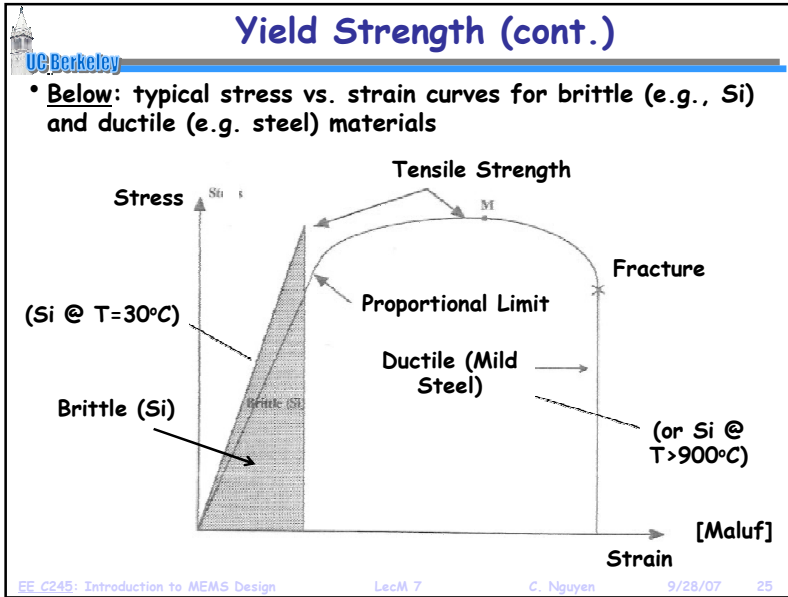
Yield Strength: defined at 0.2% offset pt.

Elastic Limit: stress at which permanent deformation begins

Proportionality Limit: point at which curve goes nonlinear

True Elastic Limit: lowest stress at which dislocations move

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Young's Modulus and Useful Strength

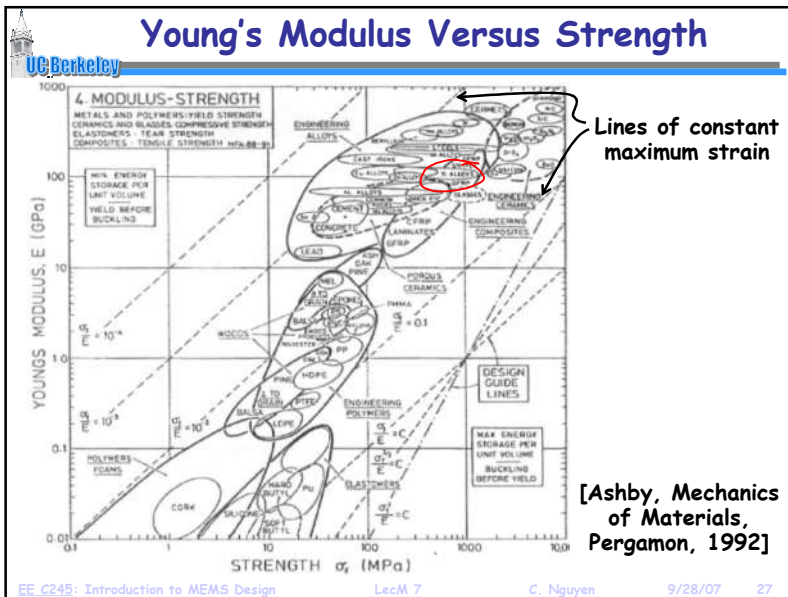
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Stored mechanical energy → $\frac{\sigma_f^2}{E}$

Material	Modulus, E, GPa	Useful Strength*, σ _f , MPa	$\frac{\sigma_f}{E}$ (-) x 10 ⁻³	$\frac{\sigma_f^2}{E}$ MJ/m ³
Silicon	165	4000	24	97
Silicon Oxide	73	1000	13	14
Silicon Nitride	304	1000	3	4
Nickel	207	500	2	1.2
Aluminum	69	300	4	1.3
Aluminum Oxide	393	2000	5	10
Silicon Carbide	430	2000	4	9.3
Diamond	1035	1000	1	0.9

From Mark Spearing, MIT, *Future of MEMS Workshop*, Cambridge, England, May 2003

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Quality Factor (or Q)

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Clamped-Clamped Beam μ Resonator

Frequency:
Stiffness k_r Young's Modulus E
 $f_o = \frac{1}{2\pi} \sqrt{\frac{k_r}{m_r}} = 1.03 \sqrt{\frac{E h}{\rho L_r^2}}$
Density ρ
Mass (e.g., $m_r = 10^{-13}$ kg) \Rightarrow Smaller mass \Rightarrow higher freq. range and lower series R_x

Note: If $V_p = 0V \Rightarrow$ device off

$i_o = V_p \frac{dC}{dt}$

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Quality Factor (or Q)

- Measure of the frequency selectivity of a tuned circuit
- Definition: $Q = \frac{\text{Total Energy Per Cycle}}{\text{Energy Lost Per Cycle}} = \frac{f_o}{BW_{3dB}}$
- Example: series LCR circuit $\Rightarrow Q = \frac{\text{Im}(Z)}{\text{Re}(Z)} = \frac{\omega_o L}{R} = \frac{1}{\omega_o CR}$
- Example: parallel LCR circuit $\Rightarrow Q = \frac{\text{Im}(Y)}{\text{Re}(Y)} = \frac{\omega_o C}{G} = \frac{1}{\omega_o LG}$

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Selective Low-Loss Filters: Need Q

General BPF Implementation: Resonator Tank - Coupler - Resonator Tank - Coupler - Resonator Tank

Typical LC implementation: $R_{s1}, C_{21}, L_{s1}, R_{s2}, C_{12}, L_{s2}, R_{s3}, C_{13}, L_{s3}$

- In resonator-based filters: high tank Q \Leftrightarrow low insertion loss
- At right: a 0.1% bandwidth, 3-res filter @ 1 GHz (simulated) \Rightarrow heavy insertion loss for resonator Q < 10,000

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Oscillator: Need for High Q

- Main Function: provide a stable output frequency
- Difficulty: superposed noise degrades frequency stability

Ideal Sinusoid: $v_o(t) = V_o \sin(2\pi f_o t)$

Real Sinusoid: $v_o(t) = (V_o + \epsilon(t)) \sin(2\pi f_o t + \theta(t))$

Higher Q \Rightarrow Tighter Spectrum

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Attaining High Q

Problem: IC's cannot achieve Q's in the thousands
 ↳ transistors ⇒ consume too much power to get Q
 ↳ on-chip spiral inductors ⇒ Q's no higher than ~10
 ↳ off-chip inductors ⇒ Q's in the range of 100's

Observation: vibrating mechanical resonances ⇒ Q > 1,000

Example: quartz crystal resonators (e.g., in wristwatches)
 ↳ extremely high Q's ~ 10,000 or higher (Q ~ 10⁶ possible)
 ↳ mechanically vibrates at a distinct frequency in a thickness-shear mode

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Energy Dissipation and Resonator Q

$$\frac{1}{Q} = \frac{1}{Q_{\text{defects}}} + \frac{1}{Q_{\text{TED}}} + \frac{1}{Q_{\text{viscous}}} + \frac{1}{Q_{\text{support}}}$$

Material Defect Losses **Gas Damping**

Thermoelastic Damping (TED) **Anchor Losses**

At high frequency, this is our big problem!

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Thermoelastic Damping (TED)

• Occurs when heat moves from compressed parts to tensioned parts → heat flux = energy loss

$$\zeta = \Gamma(T)\Omega(f) = \frac{1}{2Q}$$

$$\Gamma(T) = \frac{\alpha^2 T E}{4\rho C_p}$$

$$\Omega(f_o) = 2 \left[\frac{f_{\text{TED}} f}{f_{\text{TED}}^2 + f^2} \right]$$

$$f_{\text{TED}} = \frac{\pi K}{2\rho C_p h^2}$$

ζ = thermoelastic damping factor
 α = thermal expansion coefficient
 T = beam temperature
 E = elastic modulus
 ρ = material density
 C_p = heat capacity at const. pressure
 K = thermal conductivity
 f = beam frequency
 h = beam thickness
 f_{TED} = characteristic TED frequency

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TED Characteristic Frequency

$$f_{\text{TED}} = \frac{\pi K}{2\rho C_p h^2}$$

ρ = material density
 C_p = heat capacity at const. pressure
 K = thermal conductivity
 h = beam thickness
 f_{TED} = characteristic TED frequency

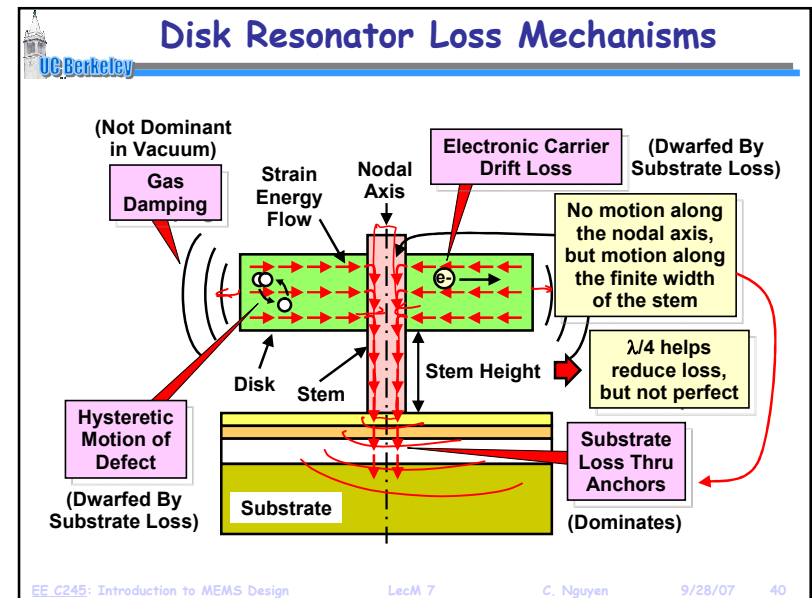
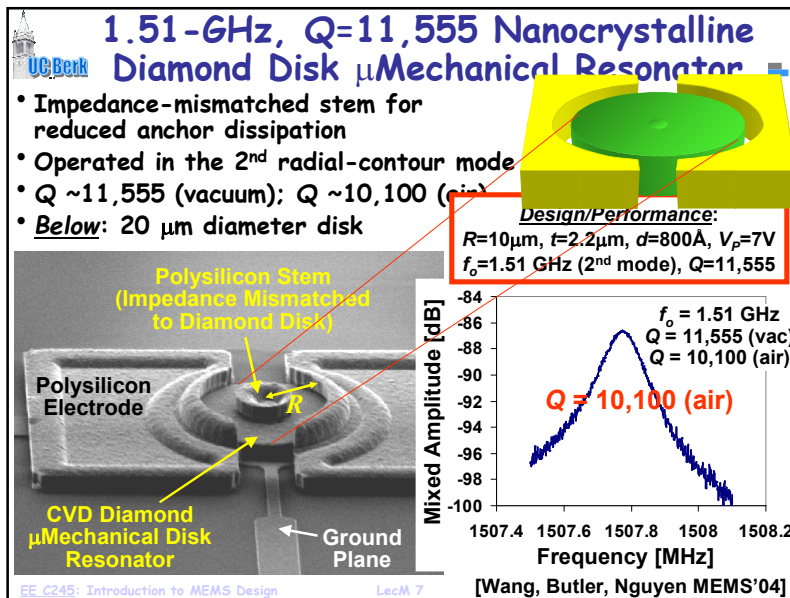
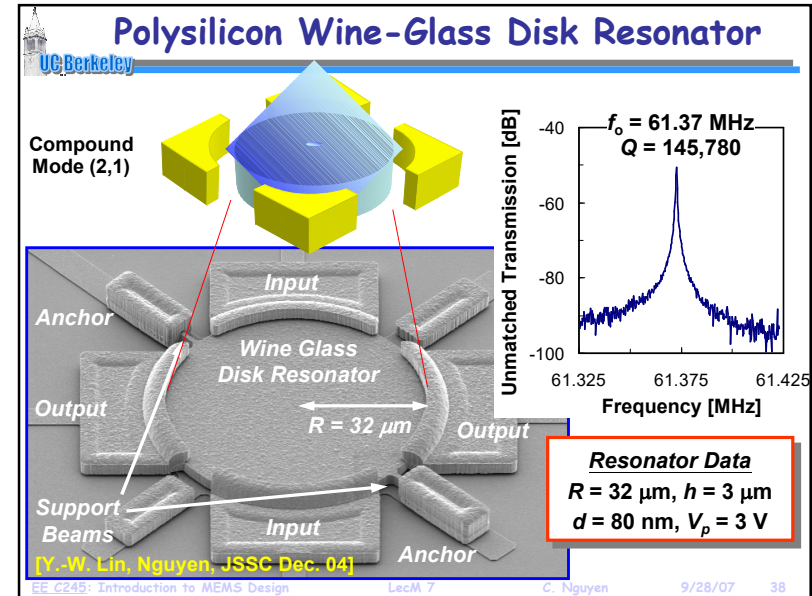
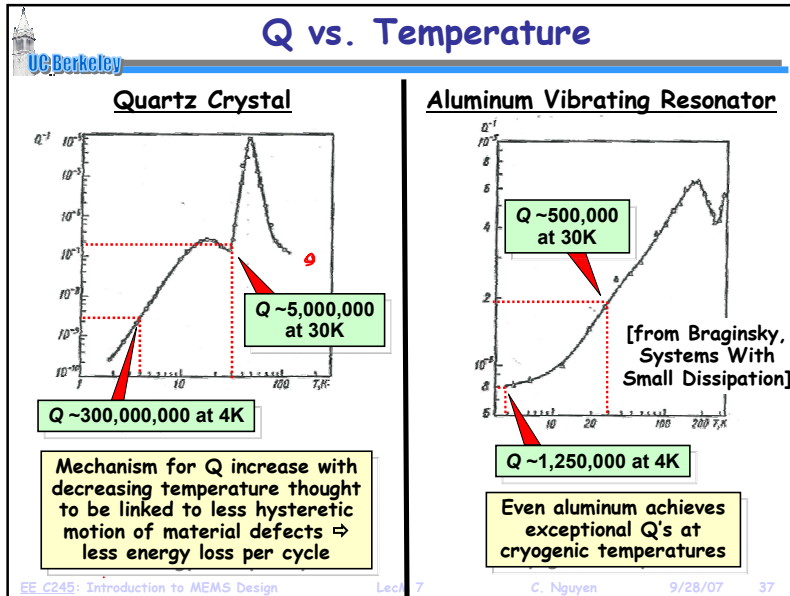
• Governed by
 ↳ Resonator dimensions
 ↳ Material properties

Peak where Q is minimized

Property	Silicon	Quartz	Units
Thermal expansion	2.60	13.70	ppm/°K
Elastic modulus	1.70	0.78	10 ¹² dyne/cm ²
Material density	2.33	2.60	g/cm ³
Heat capacity	0.70	0.75	J/g/°K
Thermal conductivity	1.50	0.10	10 ⁷ dyne/°K/s
Peak damping @ 300°K	1.06	11.34	10 ⁻⁴

[from Roszhart, Hilton Head 1990]

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MEMS Material Property Test Structures

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Stress Measurement Via Wafer Curvature

- Compressively stressed film → bends a wafer into a convex shape
- Tensile stressed film → bends a wafer into a concave shape
- Can optically measure the deflection of the wafer before and after the film is deposited
- Determine the radius of curvature R, then apply:

$$\sigma = \frac{E'h^2}{6Rt}$$

σ = film stress [Pa]
 $E' = E/(1-\nu)$ = biaxial elastic modulus [Pa]
 h = substrate thickness [m]
 t = film thickness
 R = substrate radius of curvature [m]

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MEMS Stress Test Structure

- Simple Approach:** use a clamped-clamped beam
- Compressive stress causes buckling
- Arrays with increasing length are used to determine the critical buckling load, where

$$\sigma_{critical} = -\frac{\pi^2 E h^2}{3 L^2}$$

E = Young's modulus [Pa]
 $I = (1/12)Wh^3$ = moment of inertia
 L, W, h indicated in the figure

- Limitation:** Only compressive stress is measurable

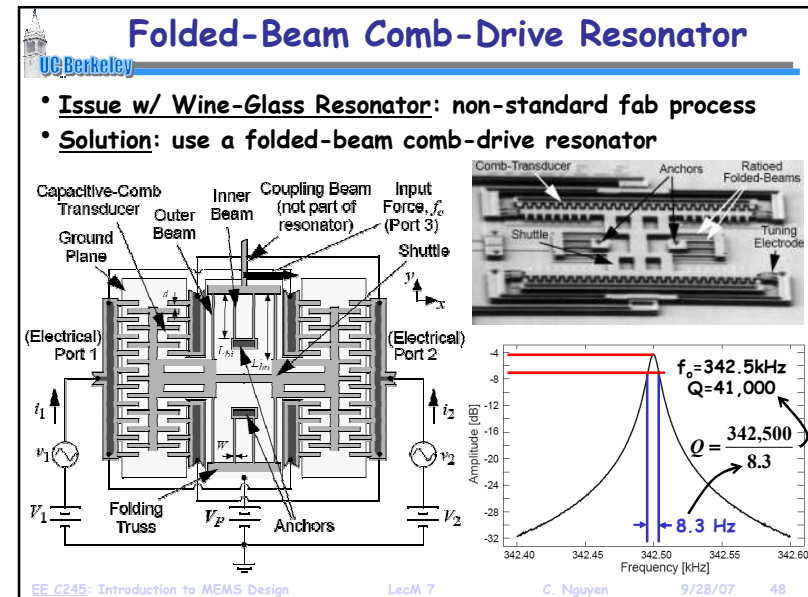
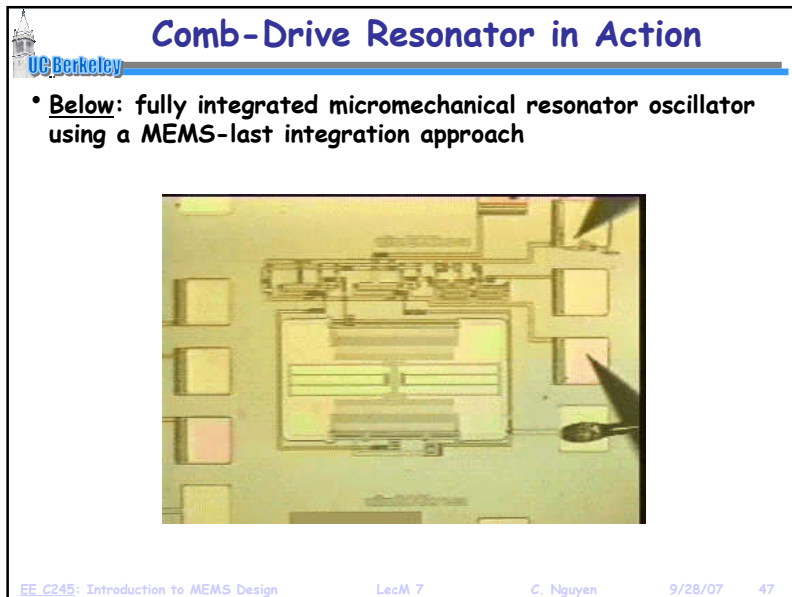
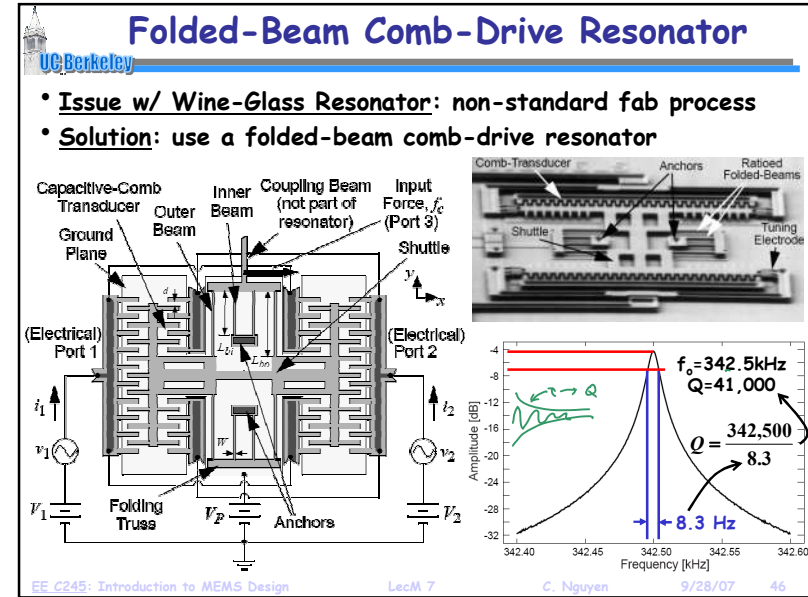
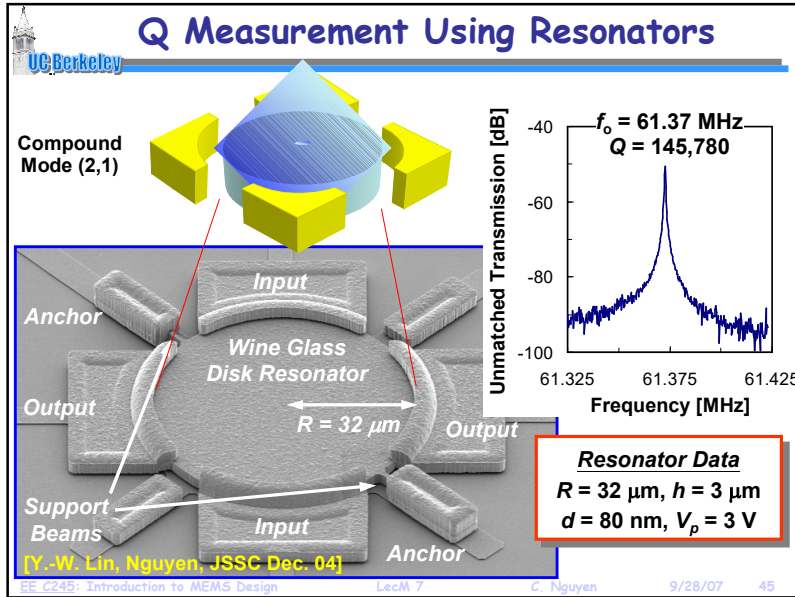
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More Effective Stress Diagnostic

- Single structure measures both compressive and tensile stress
- Expansion or contraction of test beam → deflection of pointer
- Vernier movement indicates type and magnitude of stress

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Measurement of Young's Modulus

- Use micromechanical resonators
 - Resonance frequency depends on E
 - For a folded-beam resonator:

$$\text{Resonance Frequency} = f_o = \left[\frac{4Eh(W/L)^3}{M_{eq}} \right]^{1/2}$$

h = thickness
 W = width
 L = length

Young's modulus
 M_{eq}
 Equivalent mass

- Extract E from measured frequency f_o
- Measure f_o for several resonators with varying dimensions
- Use multiple data points to remove uncertainty in some parameters

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Anisotropic Materials

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Elastic Constants in Crystalline Materials

- Get different elastic constants in different crystallographic directions → 81 of them in all
 - Cubic symmetries make 60 of these terms zero, leaving 21 of them remaining that need be accounted for
- Thus, describe stress-strain relations using a 6x6 matrix

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \sigma_z \\ \tau_{yz} \\ \tau_{zx} \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} & C_{14} & C_{15} & C_{16} \\ C_{12} & C_{22} & C_{23} & C_{24} & C_{25} & C_{26} \\ C_{13} & C_{23} & C_{33} & C_{34} & C_{35} & C_{36} \\ C_{14} & C_{24} & C_{34} & C_{44} & C_{45} & C_{46} \\ C_{15} & C_{25} & C_{35} & C_{45} & C_{55} & C_{56} \\ C_{16} & C_{26} & C_{36} & C_{46} & C_{56} & C_{66} \end{bmatrix} \begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \\ \gamma_{yz} \\ \gamma_{zx} \\ \gamma_{xy} \end{bmatrix}$$

Stresses Stiffness Coefficients Strains

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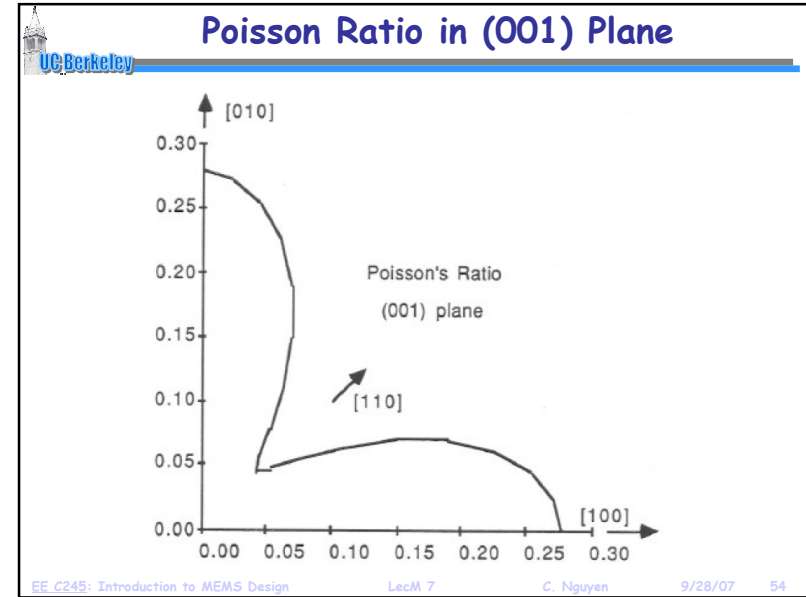
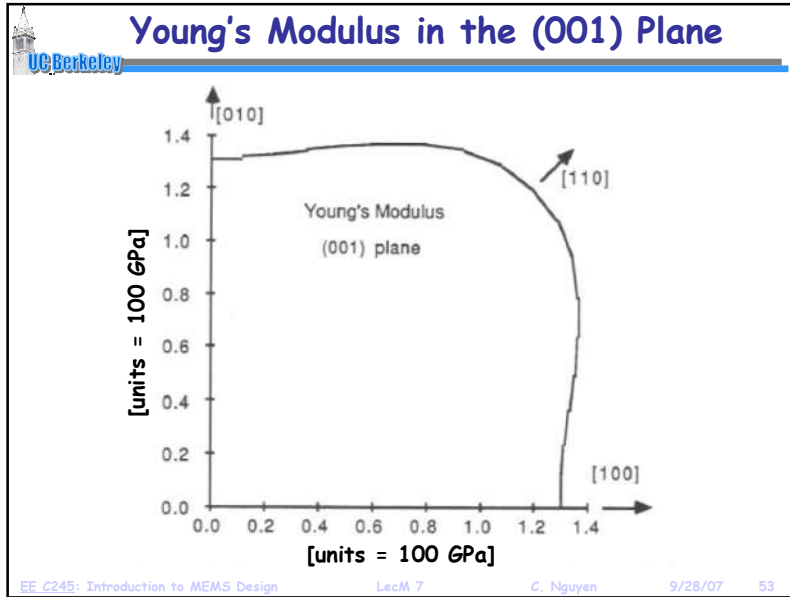
Stiffness Coefficients of Silicon

- Due to symmetry, only a few of the 21 coefficients are non-zero
- With cubic symmetry, silicon has only 3 independent components, and its stiffness matrix can be written as:

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \sigma_z \\ \tau_{yz} \\ \tau_{zx} \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} & 0 & 0 & 0 \\ C_{12} & C_{22} & C_{23} & 0 & 0 & 0 \\ C_{13} & C_{23} & C_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & C_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & C_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & C_{66} \end{bmatrix} \begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \\ \gamma_{yz} \\ \gamma_{zx} \\ \gamma_{xy} \end{bmatrix}$$

where $\begin{cases} C_{11} = 165.7 \text{ GPa} \\ C_{12} = 63.9 \text{ GPa} \\ C_{44} = 79.6 \text{ GPa} \end{cases}$

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Anisotropic Design Implications

- Young's modulus and Poisson ratio variations in anisotropic materials can pose problems in the design of certain structures
- E.g., disk or ring resonators, which rely on isotropic properties in the radial directions
 - ↳ Okay to ignore variation in RF resonators, although some Q hit is probably being taken
- E.g., ring vibratory rate gyroscopes
 - ↳ Mode matching is required, where frequencies along different axes of a ring must be the same
 - ↳ Not okay to ignore anisotropic variations, here

Wine-Glass Mode Disk

```

UNIT: 5.0,2
TOL: 0.2004
$REPLACEDEF
STEP=1
JOB = 1
PRGR: 0028000
PARAM:00000
AUX1=15
AUX2=500
SOL: 000007
*ELEM, 1100-00
DF = 1
*ELEM,0,02
*IP =1,2
$=000000
                
```

Ring Gyroscope

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