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EE C247B - ME C218 Introduction to MEMS Design Spring 2018

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Lecture Module 10: Resonance Frequency

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Lecture Outline

- Reading: Senturia, Chpt. 10: §10.5, Chpt. 19
- Lecture Topics:
 - ↪ Estimating Resonance Frequency
 - ↪ Lumped Mass-Spring Approximation
 - ↪ ADXL-50 Resonance Frequency
 - ↪ Distributed Mass & Stiffness
 - ↪ Folded-Beam Resonator

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Estimating Resonance Frequency

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Clamped-Clamped Beam μ Resonator

Resonator Beam
 W_r , L_r , h

Electrode
 v_i

Voltage-to-Force Capacitive Transducer
 V_P

Sinusoidal Excitation
 $v_i = V_i \cos[\omega_o t] \rightarrow f_i = F_i \cos[\omega_o t]$

Sinusoidal Forcing Function

i_o

$Q \sim 10,000$

$\frac{i_o}{v_i}$

ω_0 , ω

- $\omega \neq \omega_o$: small amplitude
- $\omega = \omega_o$: maximum amplitude \rightarrow beam reaches its maximum potential and kinetic energies

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Folded-Beam Suspension

Comb-Driven Folded Beam Actuator

$$\delta(x, y) = \frac{F_x}{48EI_z} (3Ly^2 - 2y^3) \quad 0 \leq y \leq L$$

Case: $y=0 \quad \delta(y=0) = 0 \quad \checkmark$

Case: $y=L \quad \delta(y=L) = \frac{F_x}{48EI_z} L^3 \rightarrow k = \frac{(F_x/4)}{x} = \frac{12EI_z}{L^3} = \frac{k_c}{2} \quad \checkmark$

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