

### Example: TransR Amplifier Noise (cont)

• To summarize, for a transresistance amplifier, the equivalent input-referred current and voltage noise generators are given by:

$$\overline{i_{eq}^2} = \overline{i_{ia}^2} + \overline{i_f^2} + \frac{\overline{v_{ia}^2}}{R_f^2}$$

$$\overline{v_{eq}^2} = \overline{v_{ia}^2}$$

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### LF356 Op Amp Data Sheet

LF155/LF156/LF256/LF257/LF355/LF356/LF357  
JFET Input Operational Amplifiers

**General Description**  
These are the first monolithic JFET input operational amplifiers to incorporate well matched, high voltage JFETs on the same chip with standard bipolar transistors (BI-FET™ Technology). These amplifiers feature low input bias and offset currents/low offset voltage and offset voltage drift, coupled with offset adjust which does not degrade drift or common-mode rejection. The devices are also designed for high slew rate, wide bandwidth, extremely fast settling time, low voltage and current noise and a low 1/f noise corner.

**Common Features**

- Logarithmic amplifiers
- Photocell amplifiers
- Sample and Hold circuits
- Low input bias current: 30pA
- Low input Offset Current: 3pA
- High input impedance: 10<sup>12</sup>Ω
- Low input noise current: 0.01 pA/√Hz
- High common-mode rejection ratio: 100 dB
- Large dc voltage gain: 106 dB

**Features**

**Advantages**

- Replace expensive hybrid and module FET op amps
- Rugged JFETs allow blow-out free handling compared with MOSFET input devices
- Excellent for low noise applications using either high or low source impedance—very low 1/f corner
- Offset adjust does not degrade drift or common-mode rejection as in most monolithic amplifiers
- New output stage allows use of large capacitive loads (5,000 pF) without stability problems
- Internal compensation and large differential input voltage capability

**Uncommon Features**

	LF155/ LF355	LF156/ LF256/ LF356 (A <sub>v</sub> =5)	LF257/ LF357	Units
Extremely fast settling time to 0.01%	4	1.5	1.5	μs
Fast slew rate	5	12	50	V/μs
Wide gain bandwidth	2.5	5	20	MHz
Low input noise voltage	20	12	12	nV/√Hz

**Applications**

- Precision high speed integrators
- Fast D/A and A/D converters
- High impedance buffers
- Wideband, low noise, low drift amplifiers

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### Example ARW Calculation

• **Example Design:**

↳ **Sensor Element:**

- $m = (100\mu\text{m})(100\mu\text{m})(20\mu\text{m})(2300\text{kg/m}^3) = 4.6 \times 10^{-10}\text{kg}$
- $\omega_s = 2\pi(15\text{kHz})$
- $\omega_d = 2\pi(10\text{kHz})$
- $k_s = \omega_s^2 m = 4.09\text{ N/m}$
- $x_d = 20\mu\text{m}$
- $Q_s = 50,000$
- $V_p = 5\text{V}$
- $h = 20\mu\text{m}$
- $d = 1\mu\text{m}$

↳ **Sensing Circuitry:**

- $R_f = 100\text{k}\Omega$
- $i_{ia} = 0.01\text{ pA}/\sqrt{\text{Hz}}$
- $v_{ia} = 12\text{ nV}/\sqrt{\text{Hz}}$

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### Example ARW Calculation (cont)

Get rotation rate to output current scale factor:

$$A = 2 \frac{\omega_d Q_s x_d \eta_e}{\omega_s} |\Theta(j\omega_d)| = 2 \left( \frac{10\text{k}}{15\text{k}} \right) (50\text{k}) (20\mu) (5) (2000\epsilon_0) (0.000024) = 2.83 \times 10^{-12}\text{C}$$

$$\Theta(j\omega_d) = \frac{(j\omega_d)(\omega_s/Q_s)}{-\omega_d^2 + j\omega_d\omega_s/Q_s + \omega_s^2} = \frac{j(10\text{k})(15\text{k})/(50\text{k})}{(15\text{k})^2 - (10\text{k})^2 + j(10\text{k})(15\text{k})/50\text{k}} = \frac{j(3\text{k})}{1.25 \times 10^8 + j(3\text{k})}$$

$$\rightarrow |\Theta(j\omega_d)| = \frac{3\text{k}}{\sqrt{(1.25 \times 10^8)^2 + (3\text{k})^2}} = 0.000024$$

$$\frac{\partial C}{\partial x} = \frac{C_0}{d} = \frac{\epsilon_0 h \eta_p}{d} = \frac{\epsilon_0 (20\mu)(100\mu)}{(1\mu)^2} = 2000\epsilon_0 \rightarrow \eta_e = V_p \frac{\partial C}{\partial x} = 5(2000\epsilon_0)$$

Assume electrode covers the whole sidewall.

Then, get noise:

$$\frac{\overline{i_{eq}^2}}{\Delta f} = \frac{4kT}{R_x} |\Theta(j\omega_d)|^2 + \frac{4kT}{R_f} + \frac{\overline{i_{ia}^2}}{\Delta f} + \frac{\overline{v_{ia}^2}}{\Delta f} \left( \frac{1}{R_f} \right)$$

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**Example ARW Calculation (cont)**

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$$R_x = \frac{\omega_s m}{Q_s \eta_e^2} = \frac{2\pi(15K)(4.6 \times 10^{-10})}{(50K)(8.85 \times 10^{-12})^2} = 110.6 k\Omega$$

$$\frac{i_{eqTOT}^2}{\Delta f} = \frac{(1.66 \times 10^{-29})}{(110.6K)} (0.000024)^2 + \frac{(1.66 \times 10^{-29})}{1M} + (0.01p)^2 + \frac{(12n)^2}{(1M)^2}$$

$8.64 \times 10^{-35} A^2/Hz$  (Sensor element noise insignificant)  
 $1.66 \times 10^{-26} A^2/Hz$  (Noise from  $R_f$  dominates!)  
 $1 \times 10^{-28} A^2/Hz$   
 $1.44 \times 10^{-28} A^2/Hz$

$$\therefore \frac{i_{eqTOT}^2}{\Delta f} = 1.68 \times 10^{-26} A^2/Hz \rightarrow i_{eqTOT} = \sqrt{\frac{i_{eqTOT}^2}{\Delta f}} = 1.30 \times 10^{-13} A/\sqrt{Hz}$$

$$\therefore \Omega_{min} = \frac{i_{eqTOT}}{A} \left( \frac{3600s}{hr} \right) \left( \frac{180^\circ}{\pi} \right) = \frac{1.30 \times 10^{-13}}{2.83 \times 10^{-12}} (3600) \left( \frac{180}{\pi} \right) = 9448 (\%/hr)/\sqrt{Hz}$$

And finally:  $ARW = \frac{1}{60} \Omega_{min} = \frac{1}{60} (9448) = 157 \%/hr = ARW \Rightarrow$  Almost turned around in 1 hour!

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**What if  $\omega_d = \omega_s$ ?**

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If  $\omega_d = \omega_s = 15KHz$ , then  $|G(j\omega_d)| = 1$  and

$$A = 2 \frac{\omega_d}{\omega_s} Q_s \chi_d \eta_e |G(j\omega_d)| = 2 Q_s \chi_d \eta_e = 2(50K)(20\mu)(5)(2000\epsilon_0) = 1.77 \times 10^{-7} C$$

$$\frac{i_{eqTOT}^2}{\Delta f} = \frac{(1.66 \times 10^{-29})}{(110.6K)} (1)^2 + \frac{(1.66 \times 10^{-29})}{1M} + (0.01p)^2 + \frac{(12n)^2}{(1M)^2}$$

$1.51 \times 10^{-25} A^2/Hz$   
 $1.66 \times 10^{-26} A^2/Hz$   
 $1 \times 10^{-28} A^2/Hz$   
 $1.44 \times 10^{-28} A^2/Hz$

Now, the sensor element dominates!

$$\therefore \frac{i_{eqTOT}^2}{\Delta f} = 1.67 \times 10^{-25} A^2/Hz \rightarrow i_{eqTOT} = \sqrt{\frac{i_{eqTOT}^2}{\Delta f}} = 4.08 \times 10^{-13} A/\sqrt{Hz}$$

$$\therefore \Omega_{min} = \frac{i_{eqTOT}}{A} \left( \frac{3600s}{hr} \right) \left( \frac{180^\circ}{\pi} \right) = \frac{4.08 \times 10^{-13}}{1.77 \times 10^{-7}} (3600) \left( \frac{180}{\pi} \right) = 0.476 (\%/hr)/\sqrt{Hz}$$

And finally:  $ARW = \frac{1}{60} \Omega_{min} = \frac{1}{60} (0.476) = 0.0079 \%/hr = ARW \Rightarrow$  Navigation grade!

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