

EE C247B - ME C218 Introduction to MEMS Design Spring 2018

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Lecture Module 15: Gyros, Noise, & MDS

E C245: Introduction to MEMS Design

LecM 1

C. Nguyen

11/18/0

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Lecture Outline

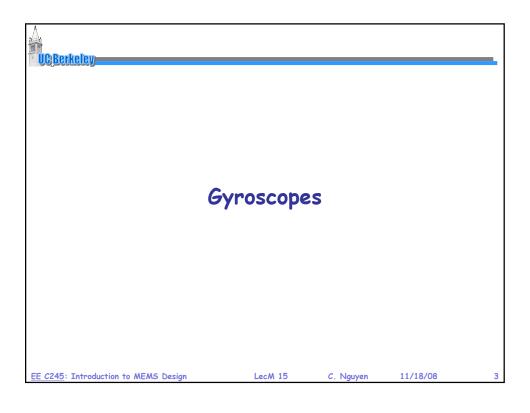
- * Reading: Senturia, Chpt. 14, Chpt. 16, Chpt. 21
- Lecture Topics:
 - **⇔** Gyroscopes
 - Syro Circuit Modeling
 - ♦ Minimum Detectable Signal (MDS)
 - ◆ Noise
 - ◆ Angle Random Walk (ARW)

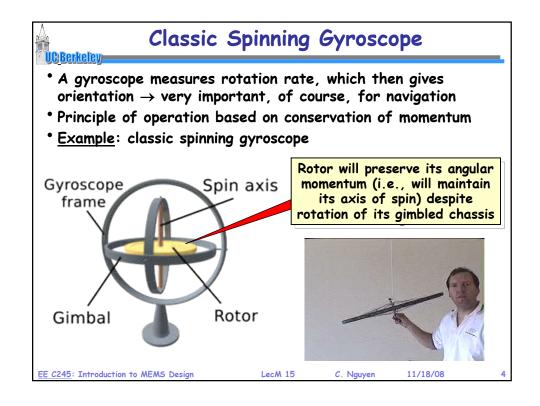
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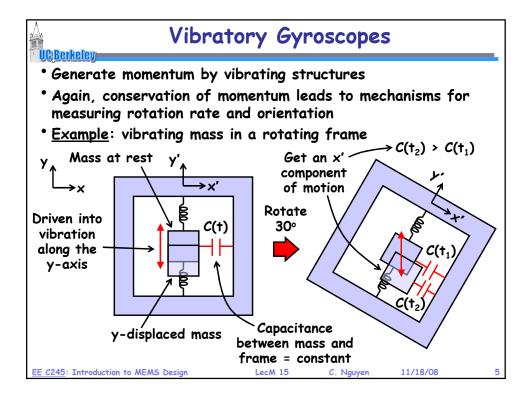
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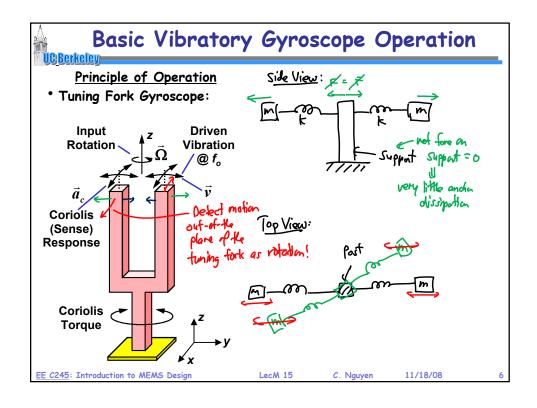
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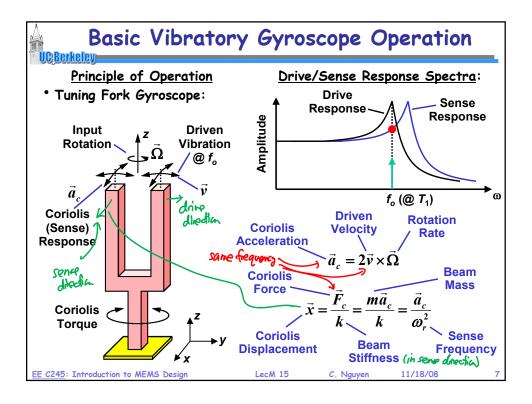
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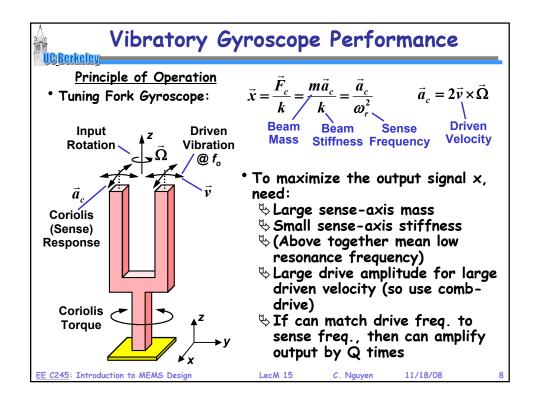


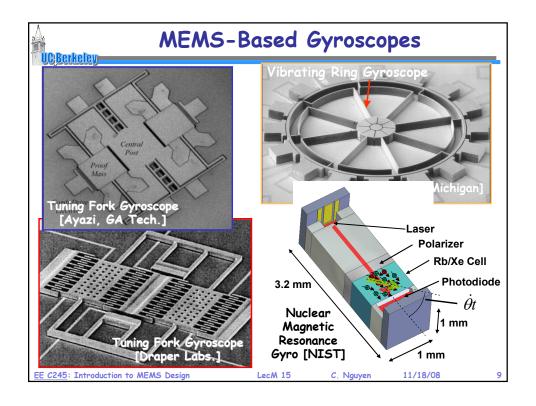


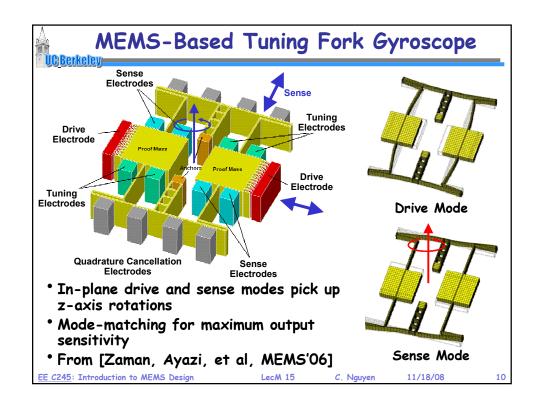


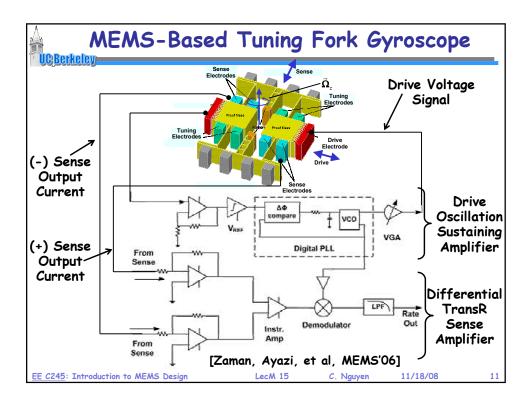


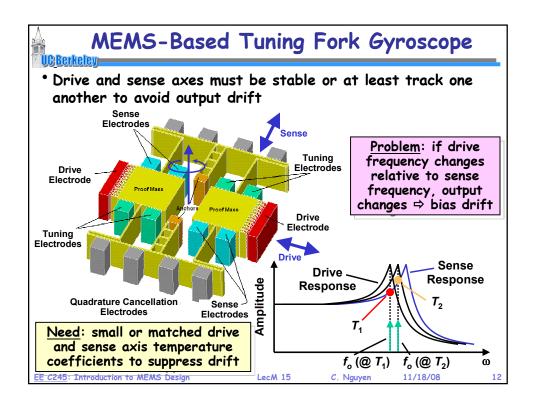


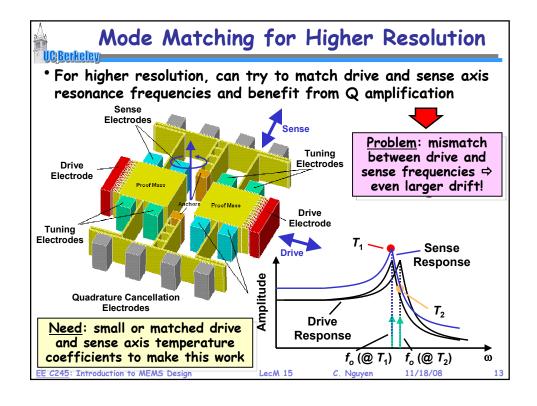


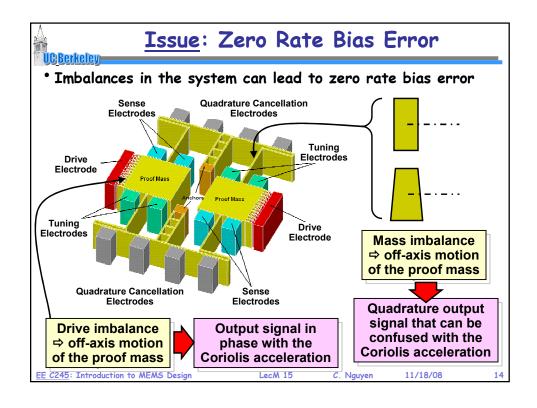


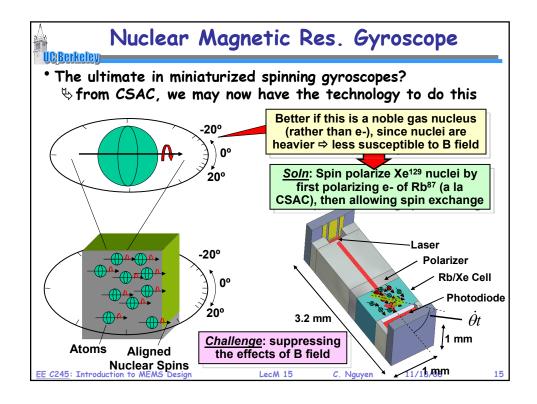


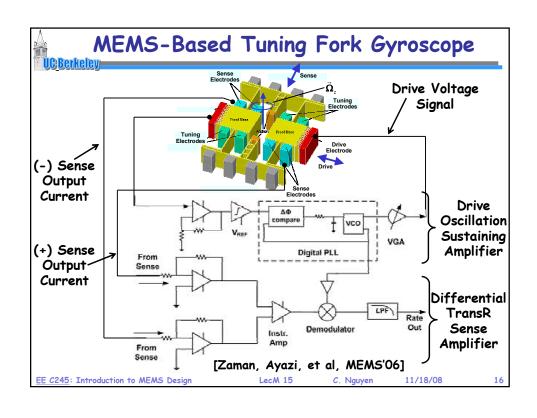


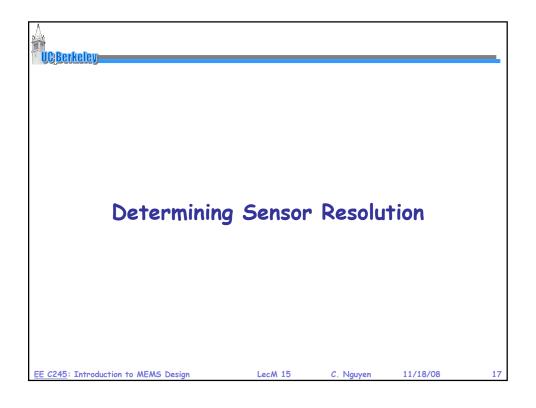


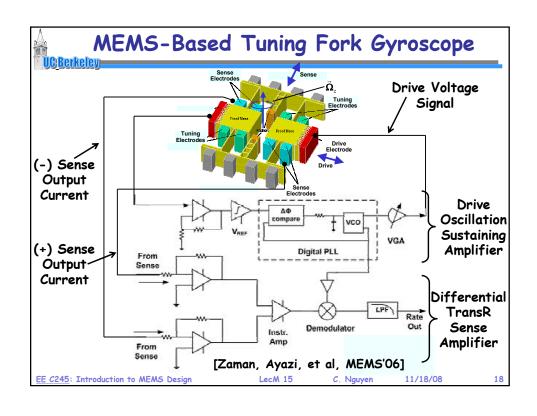


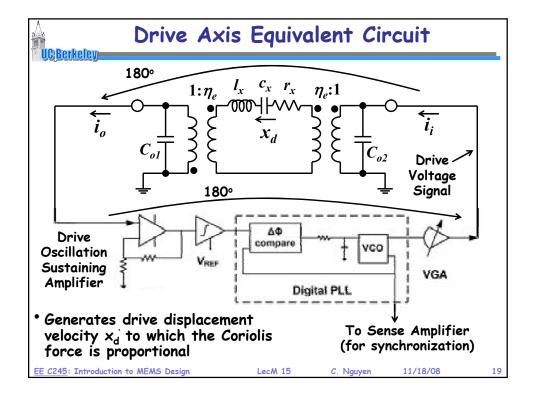


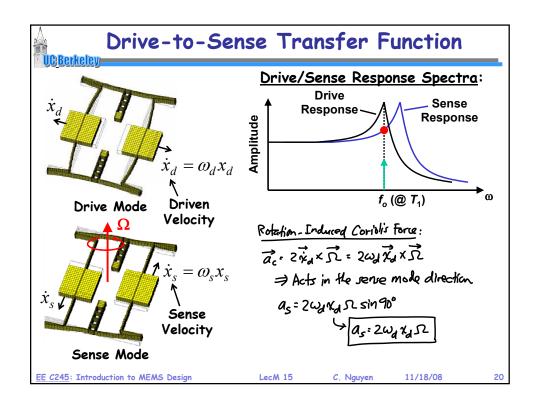


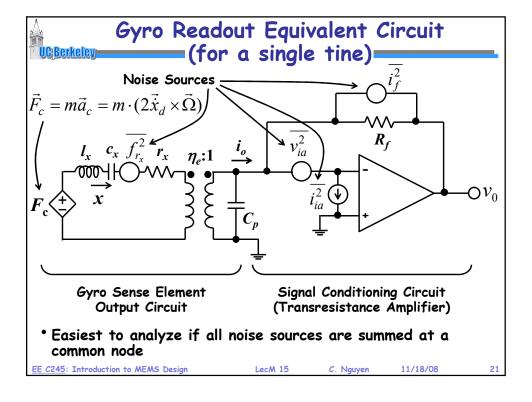


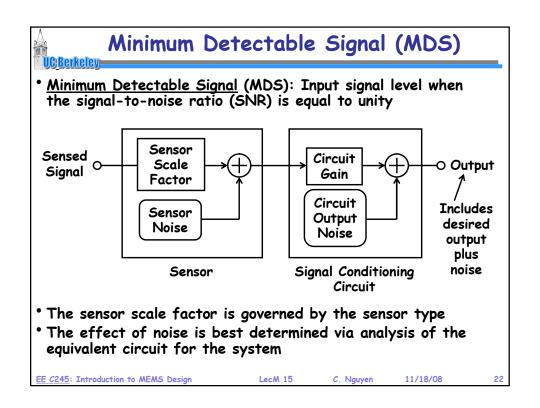


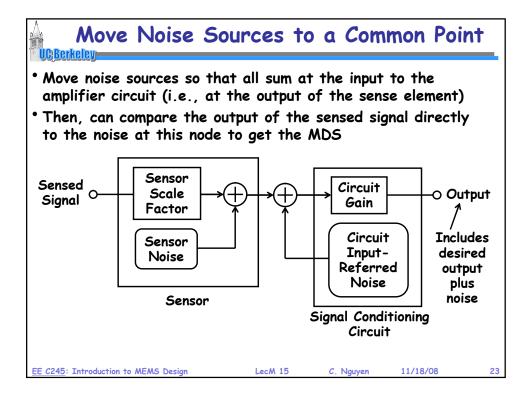


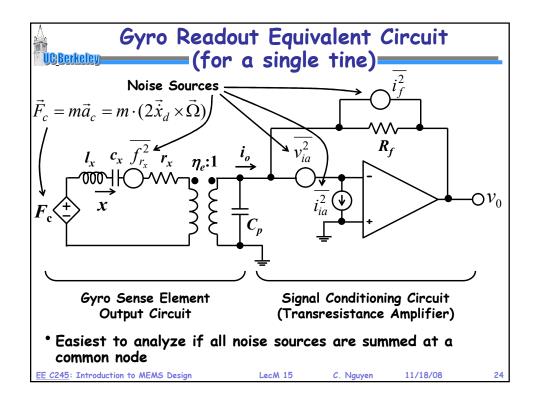


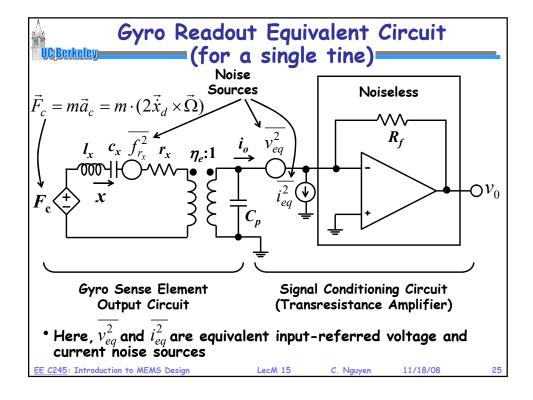


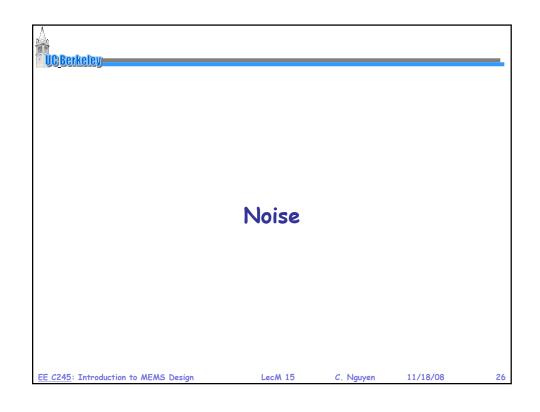




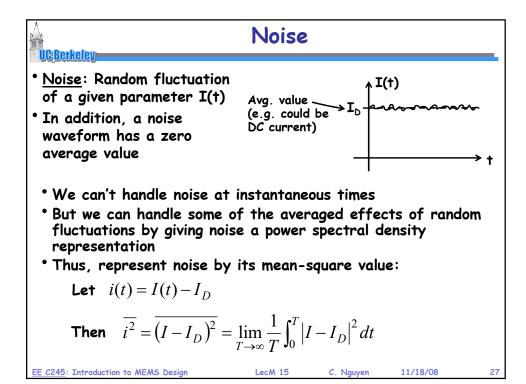


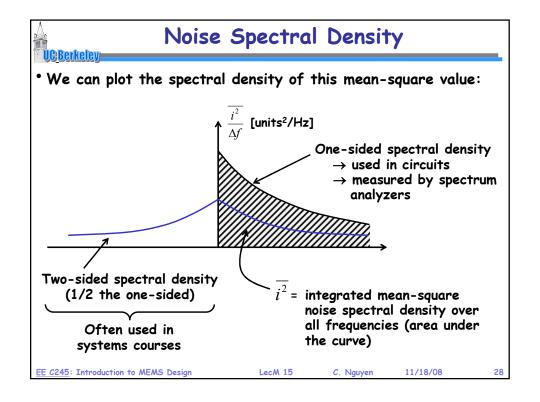


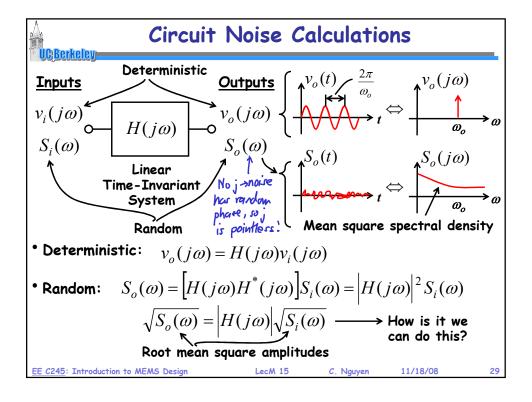


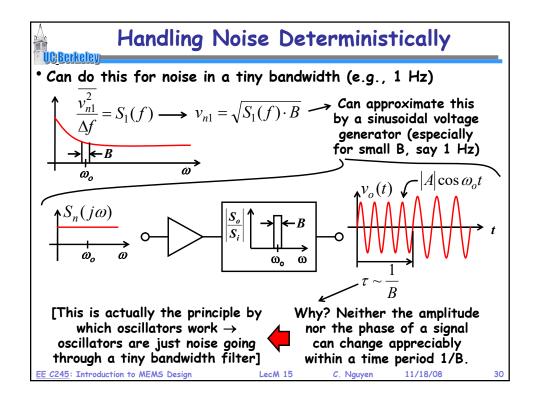


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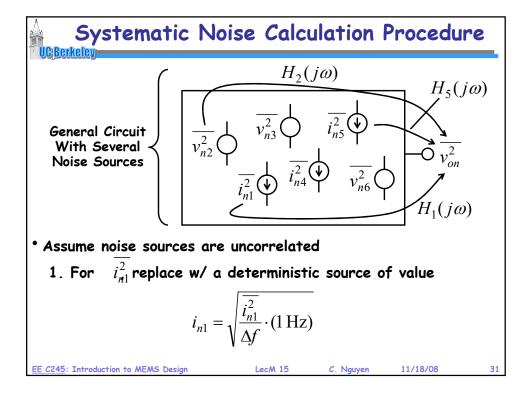






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Module 15: Gyros, Noise & MDS



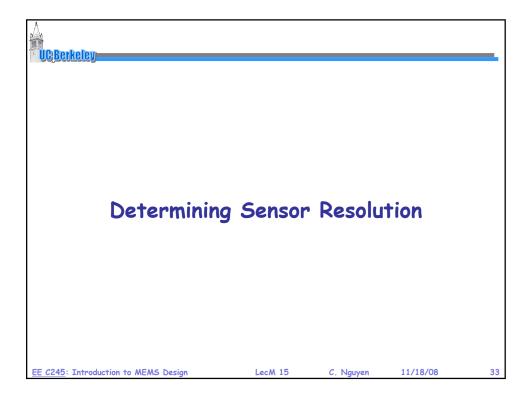
Systematic Noise Calculation Procedure

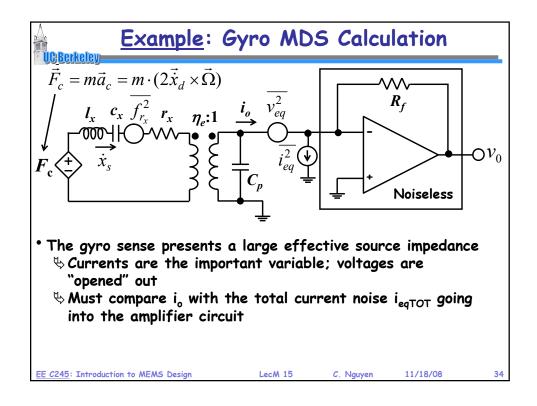
- 2. Calculate $v_{on1}(\omega)=i_{n1}(\omega)H(j\omega)$ (treating it like a deterministic signal)
- 3. Determine $v_{on1}^2 = \overline{i_{n1}^2} \cdot \left| H(j\omega) \right|^2$ 4. Repeat for each noise source: $\overline{i_{n1}^2}$, $\overline{v_{n2}^2}$, $\overline{v_{n3}^2}$
- 5. Add noise power (mean square values)

$$\overline{v_{onTOT}^2} = \overline{v_{on1}^2} + \overline{v_{on2}^2} + \overline{v_{on3}^2} + \overline{v_{on4}^2} + \cdots$$

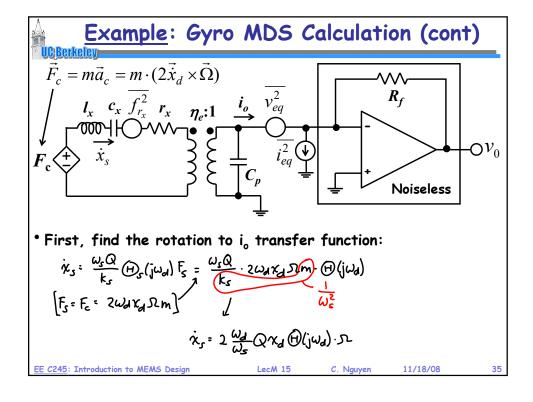
$$v_{onTOT} = \sqrt{\overline{v_{on1}^2} + \overline{v_{on2}^2} + \overline{v_{on3}^2} + \overline{v_{on4}^2} + \cdots}$$
Total rms value

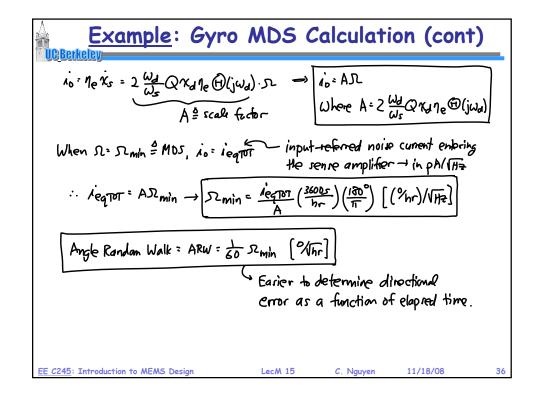
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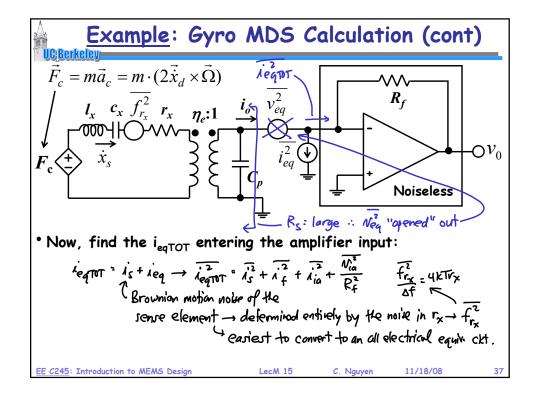


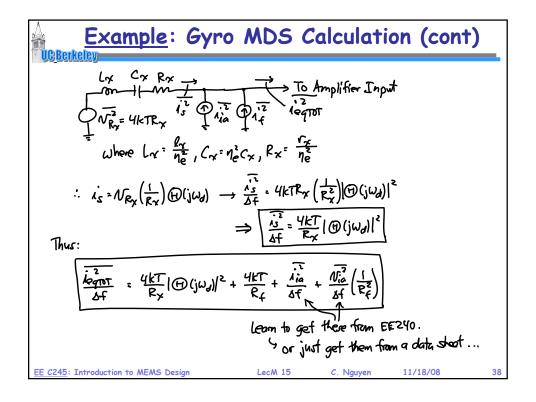


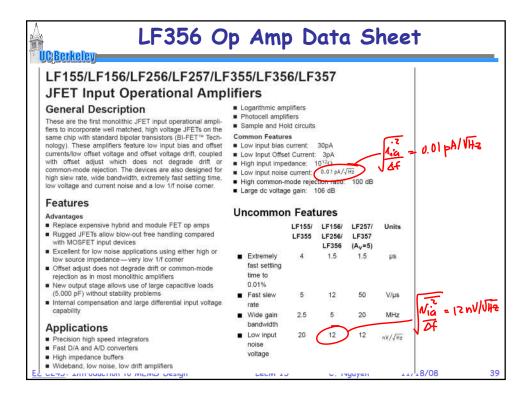
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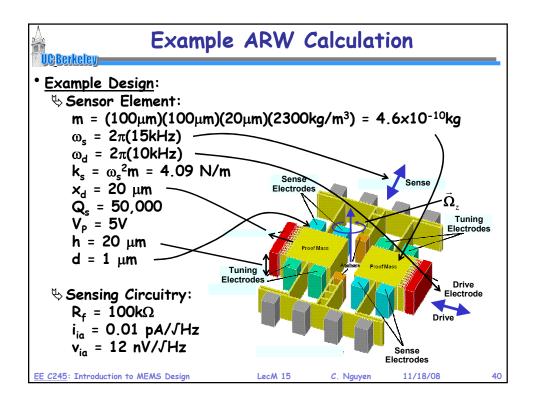












Example ARW Calculation (cont)

Get rotation rafe to output current scale factor:

$$A = 2 \frac{\omega_d}{\omega_s} Q_s \chi_d \eta_e | \Theta(j\omega_d) | = 2 \frac{\log k}{|Sk|} (sok) (20\mu) (s) (2000 \epsilon_0) (0.000024) = 2.83 \times 10^{-12} C$$

$$\Theta(j\omega_d) = \frac{(j\omega_d)(\omega_s/O_s)}{-\omega_d^2 + j\omega_d\omega_s} + \omega_s^2 = \frac{j(10k)(15k)/(50k)}{(15k)^2 - (10k)^2 + j(10k)(15k)} = \frac{j(3k)}{1.25 \times 10^8 + j(3k)}$$

$$\Rightarrow | \Theta(j\omega_d) | = \frac{3k}{\sqrt{(1.25 \times 10^8)^2 + (3k)^2}} = 0.000024$$

$$\frac{3k}{8.854 \times 10^8} = \frac{3k}{8.854 \times 10^8} = \frac{3$$

Example ARW Calculation (cont)

$$\begin{bmatrix}
R_{Y} = \frac{\omega_{SM}}{Q_{1}^{2}} = \frac{2\pi\Gamma(15K)(46X10^{-10})}{(50K)(8.85\%10^{-9})^{2}} = 110.6K5L
\end{bmatrix}$$

$$\frac{\lambda_{eqToT}}{\Delta f} = \frac{(1.66\times10^{-20})}{(110.6K)} (0.000024)^{2} + \frac{(1.66\times10^{-20})}{1M} + (0.01p)^{2} + \frac{(12n)^{2}}{(1M)^{2}}$$

$$\frac{\lambda_{eqToT}}{\lambda_{eqToT}} = \frac{(1.66\times10^{-26}A^{2}/Hz)}{(10.6K)} \frac{1.66\times10^{-26}A^{2}/Hz}{(1M)^{2}} \frac{1.410^{-28}A^{2}/Hz}{(1M)^{2}}$$

$$\frac{\lambda_{eqToT}}{\lambda_{eqToT}} = \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} = \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqToT}} = \frac{\lambda_{eqToT}}{\lambda_{eqToT}} \frac{\lambda_{eqToT}}{\lambda_{eqT$$

What if
$$\omega_{d} = \omega_{s}$$
?

If $\omega_{d} = \omega_{s} = 15KH^{2}$, then $|\mathcal{D}(j\omega_{d})| = 1$ and

$$A = 2\frac{|\omega_{d}|}{|\omega_{s}|} |\mathcal{Q}_{s} \times_{4} |\mathcal{D}(j\omega_{d})| = 2\mathcal{Q}_{s} \times_{4} |\mathcal{D}_{e}| = 2(50K)(20\mu)(5)(200066) = 1.77\times10^{-7}C$$

$$\frac{\lambda_{eqTDT}}{\Delta f} = \frac{(1.66\times10^{-20})(1)^{2} + \frac{(1.66\times10^{-20})^{2}}{|M|} + \frac{(0.01p)^{2}}{(|M|)^{2}} + \frac{(12h)^{2}}{(|M|)^{2}}$$

Now, the source elevrent dominates!

$$\frac{\lambda_{eqTDT}}{\Delta f} = 1.67\times10^{-25} |\mathcal{A}|^{2}/\mathcal{H}_{z} \longrightarrow \lambda_{eqTDT} = \frac{\lambda_{eqTDT}}{\lambda_{eqTDT}} = 4.08\times10^{-13} |\mathcal{A}|^{2}/\mathcal{H}_{z}$$

$$\therefore \sum_{min} = \frac{\lambda_{eqTDT}}{\lambda_{m}} (\frac{3600s}{hr}) (\frac{180^{0}}{11^{-}}) = \frac{4.08\times10^{-13}}{1.77\times10^{-7}} (3600) (\frac{180^{0}}{11^{-}}) = 0.476 (9/hr)/\sqrt{112}.$$

And finally:

$$ARW = \frac{1}{60} \mathcal{S}_{2min} = \frac{1}{60}(0.476) = (0.0079 9/hr = ARW) \Rightarrow Navigation grade!$$

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