

# EE C247B - ME C218 Introduction to MEMS Design Spring 2018

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Lecture Module 8: Microstructural Elements

FF C245: Introduction to MFMS Design

LecM 8

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9/28/07

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### Outline

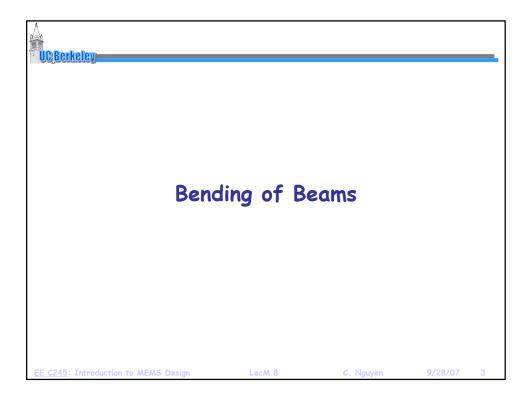
- Reading: Senturia, Chpt. 9
- Lecture Topics:
  - ♦ Bending of beams
  - Scantilever beam under small deflections
  - Scombining cantilevers in series and parallel
  - ♦ Folded suspensions
  - ♦ Design implications of residual stress and stress gradients

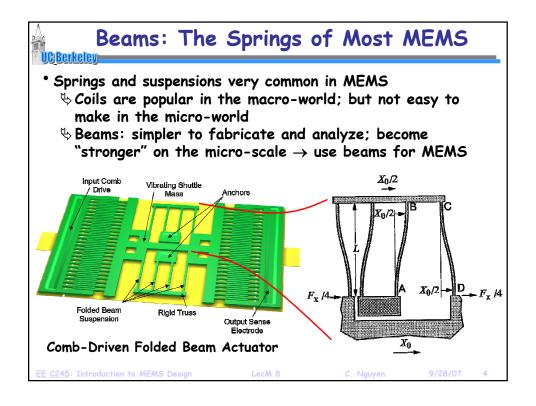
E C245: Introduction to MEMS Design

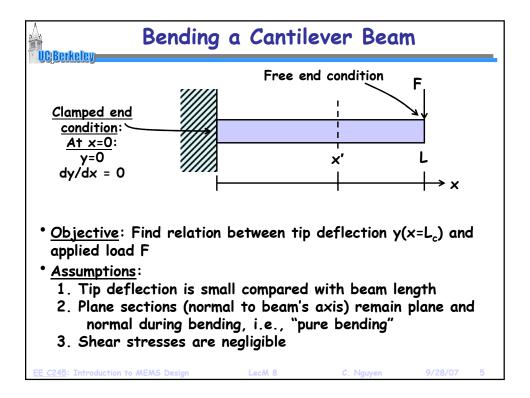
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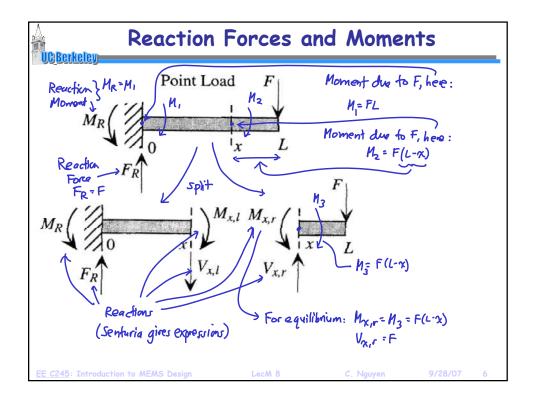
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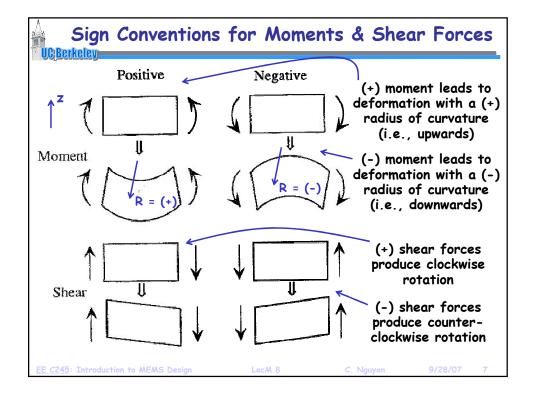
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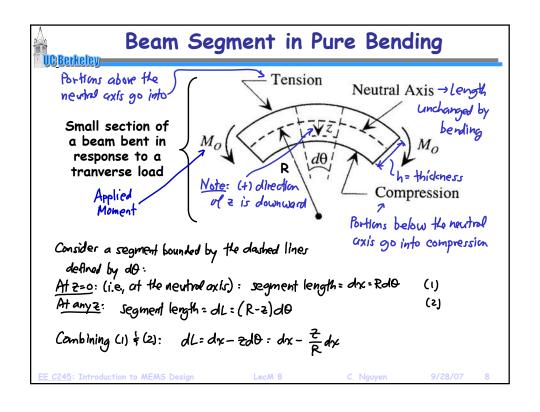


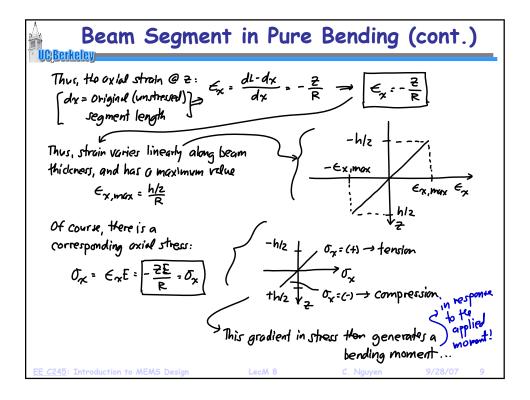


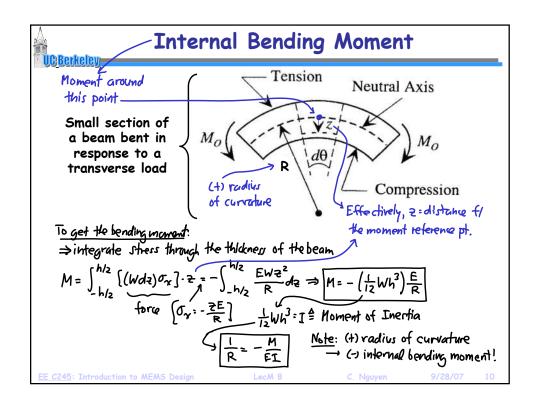


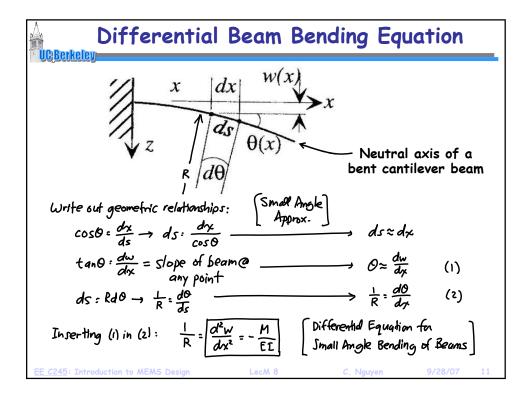


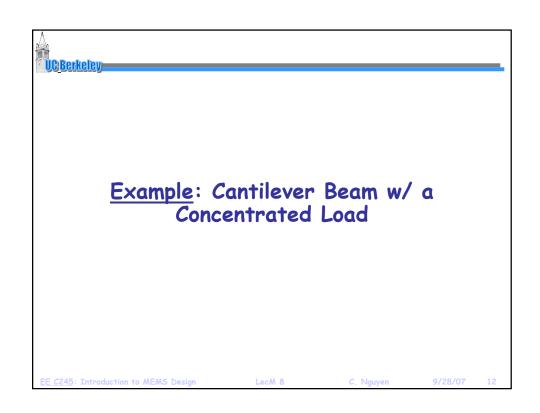


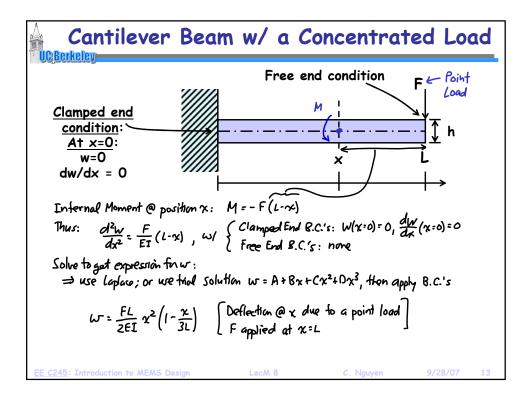


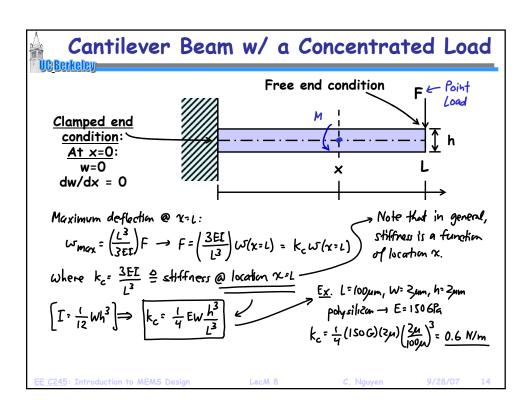


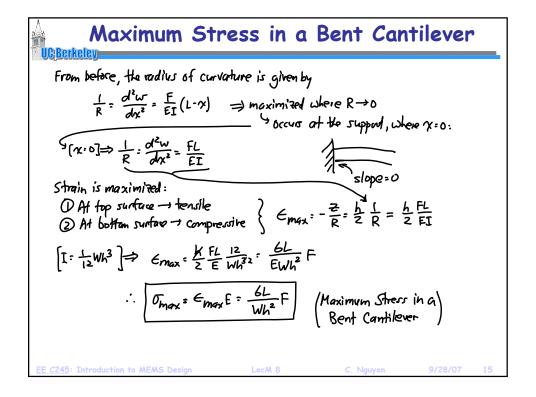


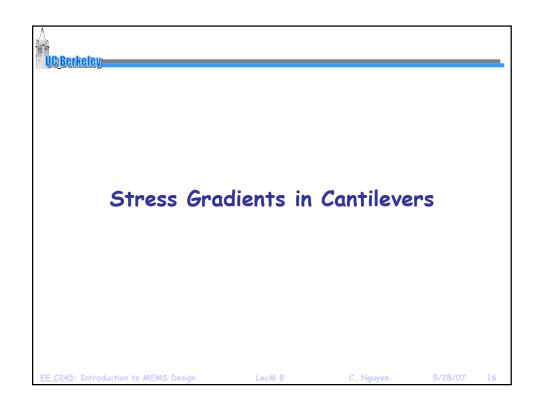


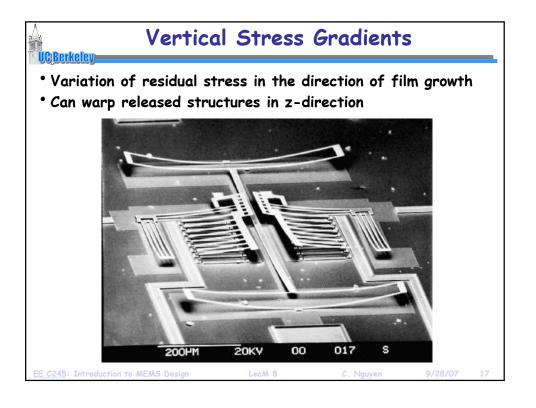


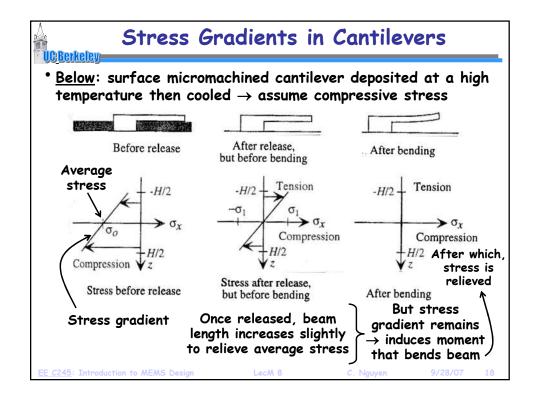


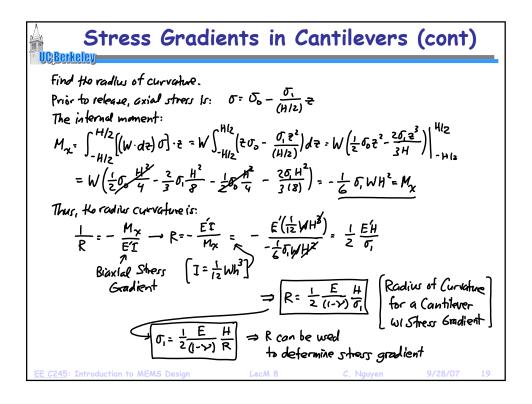


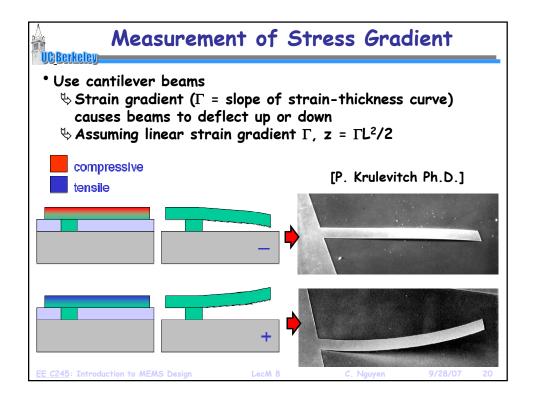


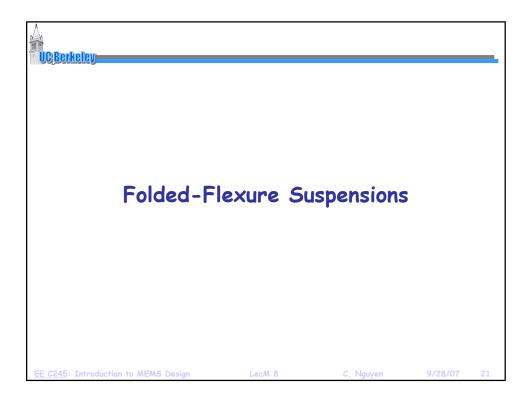


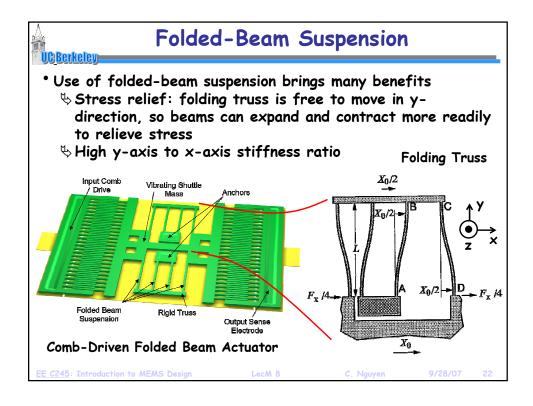


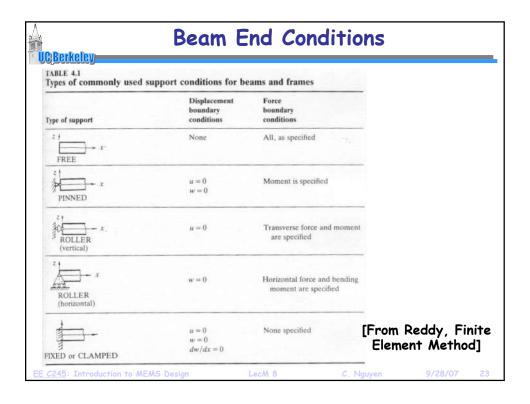


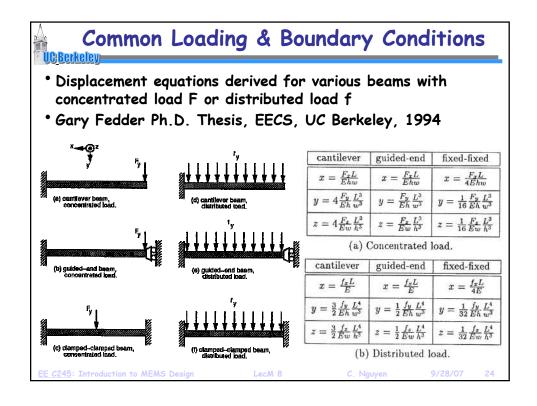


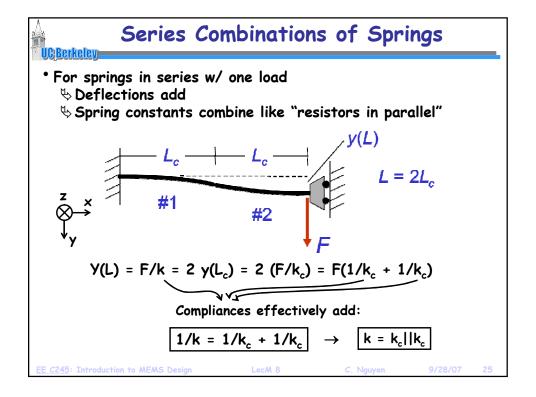


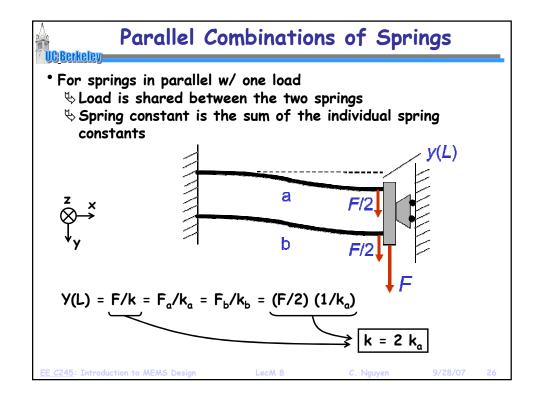


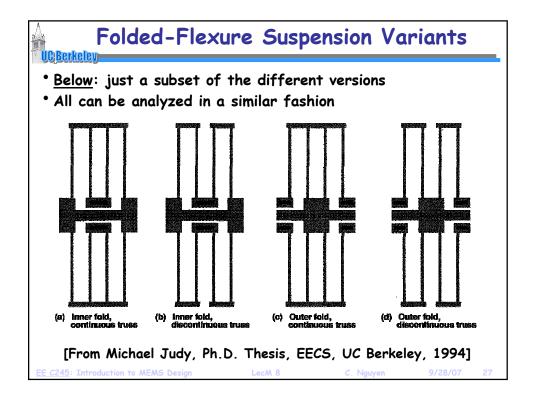


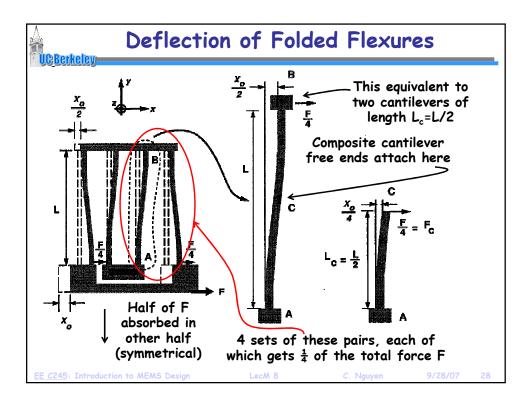


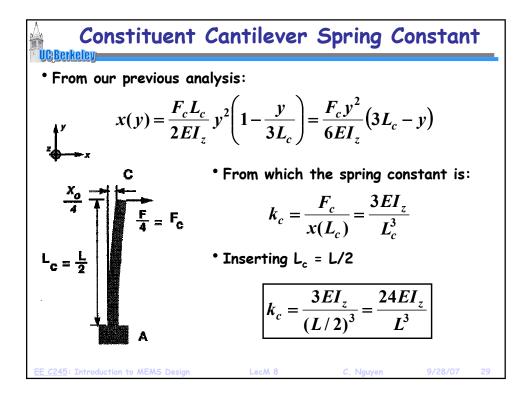


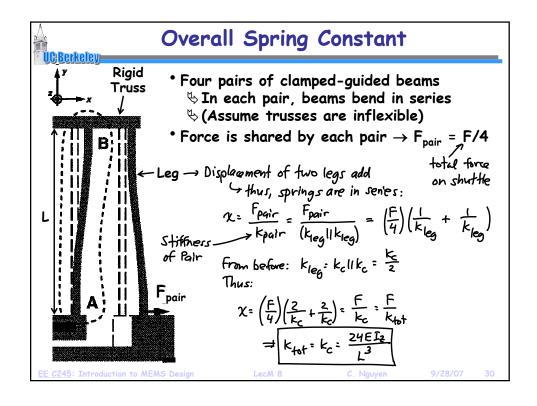


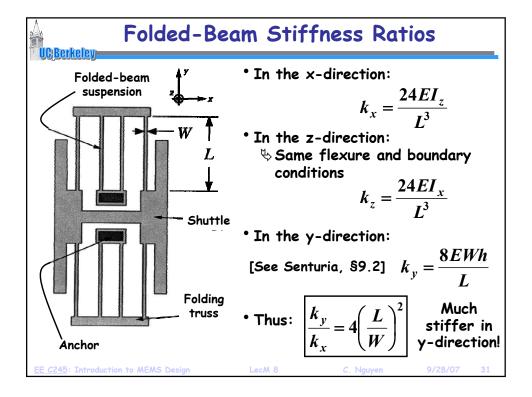


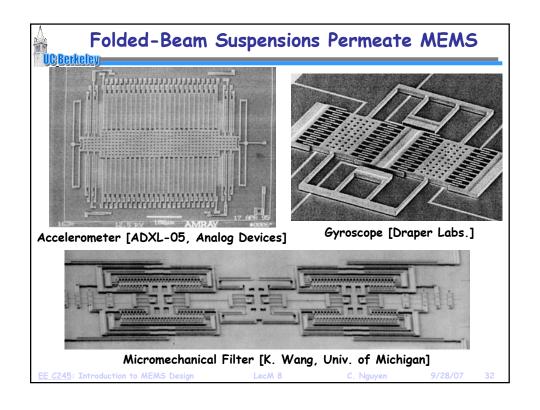


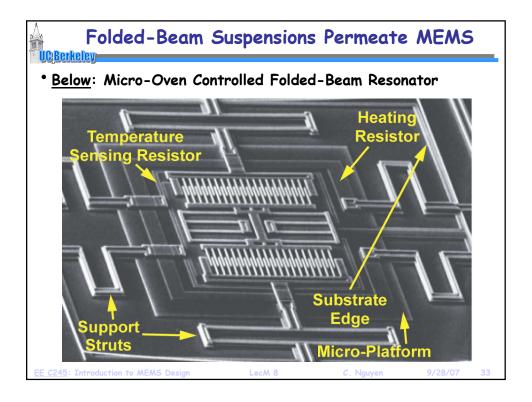


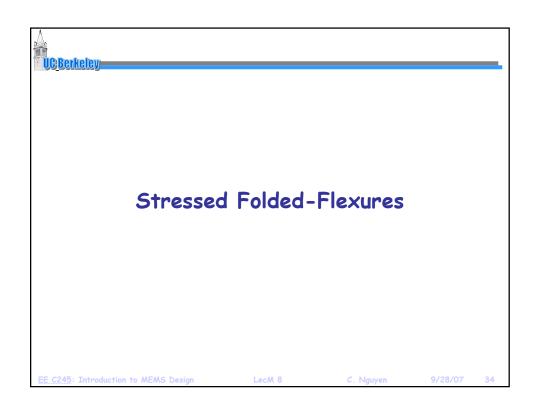


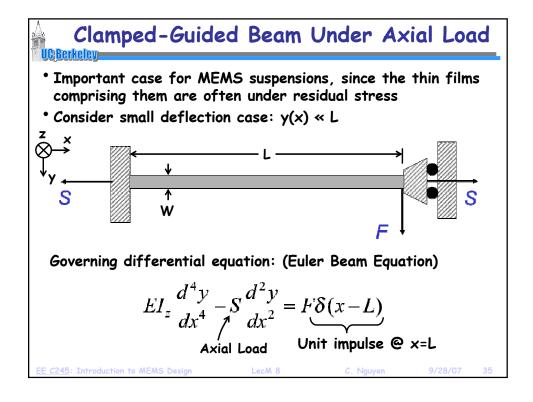


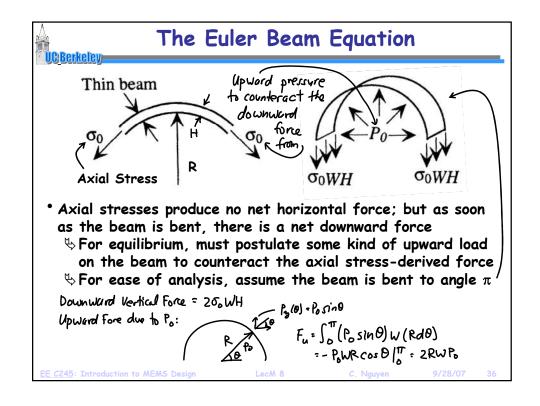


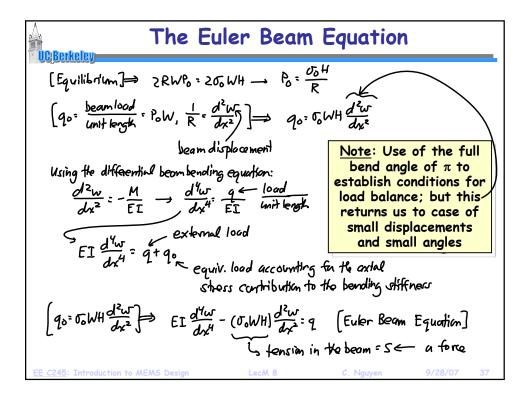


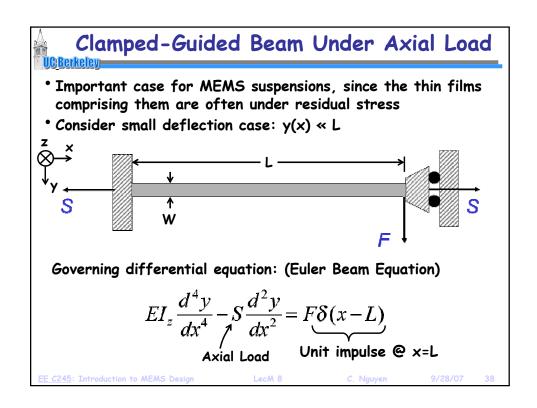












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Module 8: Microstructural Elements

## Solving the ODE

- \* Can solve the ODE using standard methods
  - Senturia, pp. 232-235: solves ODE for case of point load on a clamped-clamped beam (which defines B.C.'s)
  - ♥ For solution to the clamped-guided case: see S.
    Timoshenko, Strength of Materials II: Advanced Theory and Problems, McGraw-Hill, New York, 3<sup>rd</sup> Ed., 1955
- Result from Timoshenko:

S > 0 (tension) 
$$k^{-1} = \frac{pL - 2\tanh(pL/2)}{pS|} = \frac{y(x = L)}{F}$$

S < 0 (compression)

$$k^{-1}=\frac{-pL+2\tan(pL/2)}{p|S|}=\frac{y(x=L)}{F}$$
 where  $p=\sqrt{\frac{|S|}{FI}}$ 

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