

### Basic Concept: Scaling Guitar Strings

**Guitar String**

Vib. Amplitude vs Freq. (110 Hz)

Low Q vs High Q

Vibrating "A" String (110 Hz)

**Stiffness**

**Mass**

**Freq. Equation:**

$$f_o = \frac{1}{2\pi} \sqrt{\frac{k_r}{m_r}}$$

**Micro-mechanical Resonator**

Metallized Electrode, Polysilicon Clamped-Clamped Beam, Anchor

Dimensions:  $W_r$ ,  $L_r$ ,  $h_r$

**Performance:**

- $L_r = 40.8 \mu\text{m}$
- $m_r \sim 10^{-13} \text{ kg}$
- $W_r = 8 \mu\text{m}$ ,  $h_r = 2 \mu\text{m}$
- $d = 1000 \text{ \AA}$ ,  $V_p = 5 \text{ V}$
- Press. = 70 mTorr

[Bannon 1996]

$f_o = 8.5 \text{ MHz}$   
 $Q_{vac} = 8,000$   
 $Q_{air} \sim 50$

Transmission [dB] vs Frequency [MHz]

### 3CC 3λ/4 Bridged μMechanical Filter

**Performance:**

- $f_o = 9 \text{ MHz}$ ,  $BW = 20 \text{ kHz}$ ,  $PBW = 0.2\%$
- I.L. = 2.79 dB, Stop. Rej. = 51 dB
- 20 dB S.F. = 1.95, 40 dB S.F. = 6.45

**Design:**

- $L_r = 40 \mu\text{m}$
- $W_r = 6.5 \mu\text{m}$
- $h_r = 2 \mu\text{m}$
- $L_c = 3.5 \mu\text{m}$
- $L_b = 1.6 \mu\text{m}$
- $V_p = 10.47 \text{ V}$
- $P = -5 \text{ dBm}$
- $R_Q = R_{Qo} = 12 \text{ k}\Omega$

Transmission [dB] vs Frequency [MHz]

Loss Pole, Sharper roll-off

[S.-S. Li, Nguyen, FCS'05]

[Li, et al., UFFCS'04]

### Micromechanical Filter Circuit

Input  $v_i$ , Output  $v_o$

Resonator, Bridging Beam, Coupling Beam

Dimensions:  $\lambda/4$ ,  $3\lambda/4$

Equivalent Circuit Model:

- Series elements:  $m_r$ ,  $1/k_r$ ,  $c_r$
- Shunt elements:  $1/k_s$ ,  $-1/k_s$
- Other parameters:  $\eta$ ,  $\eta_c$ ,  $\eta_b$ ,  $1/k_b$

### 1.51-GHz, Q=11,555 Nanocrystalline Diamond Disk μMechanical Resonator

**Design/Performance:**

- $R = 10 \mu\text{m}$ ,  $t = 2.2 \mu\text{m}$ ,  $d = 800 \text{ \AA}$ ,  $V_p = 7 \text{ V}$
- $f_o = 1.51 \text{ GHz}$  (2<sup>nd</sup> mode),  $Q = 11,555$

Mixed Amplitude [dB] vs Frequency [MHz]

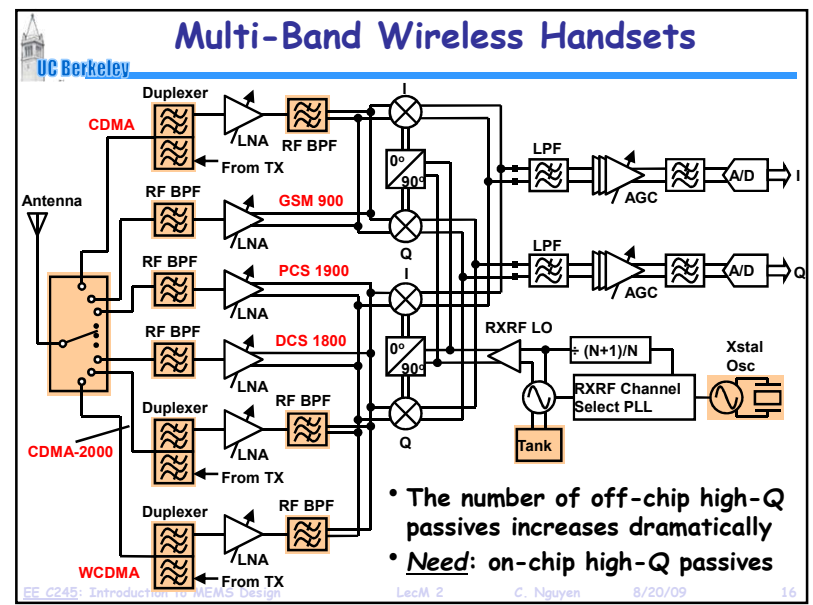
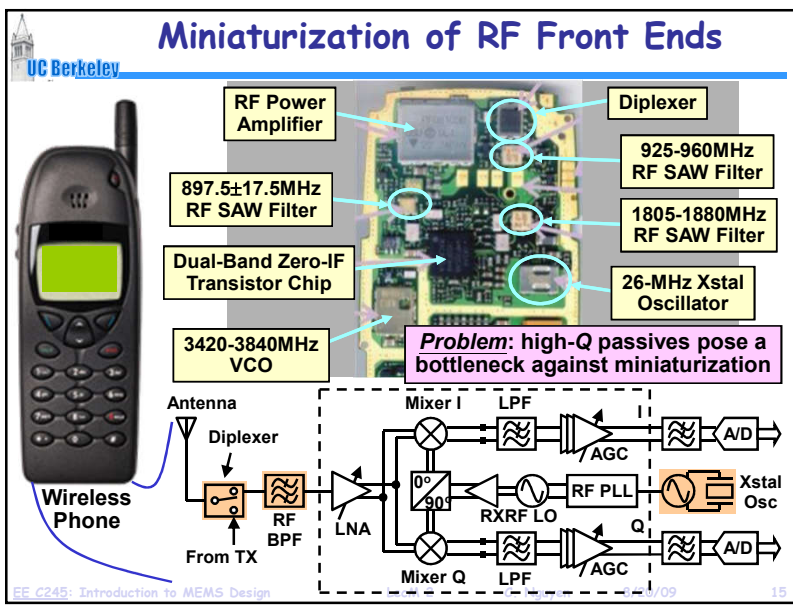
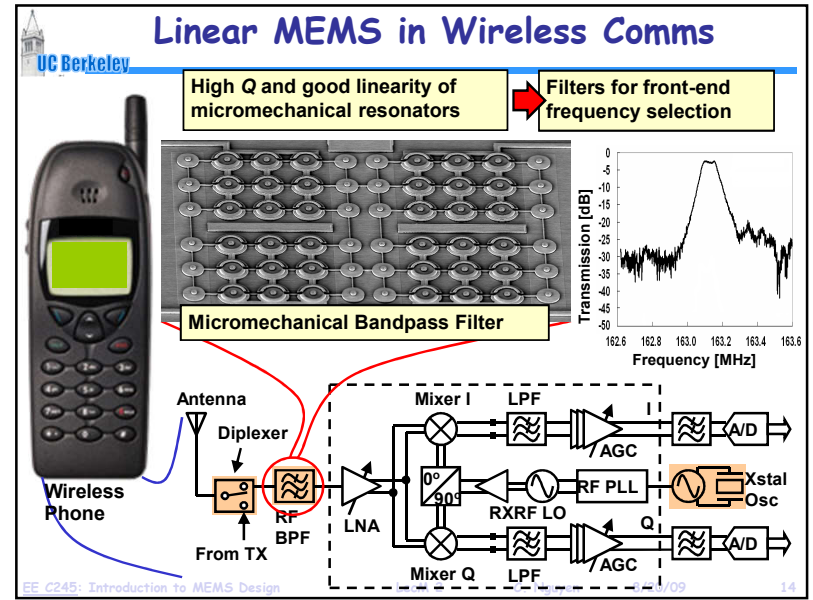
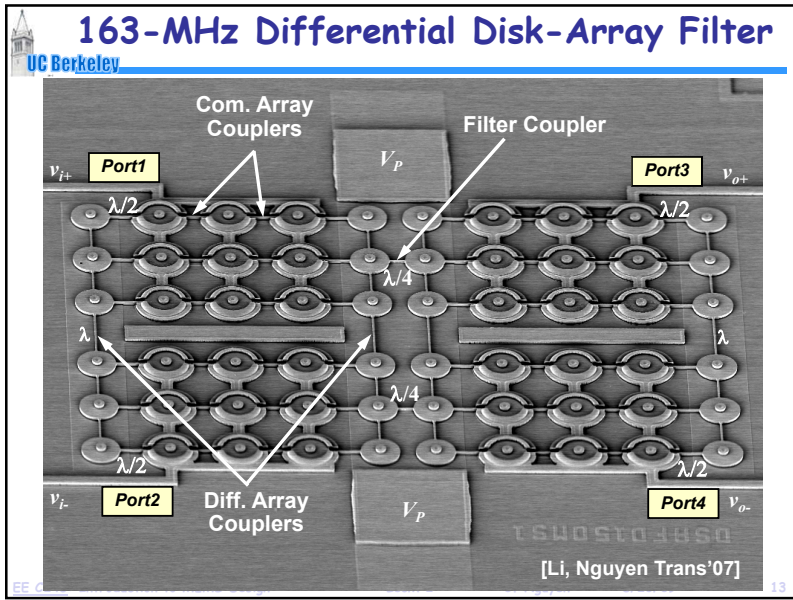
$f_o = 1.51 \text{ GHz}$   
 $Q = 11,555$  (vac)  
 $Q = 10,100$  (air)

**Q = 10,100 (air)**

Polysilicon Stem (Impedance Mismatched to Diamond Disk)

Polysilicon Electrode, CVD Diamond μMechanical Disk Resonator, Ground Plane

[Wang, Butler, Nguyen MEMS'04]



### All High-Q Passives on a Single Chip

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### Chip-Scale Atomic Clocks (CSAC)

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### NIST F1 Fountain Atomic Clock

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Vol:  $\sim 3.7 \text{ m}^3$   
 Power:  $\sim 500 \text{ W}$   
 Acc:  $1 \times 10^{-15}$   
 Stab:  $3.3 \times 10^{-15}/\text{hr}$

After 1 sec  $\Rightarrow$  Error:  $10^{-15}$  sec

Loses 1 sec every 30 million years!

Physics Package

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### Benefits of Accurate Portable Timing

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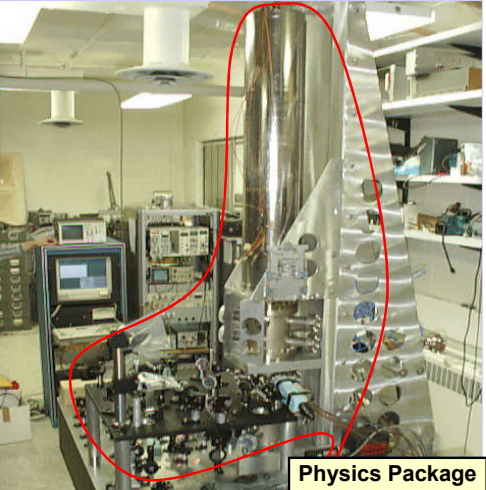
**Better Timing**

**Networked Sensors**

- Secure Communications
- More efficient spectrum utilization
- Longer autonomy periods
- Faster frequency hop rates
- Faster acquire of pseudorandom signals
- Superior resilience against jamming or interception
- Larger networks with longer autonomy
- GPS
- Fewer satellites needed
- Higher jamming margin
- Faster GPS acquire

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### NIST F1 Fountain Atomic Clock



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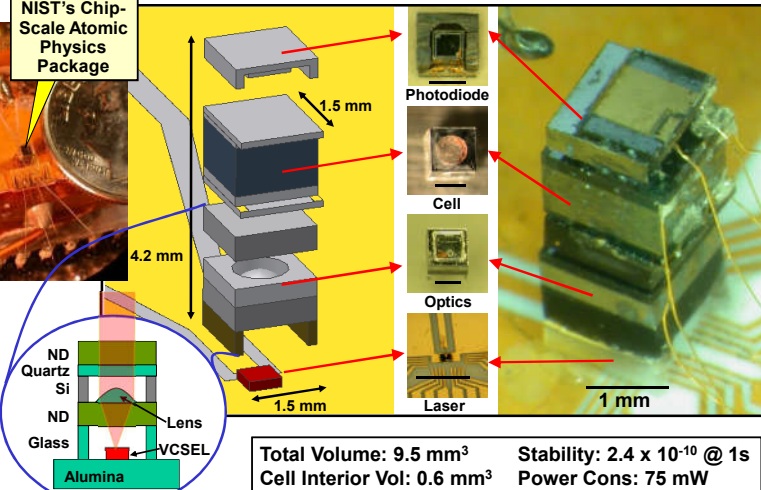
After 1 sec  $\Rightarrow$   
 Error:  $10^{-15}$  sec

Loses 1 sec every  
 30 million years!

Physics Package

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### 1<sup>st</sup> Chip-Scale Atomic Physics Package



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NIST's Chip-Scale Atomic Physics Package

Photodiode  
 Cell  
 Optics  
 Laser

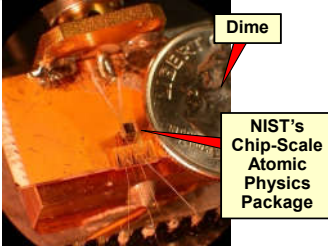
1.5 mm  
 4.2 mm  
 1.5 mm  
 1 mm

ND  
 Quartz  
 Si  
 ND  
 Glass  
 Alumina  
 Lens  
 VCSEL

Total Volume:  $9.5 \text{ mm}^3$  Stability:  $2.4 \times 10^{-10}$  @ 1s  
 Cell Interior Vol:  $0.6 \text{ mm}^3$  Power Cons: 75 mW

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### Tiny Physics Package Performance



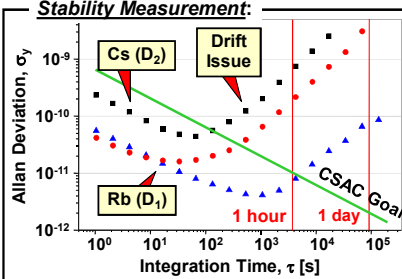
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Dime

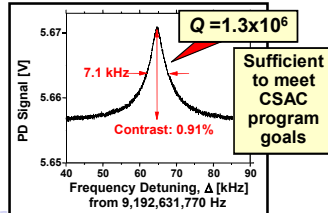
NIST's Chip-Scale Atomic Physics Package

- Experimental Conditions:
  - Cs D2 Excitation
  - External (large) Magnetic Shielding
  - External Electronics & LO
  - Cell Temperature:  $\sim 80 \text{ }^\circ\text{C}$
  - Cell Heater Power: 69 mW
  - Laser Current/Voltage: 2mA / 2V
  - RF Laser Mod Power: 70 $\mu$ W

Stability Measurement:



Open Loop Resonance:

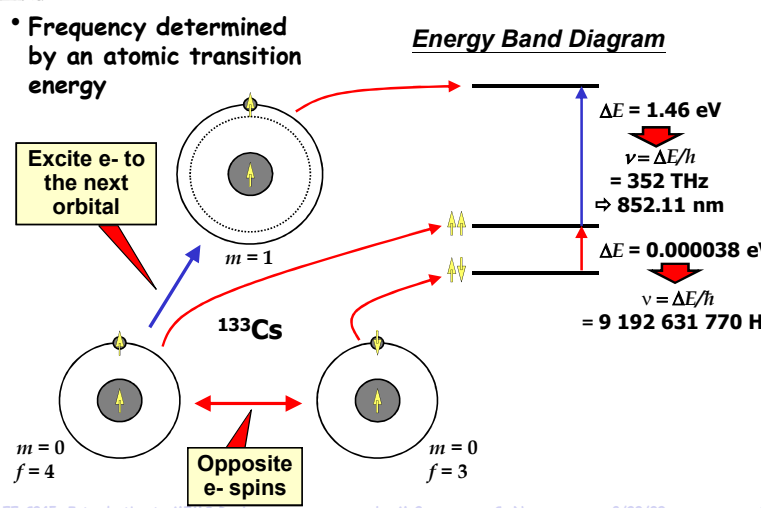


Q =  $1.3 \times 10^6$   
 7.1 kHz  
 Contrast: 0.91%

Sufficient to meet CSAC program goals

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### Atomic Clock Fundamentals



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- Frequency determined by an atomic transition energy

Energy Band Diagram

$\Delta E = 1.46 \text{ eV}$   
 $\nu = \Delta E/h = 352 \text{ THz}$   
 $\Rightarrow 852.11 \text{ nm}$

$\Delta E = 0.000038 \text{ eV}$   
 $\nu = \Delta E/h = 9\,192\,631\,770 \text{ Hz}$

Excite e- to the next orbital

133Cs

Opposite e- spins

$m = 1$   
 $m = 0$   
 $f = 4$   
 $f = 3$

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