

EE C247B - ME C218 Introduction to MEMS Design Spring 2019

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Lecture Module 15: Gyros, Noise, & MDS

EE C245: Introduction to MEMS Design

ecM 15

C. Nguyen

11/18/08

UC Berkeley.

Lecture Outline

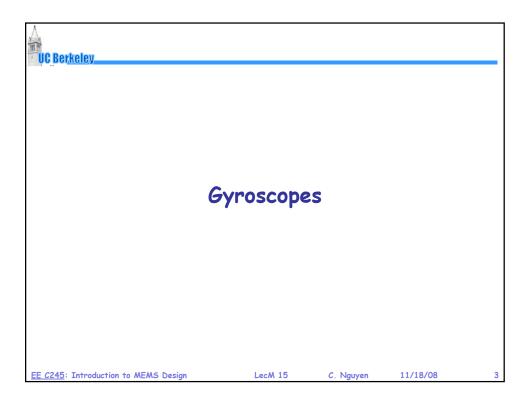
- Reading: Senturia, Chpt. 14, Chpt. 16, Chpt. 21
- Lecture Topics:
 - **♦** Gyroscopes
 - Syro Circuit Modeling
 - ♦ Minimum Detectable Signal (MDS)
 - ◆ Noise
 - ◆ Angle Random Walk (ARW)

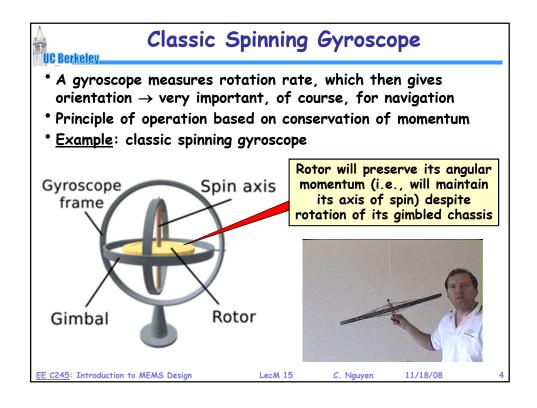
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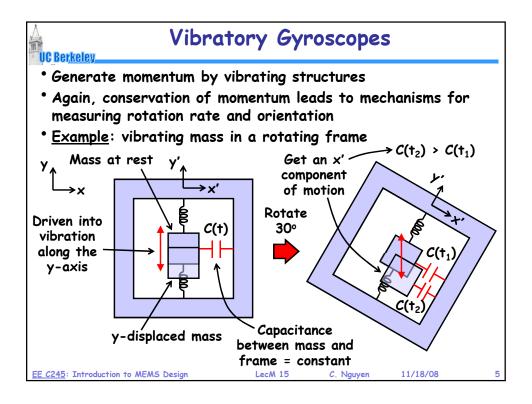
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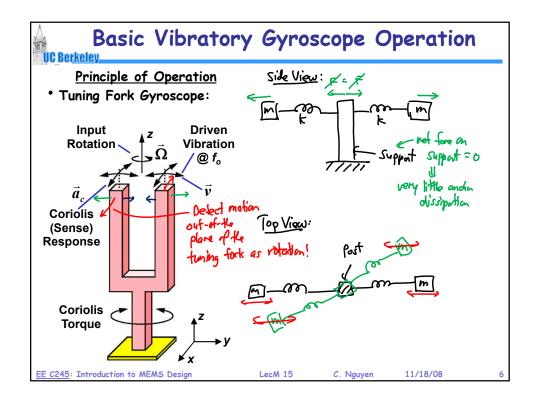
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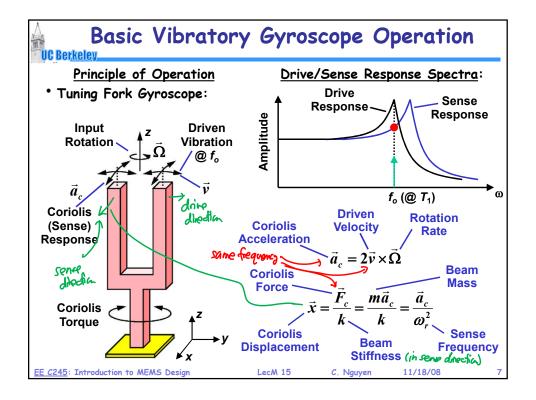
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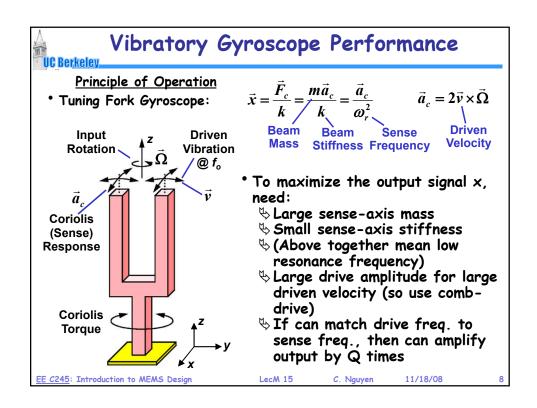


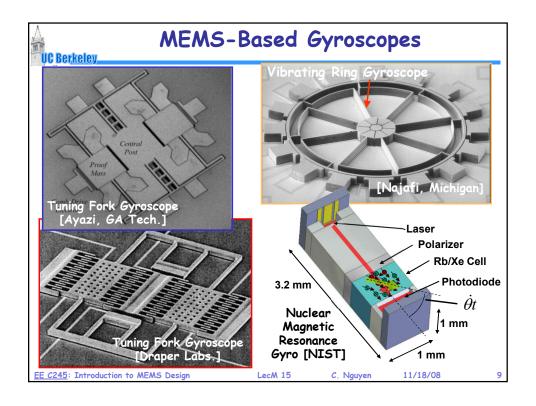


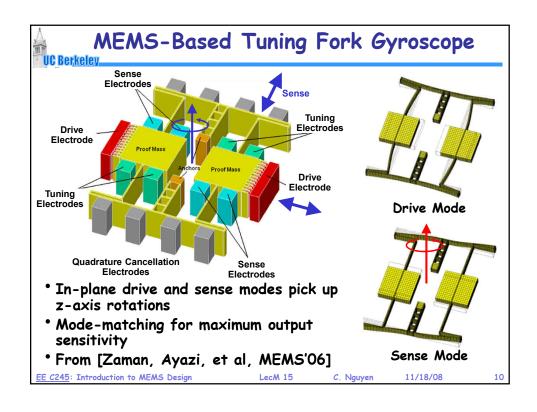


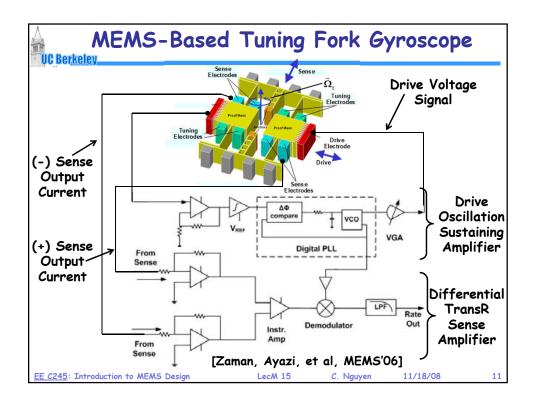


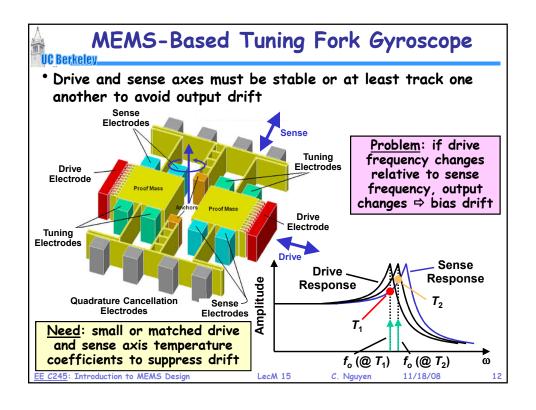


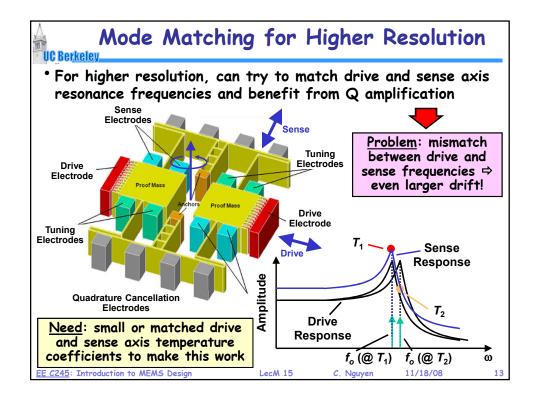


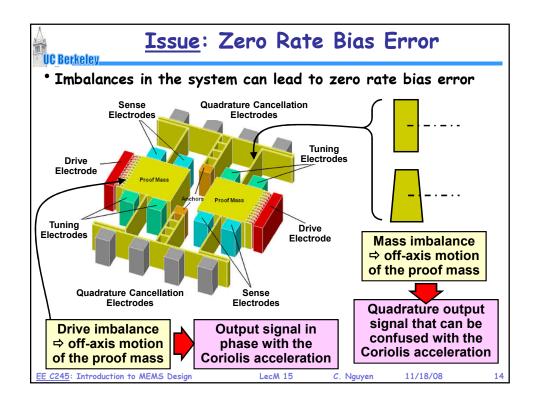




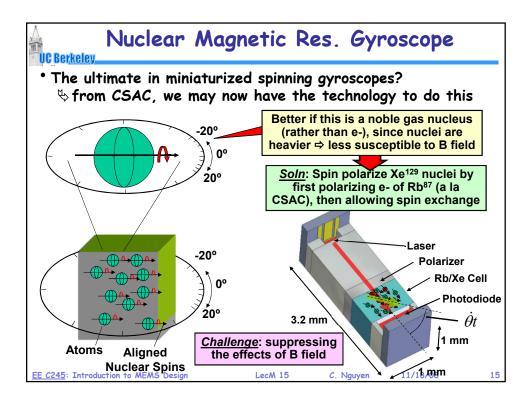


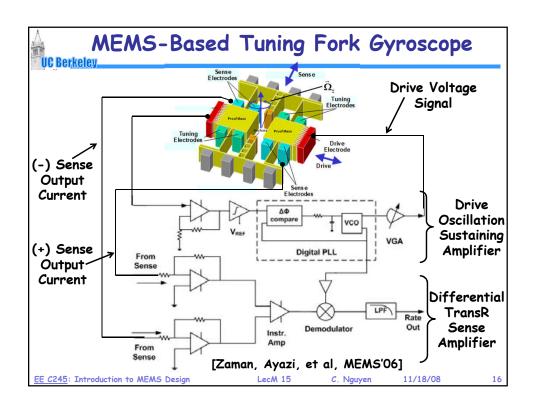


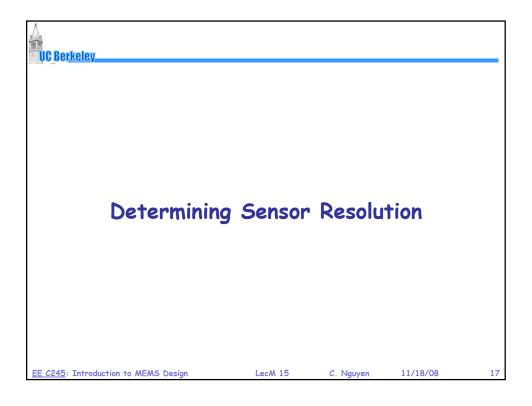


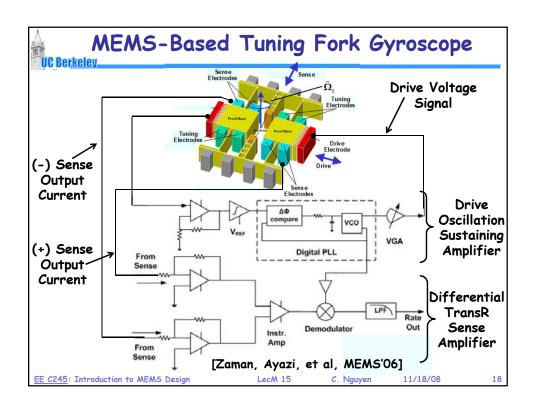


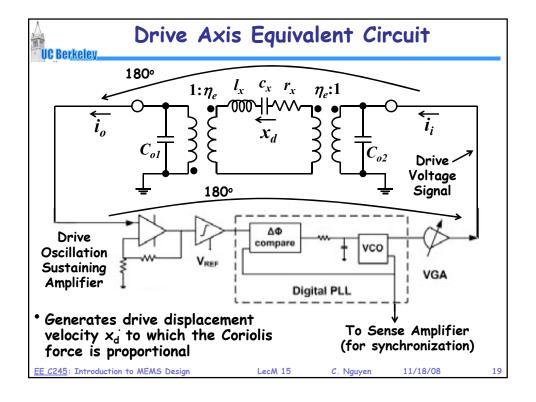
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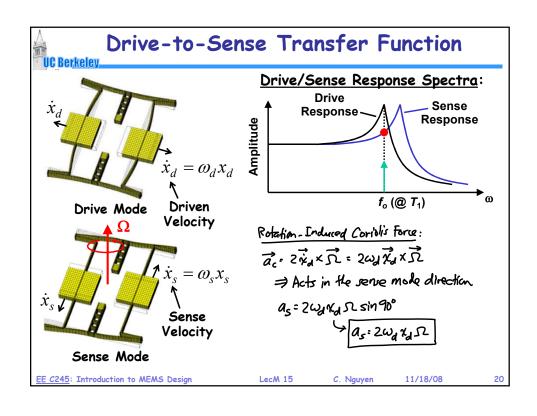


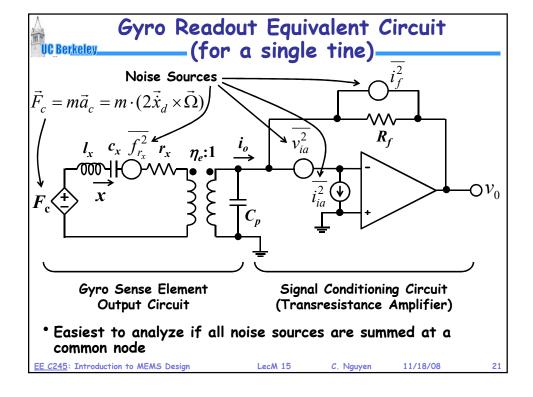


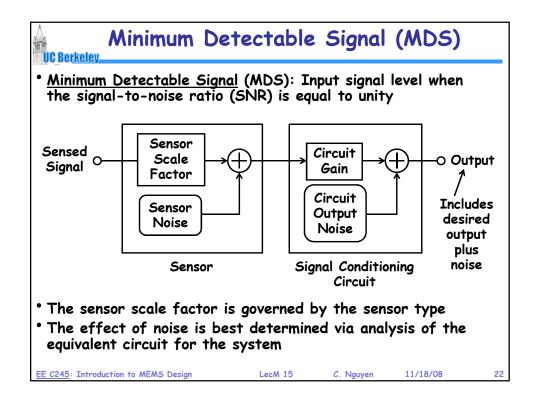


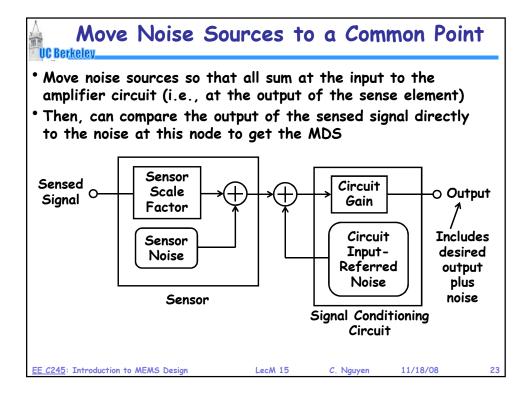


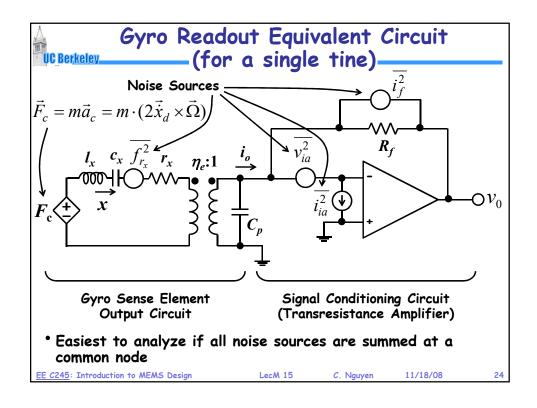


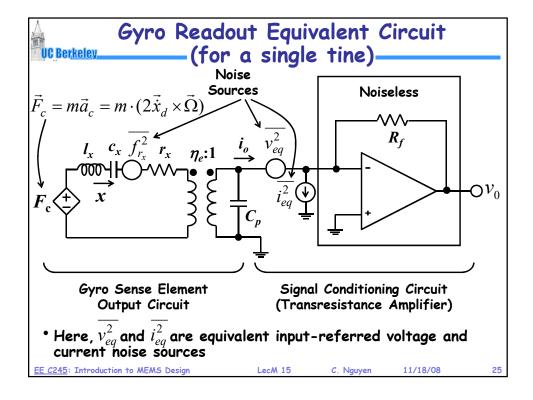


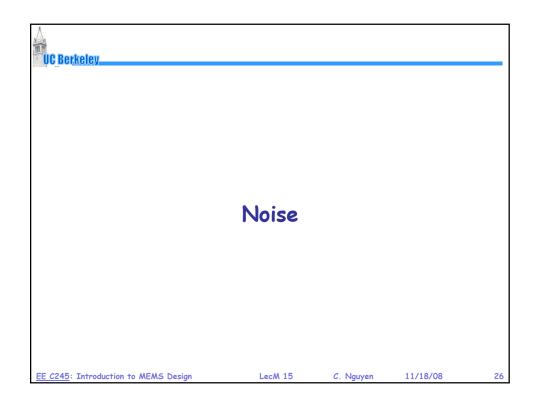






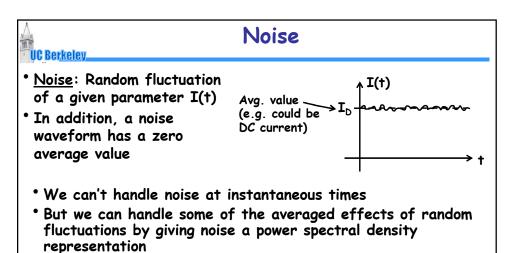






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Module 15: Gyros, Noise & MDS



Thus, represent noise by its mean-square value:

Let
$$i(t) = I(t) - I_D$$

Then
$$\overline{i^2} = \overline{\left(I - I_D\right)^2} = \lim_{T \to \infty} \frac{1}{T} \int_0^T \left|I - I_D\right|^2 dt$$

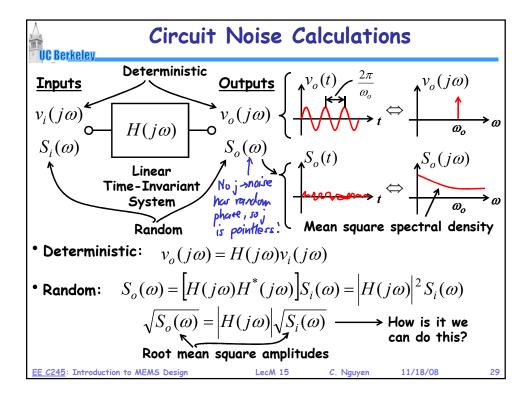
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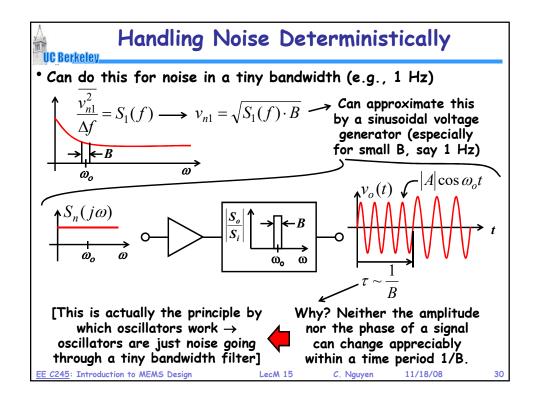
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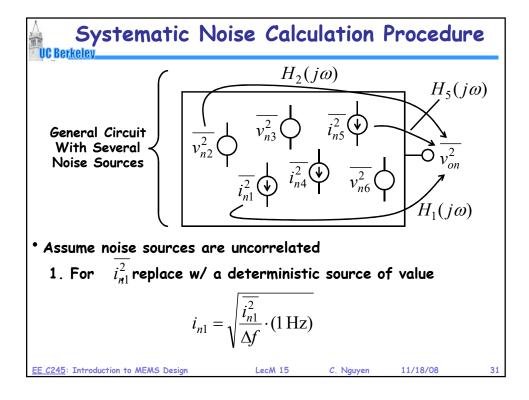
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Noise Spectral Density UC Berkeley We can plot the spectral density of this mean-square value: [units2/Hz] One-sided spectral density → used in circuits → measured by spectrum analyzers Two-sided spectral density \overline{i}^2 = integrated mean-square (1/2 the one-sided) noise spectral density over all frequencies (area under Often used in the curve) systems courses EE C245: Introduction to MEMS Design







Systematic Noise Calculation Procedure

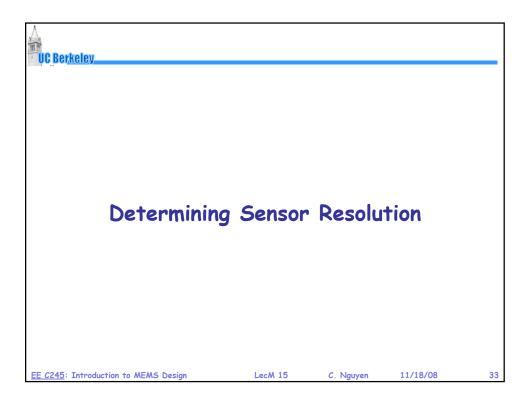
- 2. Calculate $v_{on1}(\omega)=i_{n1}(\omega)H(j\omega)$ (treating it like a deterministic signal)
- 3. Determine $v_{on1}^2 = \overline{i_{n1}^2} \cdot \left| H(j\omega) \right|^2$ 4. Repeat for each noise source: $\overline{i_{n1}^2}$, $\overline{v_{n2}^2}$, $\overline{v_{n3}^2}$
- 5. Add noise power (mean square values)

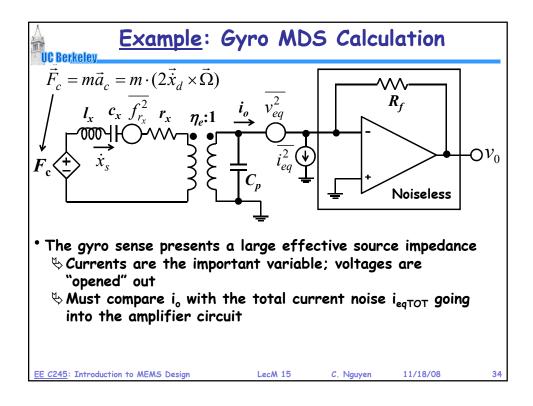
$$\overline{v_{onTOT}^2} = \overline{v_{on1}^2} + \overline{v_{on2}^2} + \overline{v_{on3}^2} + \overline{v_{on4}^2} + \cdots$$

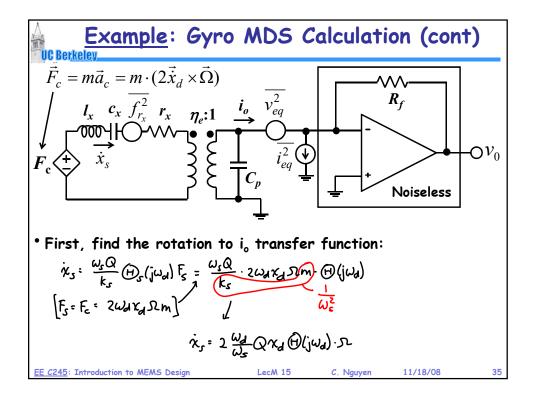
$$v_{onTOT} = \sqrt{\overline{v_{on1}^2} + \overline{v_{on2}^2} + \overline{v_{on3}^2} + \overline{v_{on4}^2} + \cdots}$$

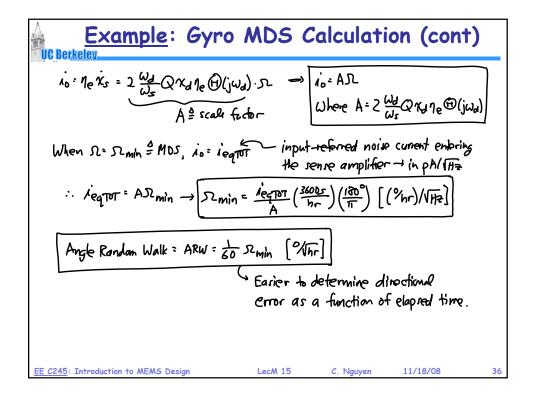
Total rms value

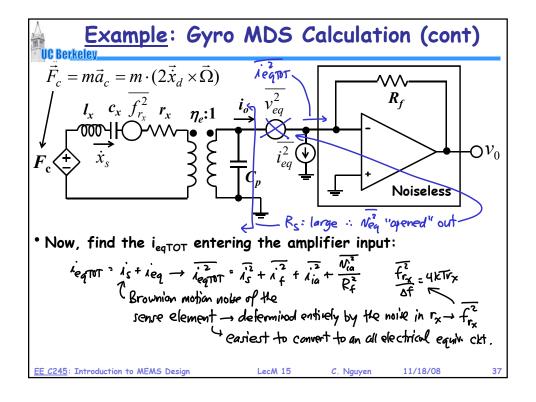
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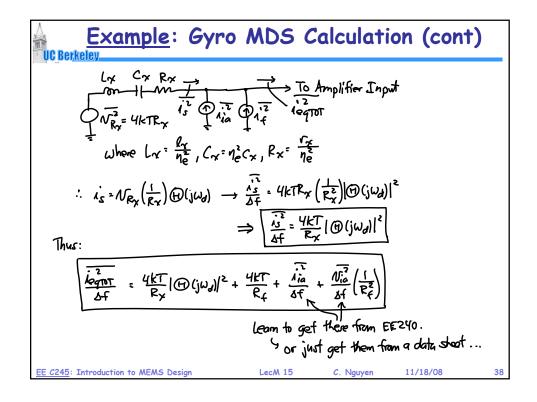


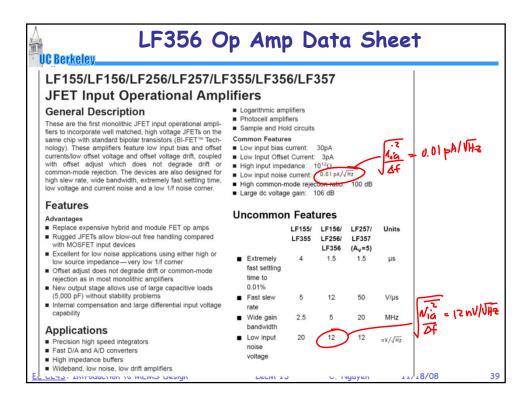


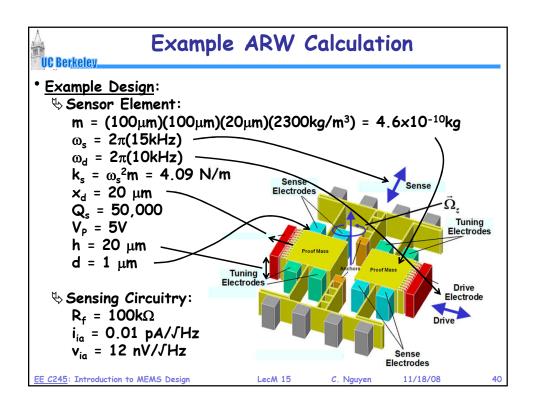












Example ARW Calculation (cont)

(Continue Berkeley)

Get notation rate to output current scale factor:

$$A = 2 \frac{\omega_d}{\omega_s} Q_s \kappa_d \eta_e \left(\frac{1}{3} \left(\frac{1}$$

Example ARW Calculation (cont)

$$\begin{bmatrix}
R_{xy} = \frac{\omega_{sm}}{Q_{y}^{1}} = \frac{2\pi\Gamma(15K)(46X10^{-10})}{(50K)(8.85\%10^{-20})^{2}} = 110.6 k \text{ s.t.}
\end{bmatrix}$$

$$\frac{\lambda_{eq1DT}}{\Delta f} = \frac{(1.66 \times 10^{-20})}{(110.6K)} (0.000024)^{2} + \frac{(1.66 \times 10^{-20})}{1M} + \frac{(0.61)^{2}}{(1M)^{2}} + \frac{(12n)^{2}}{(1M)^{2}}$$

$$\frac{\lambda_{eq1DT}}{\lambda_{f}} = \frac{(1.66 \times 10^{-20})}{(110.6K)} (0.000024)^{2} + \frac{(1.66 \times 10^{-20})}{1M} + \frac{(0.61)^{2}}{(1M)^{2}} + \frac{(12n)^{2}}{(1M)^{2}}$$

$$\frac{\lambda_{eq1DT}}{\lambda_{f}} = \frac{(1.66 \times 10^{-20})^{2}}{(10.6K)} + \frac{\lambda_{eq1DT}}{\lambda_{f}} = \frac{\lambda_{$$

What if
$$\omega_{d} = \omega_{s}$$
?

If $\omega_{d} = \omega_{s} = 15KH^{2}$, then $|\mathbb{D}[j\omega_{d}]| = 1$ and

$$A = 2\frac{\omega_{d}}{\omega_{s}}Q_{s}K_{d}\eta_{e}|\mathbb{D}(j\omega_{d})| = 2Q_{s}K_{d}\eta_{e} = 2(50K)(20\mu)(5)(20006) = 1.77X10^{-7}C$$

Aegist = $\frac{(1.66\times10^{-20})(1)^{2} + \frac{(1.66\times10^{-20})}{1M} + (0.01p)^{2} + \frac{(12n)^{2}}{(1M)^{2}}$

(10.6K)

Now, the sensor element dominates!

$$\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}} = 1.67\times10^{-25}A^{2}/H_{2} \longrightarrow Aeqist = \frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}} = 4.08\times10^{-13}A/\sqrt{H_{2}}$$

$$\therefore \frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}\frac{1}$$