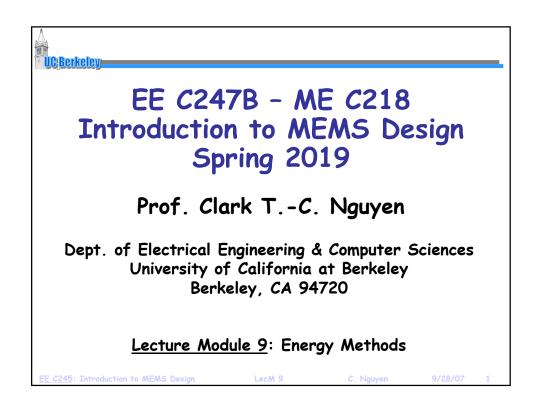
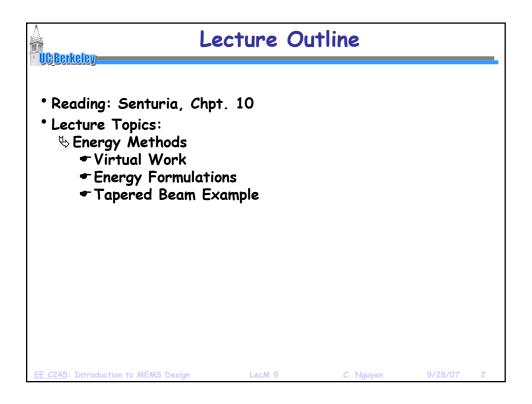
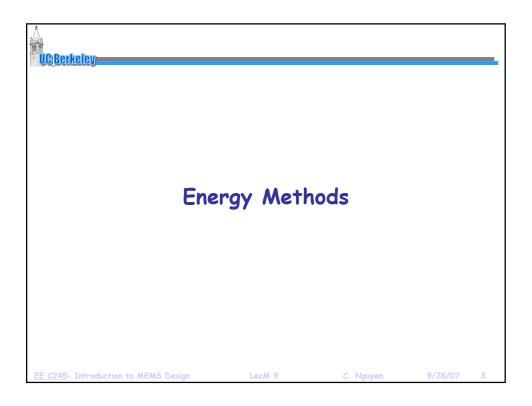
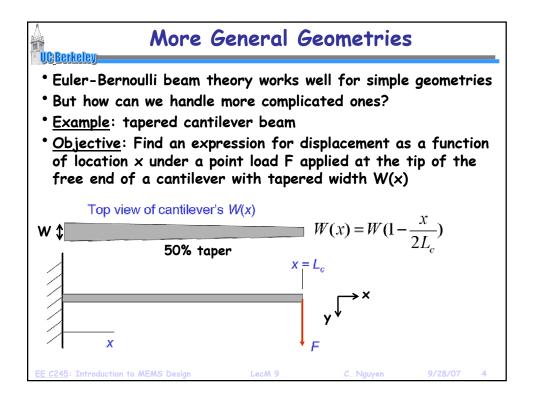
<u>EE 247B/ME 218: Introduction to MEMS Design</u> <u>Module 9: Energy Methods</u>

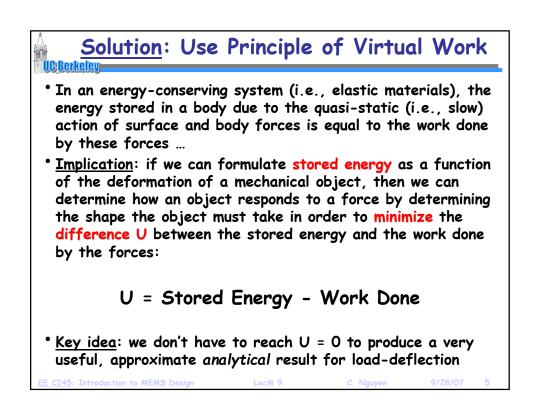


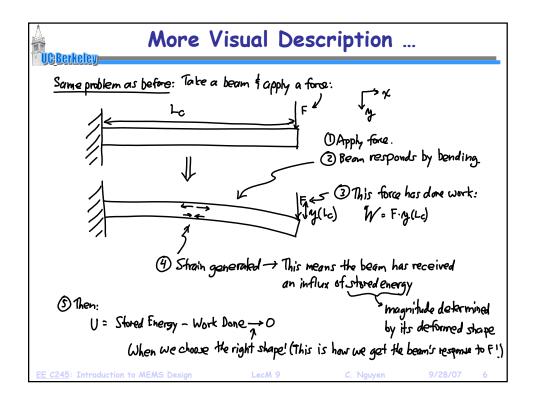


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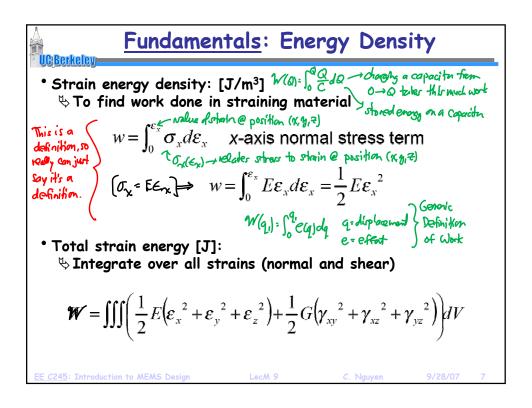


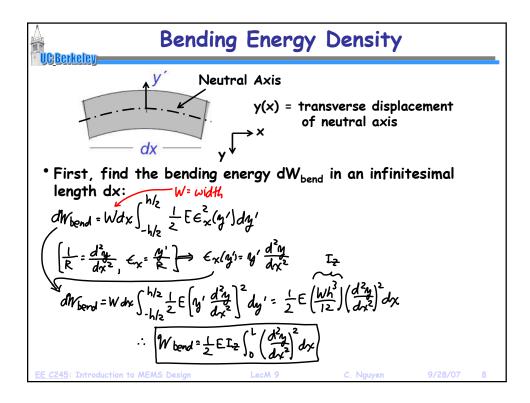


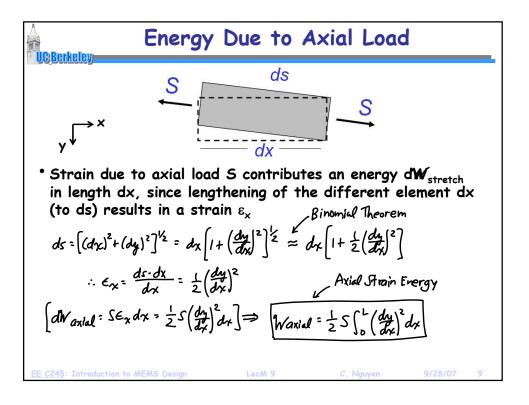


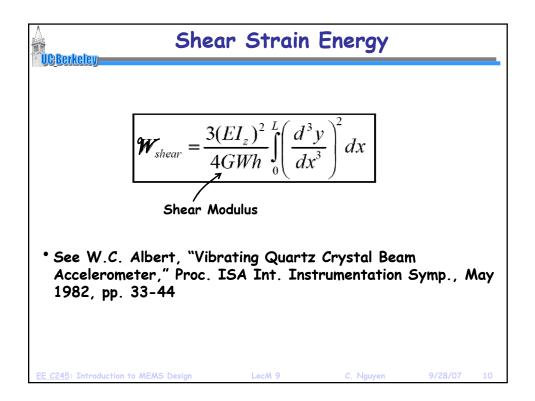


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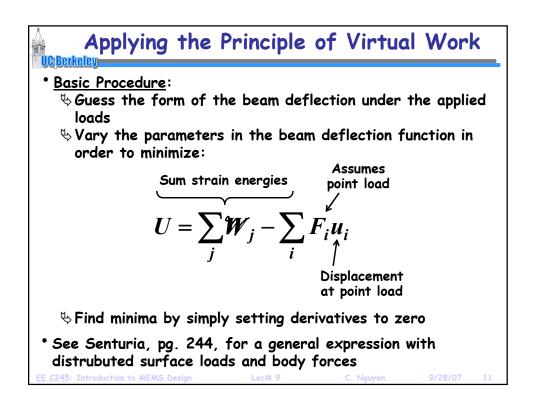


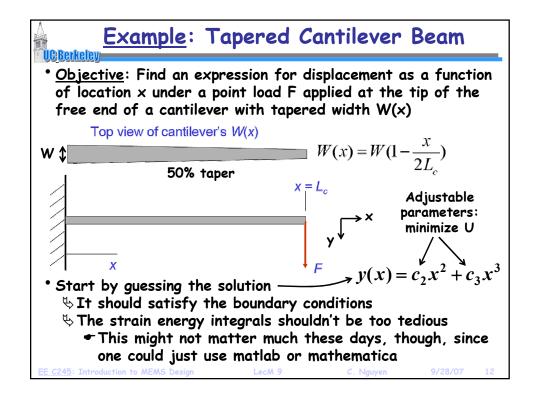






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$$W_{bend} = \frac{1}{2}E\int_{0}^{L_{c}}I_{z}(x)\left(\frac{d^{2}y}{dx^{2}}\right)^{2}dx \quad \text{(Bending Energy)}$$

$$I_{z}(x) = \frac{W(x)h^{3}}{12} \qquad \qquad \frac{d^{2}y}{dx^{2}} = 2c_{2} + 6c_{3}x$$

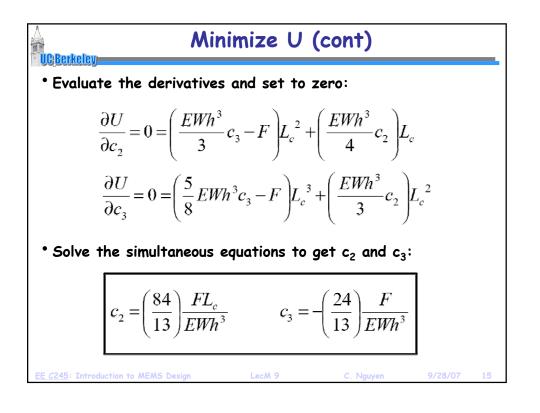
$$W(x) = W(1 - \frac{x}{2L_{c}}) \quad \qquad \text{(Using our guess)}$$

$$I = \frac{1}{24}EWh^{3}\int_{0}^{L_{c}}(1 - \frac{x}{2L_{c}})(2c_{2} + 6c_{3}x)^{2}dx - F(c_{2}L_{c}^{2} + c_{3}L_{c}^{3})$$

$$EE C245: Introduction to MEMS Design \qquad Letting 9 \qquad (2. Nauer 12)$$

Find c_2 and c_3 That Minimize U Minimize U \rightarrow basically, find the c_2 and c_3 that brings U closest to zero (which is what it would be if we had guessed correctly) The c_2 and c_3 that minimize U are the ones for which the partial derivatives of U with respective to them are zero: $\frac{\partial U}{\partial c_2} = 0 \qquad \frac{\partial U}{\partial c_3} = 0$ Proceed: ψ First, evaluate the integral to get an expression for U: $U = EWh^3 \left\{ \frac{5c_3^2}{16} L_c^3 + \frac{c_2c_3}{3} L_c^2 + \frac{c_2^2}{8} L_c \right\} - F(c_2L_c^2 + c_3L_c^3)$

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The Virtual Work-Derived Solution (CREATED SOLUTI

