EE 245: Introduction to MEMS
Module 15: Gyros, Noise & MDS



EE C245 - ME C218 Introduction to MEMS Design Fall 2011

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Lecture Module 15: Gyros, Noise, & MDS

EE C245: Introduction to MEMS Design

LecM 1

C. Nguyen

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Lecture Outline

- Reading: Senturia, Chpt. 14, Chpt. 16, Chpt. 21
- Lecture Topics:
 - **⇔** Gyroscopes
 - Syro Circuit Modeling
 - ♦ Minimum Detectable Signal (MDS)
 - 🕶 Noise
 - ◆ Angle Random Walk (ARW)

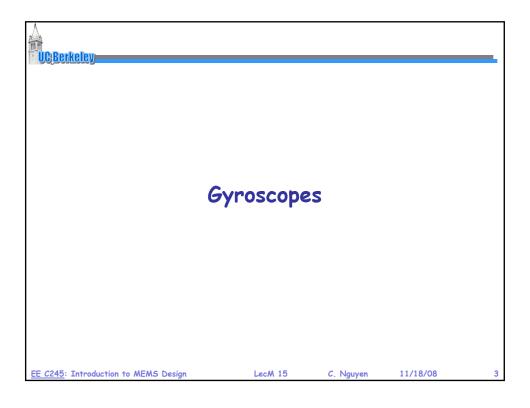
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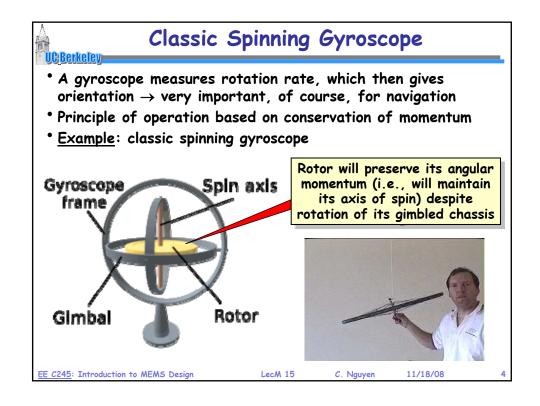
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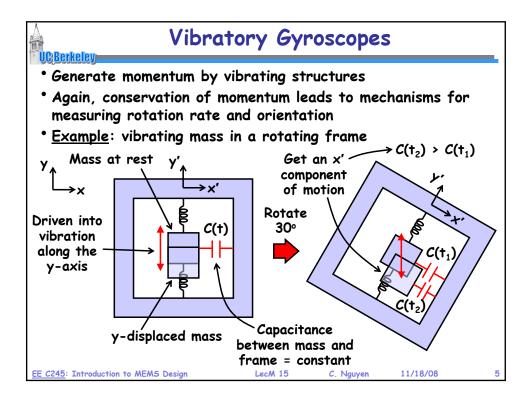
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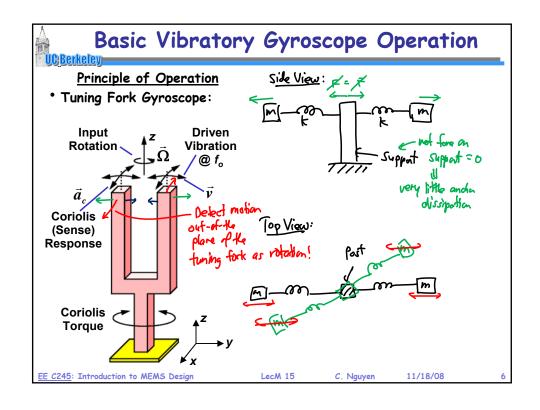
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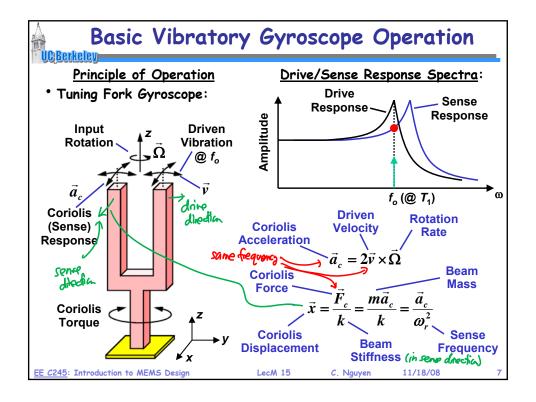
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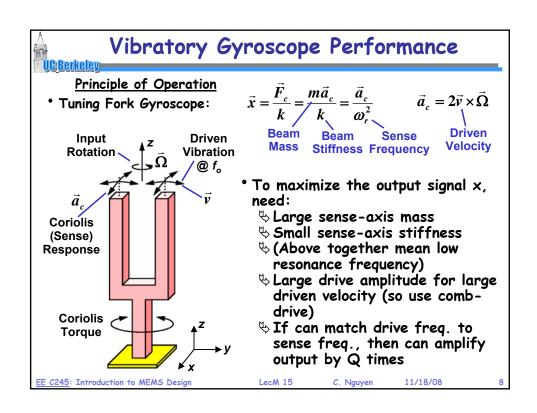


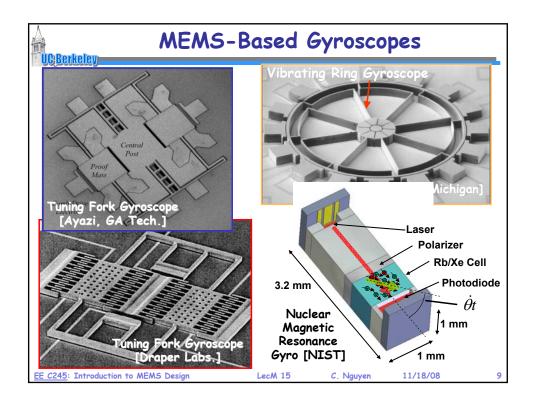


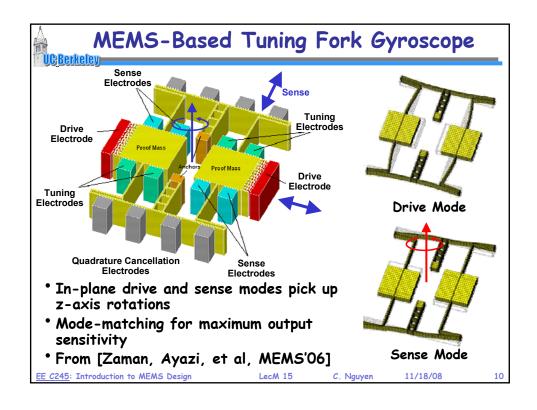


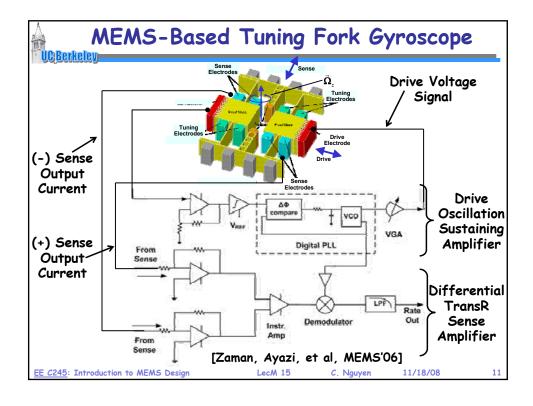


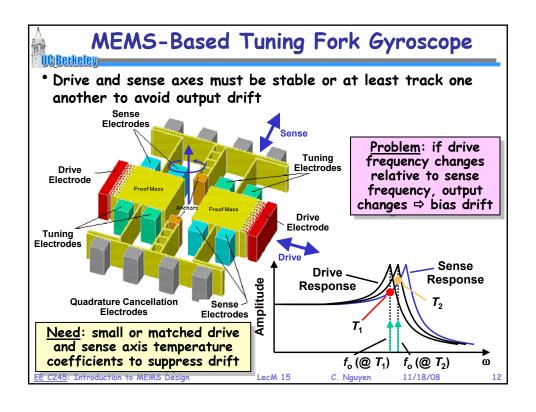


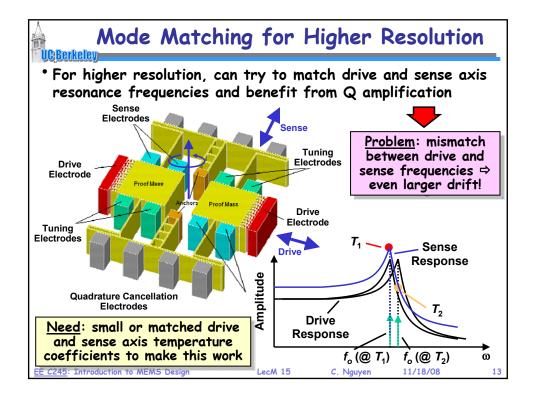


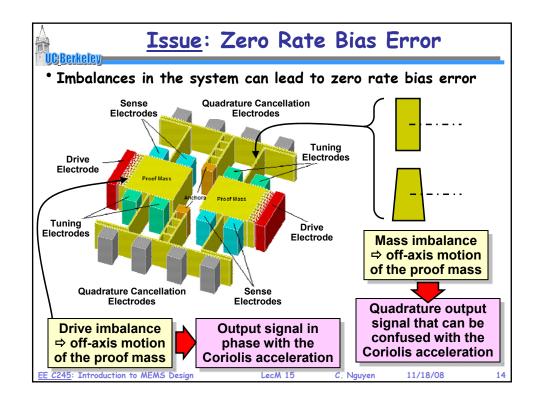


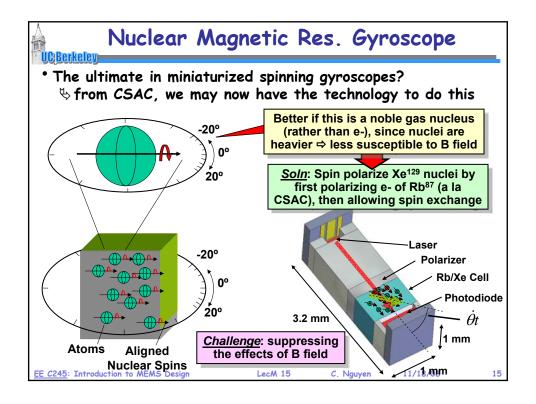


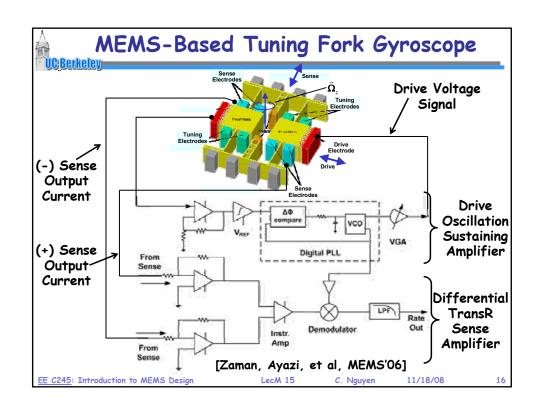


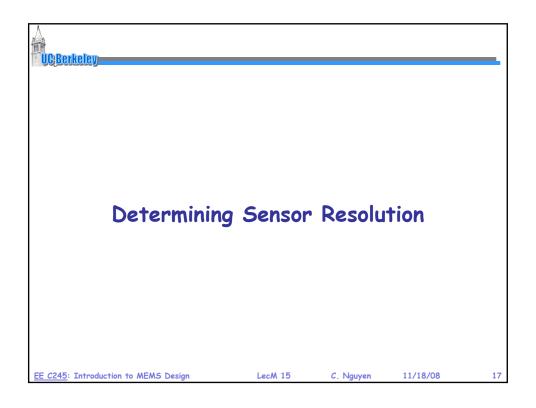


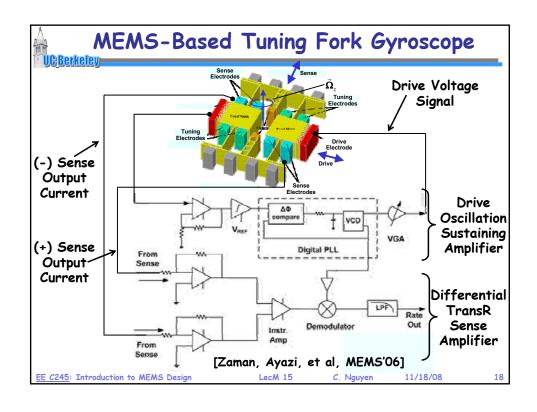






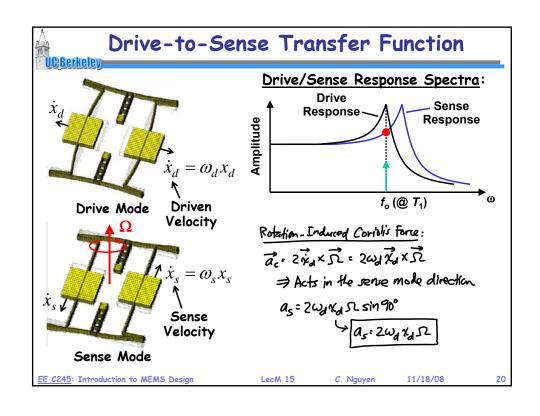




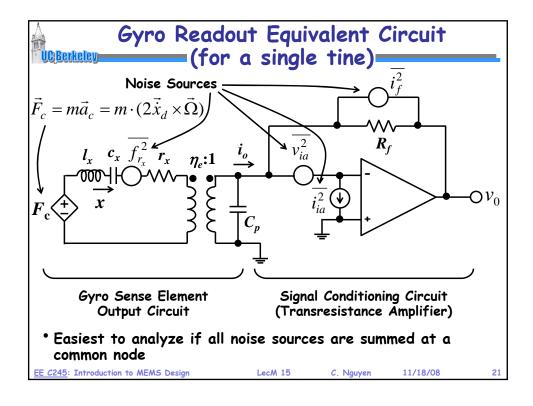


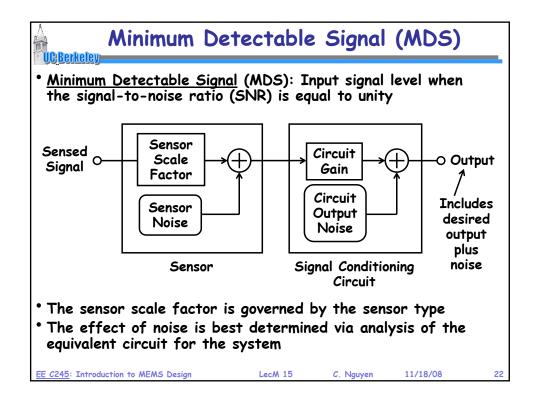
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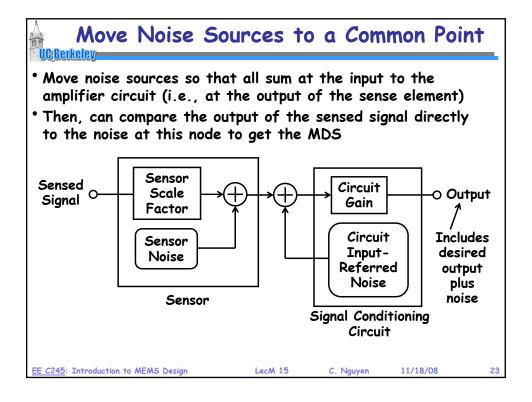
Drive Axis Equivalent Circuit UC Berkeley 180° $1:\eta_e$ η_e :1 \sim Drive -Voltage 180° Signal Drive compare Oscillation Sustaining VGA **Amplifier Digital PLL** Generates drive displacement To Sense Amplifier velocity x_d to which the Coriolis (for synchronization) force is proportional C245: Introduction to MEMS Design 11/18/08

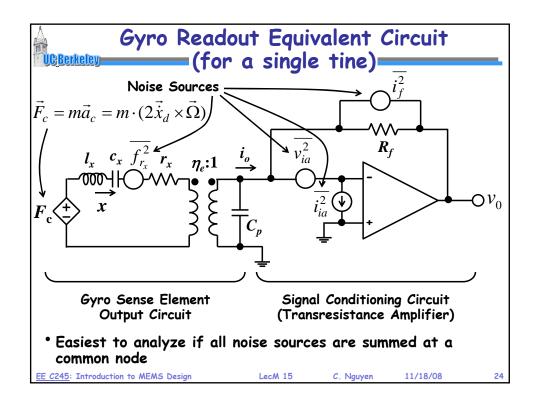


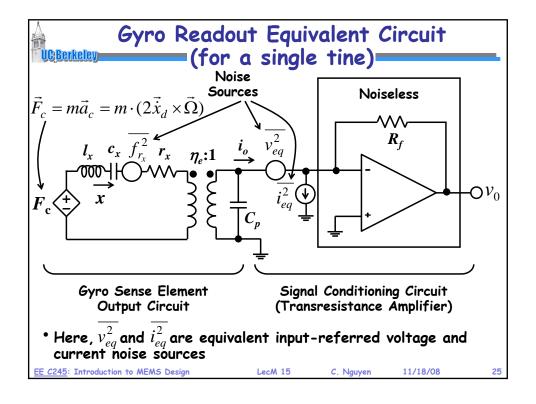
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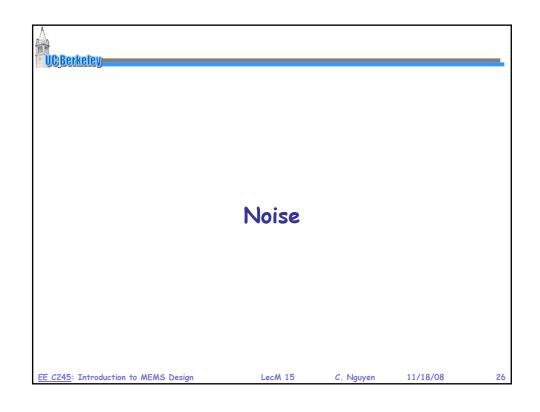


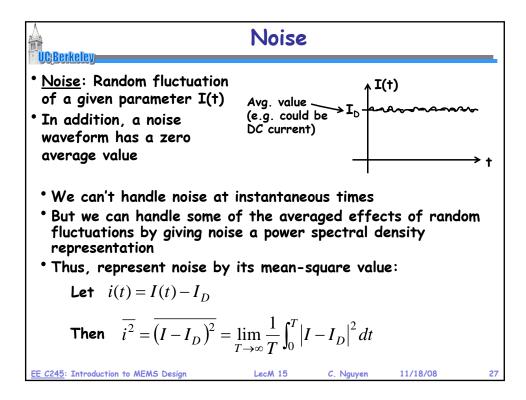


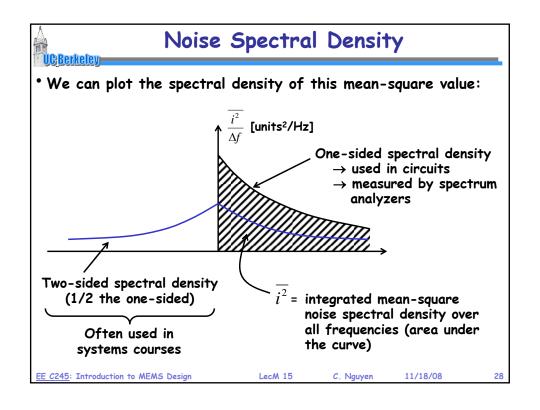


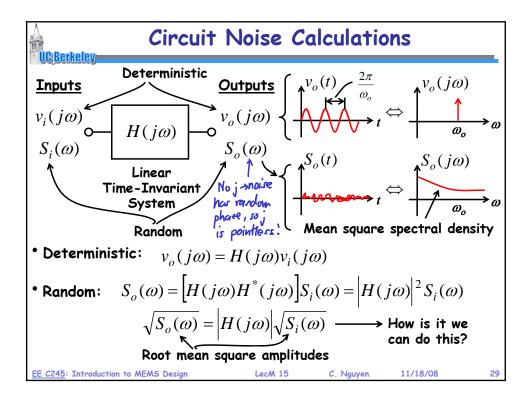


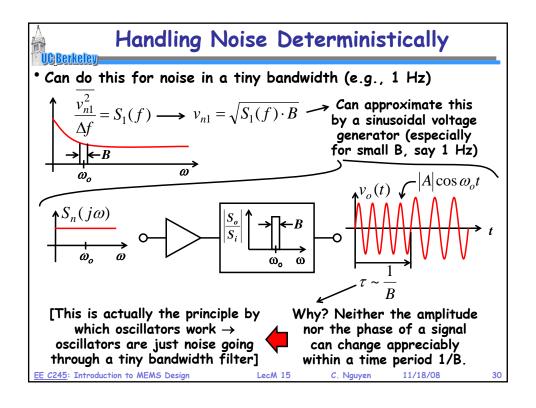


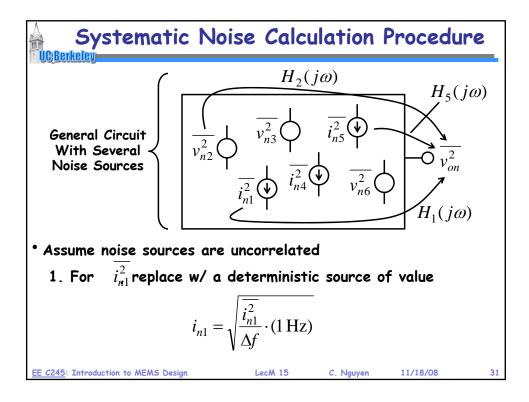


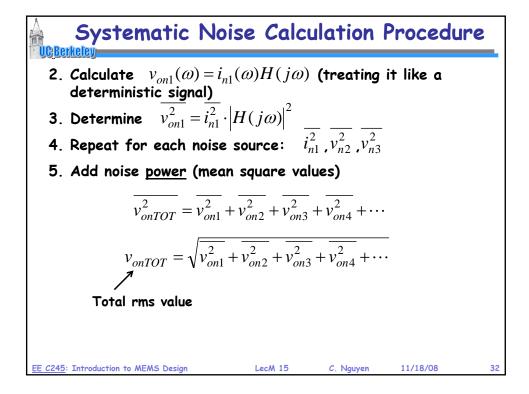


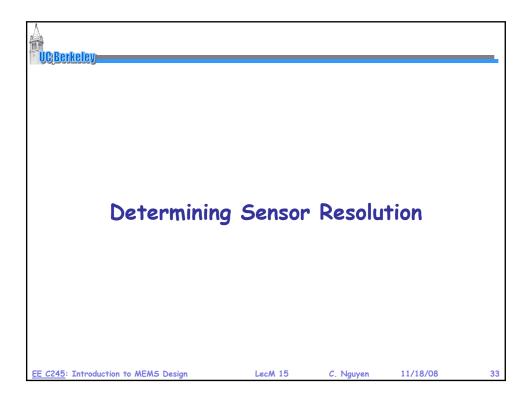


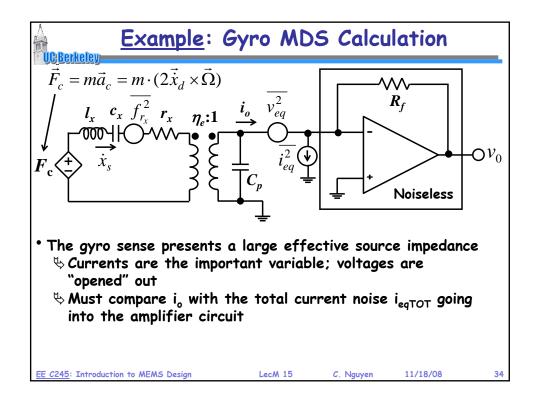


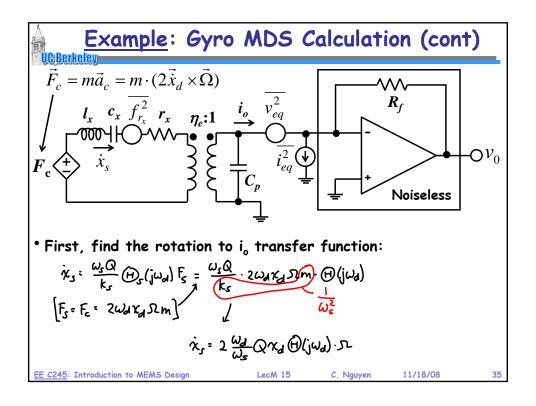


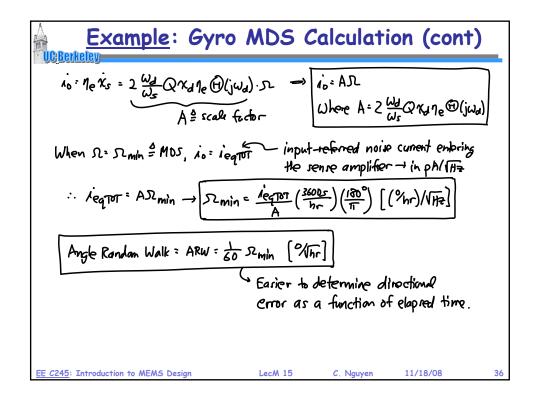


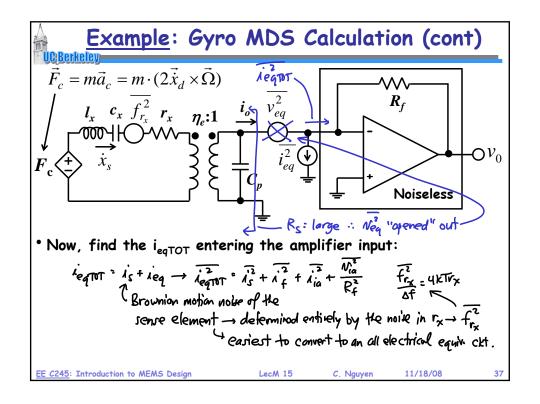


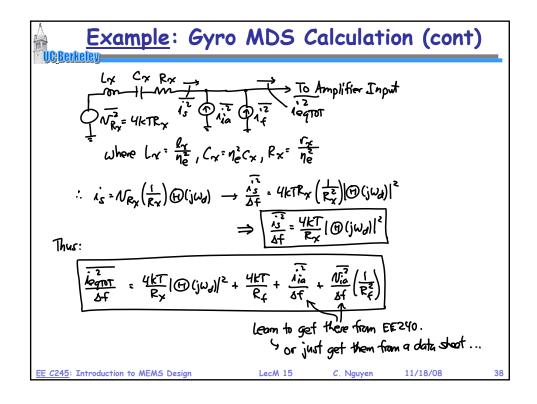


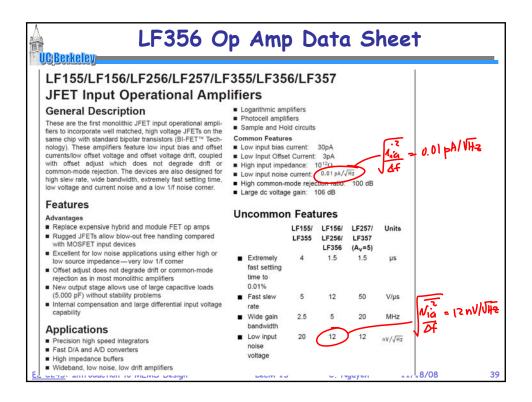


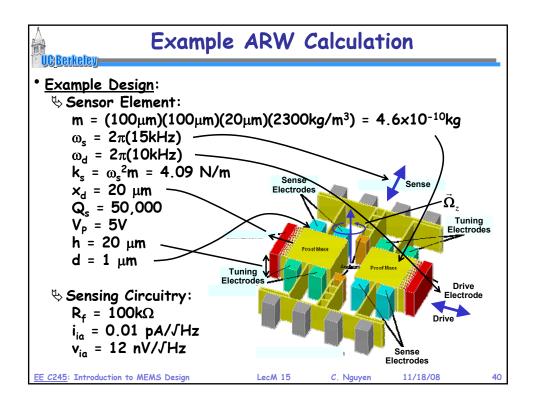












Example ARW Calculation (cont)

Get rotation rate to output current scale factor:

$$A = 2 \frac{\omega_d}{\omega_s} \frac{Q_s K_d \eta_e^{\left(\overrightarrow{D}(j\omega_d)\right)}}{Q_s K_d \eta_e^{\left(\overrightarrow{D}(j\omega_d)\right)}} = 2 \frac{(OK)}{(ISK)} (SOK) (20\mu)(S)(25000E_0)(0.000024) = 2.83 \times 10^{-12} C$$

$$\left(\frac{O(j\omega_d)}{\omega_s} = \frac{(j\omega_d)(\omega_s/O_s)}{-\omega_d^2 + j\omega_d\omega_s} + \omega_s^2 = \frac{j(10K)(15K)/(SOK)}{(ISK)^2 + j(0K)(ISK)} = \frac{j(3K)}{I.25 \times 10^{-6} + j(3K)} \right)$$

$$\Rightarrow \left(\frac{\partial C}{\partial x} = \frac{C_0}{d} = \frac{E_0 hW_p}{d} = \frac{E_0(20\mu)(100\mu)}{(I\mu)^2} = 2000E_0 \rightarrow \eta_e = V_p \frac{Q_s}{\partial x} = \frac{S}{2} (2000E_0) \right)$$

$$\Rightarrow \frac{\partial C}{\partial x} = \frac{C_0}{d} = \frac{E_0 hW_p}{d} = \frac{E_0(20\mu)(100\mu)}{(I\mu)^2} = 2000E_0 \rightarrow \eta_e = V_p \frac{Q_s}{\partial x} = \frac{S}{2} (2000E_0)$$

Assume electrode covers $R_s = \frac{S}{2} S \times 10^{-12} F/m$

Then, get noise:

$$\frac{1}{\log^2 1} = \frac{Q_s \times 1}{R_s} |F(1j\omega_d)|^2 + \frac{Q_s \times 1}{R_s} + \frac{A_{10}}{A_s} + \frac{A_{10}}{A_s} \left(\frac{1}{R_s^2}\right)$$

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Example ARW Calculation (cont)

$$\begin{bmatrix}
R_{Y} = \frac{\omega_{SM}}{Q_{S}^{1}} = \frac{2\pi\Gamma(15K)(46X10^{-10})}{(50K)(8.85\%10^{-2})^{2}} = 110.6 \, \text{k} \, \text{IL}
\end{bmatrix}$$

$$\frac{1.2}{464107} = \frac{(1.66\times10^{-20})}{(110.6K)} (0.000024)^{2} + \frac{(1.66\times10^{-20})}{1M} + \frac{(0.01)^{2}}{(10.06K)} + \frac{(12)^{2}}{(1M)^{2}}$$

$$\frac{1.66\times10^{-26}}{1M} + \frac{(1.66\times10^{-20})}{(110.6K)} + \frac{(12)^{2}}{(1M)^{2}}$$

$$\frac{1.66\times10^{-26}}{1M} + \frac{(1.66\times10^{-20})^{2}}{(1M)^{2}} + \frac{(1.20)^{2}}{(1M)^{2}}$$

$$\frac{1.47\times10^{-28}}{10} + \frac{1.47\times10^{-28}}{10} + \frac{1.47\times10^{-28}}{10}$$

$$\frac{1.47\times10^{-28}}{10} + \frac{1.47\times10^{-28}}{10} + \frac{1.47\times10^{-28}}{10}$$

$$\frac{1.47\times10^{-28}}{10} + \frac{1.47\times10^{-28}}{10}$$

$$\frac{1.47\times10^{-28}}{10$$

What if
$$\omega_{d} = \omega_{s}$$
?

If $\omega_{d} = \omega_{s} = 15KH^{2}$, then $|\mathbb{D}[j\omega_{d}]| = 1$ and

$$A = 2\frac{\omega_{d}}{\omega_{s}}Q_{s}K_{d}\eta_{e}|\mathbb{D}(j\omega_{d})| = 2Q_{s}K_{d}\eta_{e} = 2(50K)(20\mu)(5)(200066) = 1.77X10^{-7}C$$

Aegist = $\frac{(1.66\times10^{-20})}{(110.6K)}(1)^{2} + \frac{(1.66\times10^{-20})}{1M} + \frac{(0.61)^{2}}{(1M)^{2}} + \frac{(12\pi)^{2}}{(1M)^{2}}$

Now, the sensor element dominates!

$$\frac{1}{\sqrt{4}}\frac{1}{\sqrt{4}} = 1.67\times10^{-25}A^{2}/H_{2} \rightarrow 1.67\times10^{-25}$$