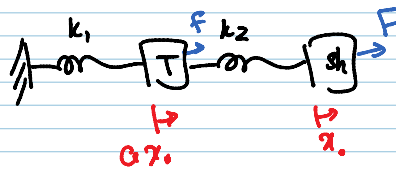
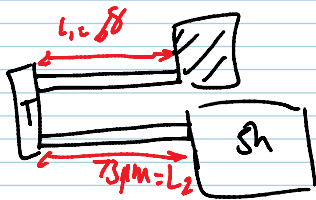


$$M_{eff} = \int_0^L (\dots)^2 dx$$



$$k = k_1 || k_2$$

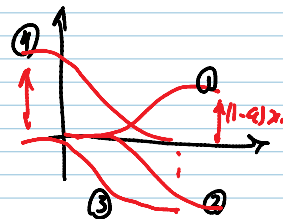
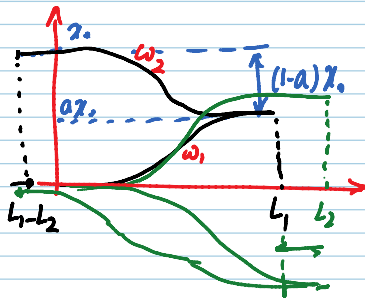
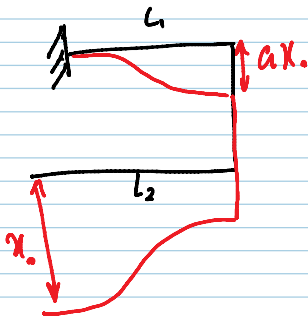
$$a = \frac{k_2}{k_1 + k_2}$$

$$\left(\frac{1}{2}\right)^2 M_T$$

$$\downarrow$$

$$a^2 M_T$$

$$F = \alpha \cdot (k_1 || k_2) = \alpha x_0 \cdot k_1 \rightarrow a = \frac{k_2}{k_1 + k_2}$$



$$w(x) = \delta \left[3(x/L_2)^2 - 2(x/L_2)^3 \right]$$

$$w_1(x) = a x_0 \left[3 \left(\frac{x}{L_1} \right)^2 - 2 \left(\frac{x}{L_1} \right) \right] \leftarrow \frac{x}{L_1} = t$$

$$w_2(x) = x_0 - (1-a)x_0 \left[3 \left(\frac{x-L_1}{L_2} \right)^2 - 2 \left(\frac{x-L_1}{L_2} \right) \right]$$

$$\left(\frac{x - (L_1 - L_2)}{L_2} = z \right)$$

$$m_{\text{eff}, L_1} = \frac{\int_0^{L_1} w_1^2(x) dx / L_1}{x_0^2} \quad m_1 = \frac{\int_0^1 (a x_0 (3t^2 - 2t))^2 dt}{x_0^2} \quad (m_1) = \left[a^2 \frac{13}{35} \right] m_1$$

$$m_{\text{eff}, L_2} = \frac{\int_{L_1-L_2}^{L_1} w_2^2(x) dx / L_2}{x_0^2} \quad m_2 = \frac{\int_0^1 [x_0 - (1-a)x_0 (3z^2 - 2z)]^2 dz}{x_0^2} \quad (m_2) = \left[a + \frac{13}{35} (1-a)^2 \right] m_2$$

$$m_{\text{eff}, L_1} = \left[a^2 \frac{13}{35} \right] m_1$$

$$m_{\text{eff}, L_2} = \left[a + \frac{13}{35} (1-a)^2 \right] m_2$$

$$a = \frac{k_2}{k_1 + k_2}$$

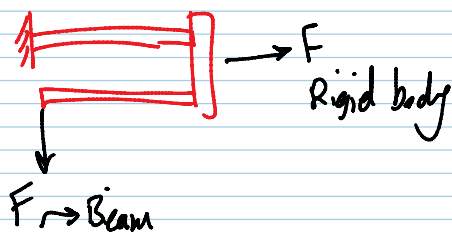
$$m_{\text{eff}, \text{Trans}} = a^2 m_T$$

$$\text{if } k_1 = k_2, a = \frac{1}{2} \text{ and } m_{\text{eff}, L_1} = \frac{13}{140} m_1$$

$$m_{\text{eff}, L_2} = \frac{83}{140} m_2$$

$$m_{\text{eff}, T} = \frac{1}{4} m_T$$

as we derived before.



all the fingers 41 μm long

overlap 35 μm

overlap 35 μm

$$k_e = \frac{1}{2} V_p^2 \frac{d^2 C}{dx^2}$$

Part 3 $V_{n,s} = V_{tunc}$ $V_p = 0$

Part 4 $\left\{ \begin{array}{l} V_{tunc} = 100V \\ V_{mos} = 20V \end{array} \right.$ $k_e = \frac{1}{2} (60-20)^2 \frac{d^2 C}{dx^2}$

effective mass
 ↓
 effective spring
 $\left\{ \begin{array}{l} m_x, k_x \\ m_y, k_y \end{array} \right.$

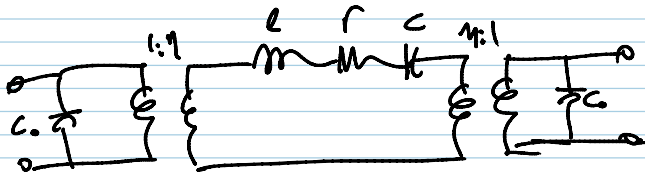
after Electrical stiffness

$$C_{eq,x} = \frac{M_x \omega_x}{C_{ex}} = \frac{1}{k_x \omega_x \omega_x} \quad k_x = k_m - k_e$$

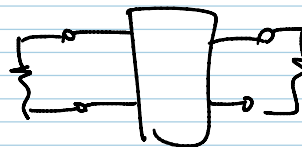
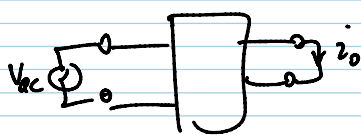
$$C_{eq,y} =$$

$$m_x = V_p \frac{dC}{dx}$$

$$m_y = V_p \frac{dC}{dy}$$



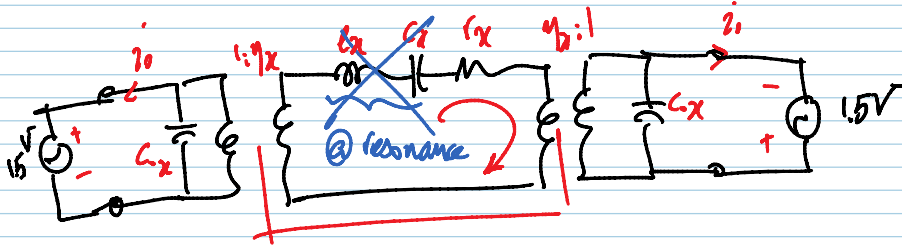
$f_x = M_x$
 $\underline{V_x = C_{eq,x}}$
 $\underline{C_x = \frac{1}{k_x}}$ ← $\underline{k_x = k_m - k_e}$



SP analysis

S1 S2

Part 7)



eg. mass in sense mode

$$F = 2 * \dot{x}_d * M_s * \Omega$$

velocity drive mode

