## PROBLEM SET \#6

Issued: Tuesday, Oct. 30, 2012
Due (at 7 p.m.): Tuesday Nov. 20, 2012, in the EE C245 HW box near 125 Cory.

Figures PS6.1-6 show a dual-axis $x-y$ accelerometer manufactured via the following 3-mask surface micromachining process:
i) Deposit $1.0 \mu \mathrm{~m}$ of $\mathrm{SiO}_{2}$ on a Silicon wafer
ii) Deposit 300 nm of $\mathrm{SiN}_{3}$ via LPCVD
iii) Deposit 200 nm of in-situ doped polysilicon
iv) Lithographically define and etch polysilicon interconnects (anisotropic)
v) Deposit $2.0 \mu \mathrm{~m}$ of $\mathrm{SiO}_{2}$ (LTO)
vi) Lithographically define and then etch anchor openings in $\mathrm{SiO}_{2}$ (anisotropic)
vii) Deposit $3.0 \mu \mathrm{~m}$ of in-situ doped polysilicon
viii) Lithographically define and then etch the polysilicon structure (anisotropic)
ix) Etch $\mathrm{SiO}_{2}$ completely using an HF etch, releasing structure (isotropic)

Assume all materials are stress-free at room temperature and have the material properties listed in Table PS6.1.

Table PS6.1

| Material | $\rho_{m}$ <br> $\mathrm{~kg} / \mathrm{m}^{3}$ | $E$ <br> GPa | $v$ | $\alpha_{T}$ <br> $\mu \mathrm{strain} / \mathrm{K}$ | $\sigma_{0}$ <br> MPa | Comment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polysilicon | 2300 | 150 | 0.2 | 2.8 | Varies | Random Grains |
| Silicon Dioxide | 2200 | 69 | 0.17 | 0.7 | -300 | Amorphous |
| Silicon Nitride | 3170 | 270 | 0.27 | 2.3 | 1100 | Stoichiometric |



Figure PS6.1 - Perspective view of the accelerometer.


Figure PS6.2 - Top view of the accelerometer.


Figure PS6.3 - Top view of accelerometer showing only the interconnect layer.


Figure PS6.4-Zoom-in view of the $x$-direction interdigital comb finger structure. There are 71 fingers on each side of the proof mass.


Figure PS6.5 - Top view showing the $\boldsymbol{y}$-direction capacitor structure.


Figure PS6.6 - Zoom-in view of the $\boldsymbol{y}$-direction capacitor structure.

1. Calculate the $x$ - and $y$-directed resonance frequencies of the accelerometer structure with no applied DC bias, making simplifying assumptions as necessary. Do NOT neglect the beam masses in these calculations. Assuming a quality-factor $Q$ of 5 in both directions, draw the frequency response for the accelerometer in both the $x$ - and $y$-directions.
2. Derive an expression for the capacitance between port $A$ and $B$ shown in Figure PS6.7 as a function of displacement $x$ using a parallel-plate approximation. Also, calculate the overlap capacitance between these two ports at rest.
3. Derive an expression for the capacitance between port $A$ and $C$ shown in Figure PS6.7 as a function of displacement $y$ using a parallel-plate approximation. Also calculate the overlap capacitance between these two ports at rest.
4. Suppose the accelerometer is now hooked up as shown in Figure PS6.7, with a DC bias $V_{\text {bias }}$ of 10 V applied to the structure.
(a) Calculate the new $x$ - and $y$-directed resonance frequencies with this DC bias.
(b) If a sinusoidal force signal is applied to the structure in the $x$-direction with a magnitude of 1 g , what will be the magnitude and phase of the resulting output current $i_{B}$ as a function of frequency?
(c) If a sinusoidal force signal is applied to the structure in the $y$-direction with a magnitude of 1 g , what will be the magnitude and phase of the resulting output current $i_{C}$ as a function of frequency?


Figure PS6.7-Top view of the accelerometer with circuit connections for problem 4.

