## EE40 Spring 2008 Homework 2 Problem 9 Solution

9) [Hambley 2.72 modified]

The graph of the circuit is:


We choose the tree (this is not unique):


This gives three loops, each with its associated mesh current


Note that $\mathrm{i}_{3}=-4$ is not a variable.
Writing KVL for the first mesh,
Writing KVL for the second mesh:

$$
\begin{aligned}
& 15 i_{1}+15\left(i_{1}-i_{2}\right)+15\left(i_{11}-i_{2}-i_{3}\right)=0 \\
& 5\left(i_{2}+i_{3}\right)+15\left(i_{2}+i_{3}-i_{1}\right)+15\left(i_{2}-i_{1}\right)+25 i_{2}=0
\end{aligned}
$$

Substituting for i3 and rearranging

$$
\begin{aligned}
45 \mathrm{i}_{1}-30 \mathrm{i}_{2} & =-60 \\
-30 \mathrm{i}_{1}+60 \mathrm{i}_{2} & =80
\end{aligned}
$$

Adding 2*eq1+eq2 gives

$$
60 i_{1}=-40
$$

Hence

$$
\mathrm{i}_{1}=-2 / 3 \mathrm{~A}
$$

Substituting into either equation gives

$$
\mathrm{i}_{2}=1 \mathrm{~A} .
$$

We get $v_{3}=25 \mathrm{i}_{2}=25 \mathrm{~V}$.

