Table 0.2 Rules of boolean algebra. The two entries in the last row are used frequently and are known as DeMorgan's theorem.

| AND Rules | OR Rules |
| ---: | ---: |
| $A \cdot A=A$ | $A+A=A$ |
| $A \cdot \bar{A}=0$ | $A+\bar{A}=1$ |
| $0 \cdot A=0$ | $0+A=A$ |
| $1 \cdot A=A$ | $1+A=1$ |
| $A \cdot B=B \cdot A$ | $A+B=B+A$ |
| $A(B C)=(A B) C$ | $A+(B+C)=(A+B)+C$ |
| $A(B+C)=A B+A C$ | $A+B C=(A+B)(A+$ |
| $\bar{A} \cdot \bar{B}=\overline{A+B}$ | $\bar{A}+\bar{B}=\bar{A} \cdot B$ |

Example 0.1 Using these rules we can take a number of steps to successively simplify the expression as follows:

$$
\begin{gathered}
F=\overline{\mathbf{A}} \mathbf{B} \overline{\mathbf{C}}+\overline{\mathbf{A}} \mathbf{B C}+\mathbf{A} \bar{B} \mathbf{C}+\mathbf{A B C} \\
F=(\overline{\mathbf{A}} \mathbf{B} \overline{\mathbf{C}}+\overline{\mathbf{A}} \mathbf{B C})+(\mathbf{A} \bar{B} \mathbf{C}+\mathbf{A B C}) \\
F=\overline{\mathbf{A}} \mathbf{B}(\overline{\mathbf{C}}+\mathbf{C})+\mathbf{A C}(\bar{B}+\mathbf{B}) \\
F=\overline{\mathbf{A}} \mathbf{B}(\mathbf{1})+\mathbf{A C}(\mathbf{1})
\end{gathered}
$$

Finally,

$$
F=\overline{\mathbf{A}} \mathbf{B}+\mathbf{A C}
$$

The final expression is clearly simpler than our initial expression.
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