

## Lecture 16: October 24, 2001

### Logic with Complementary State Devices

A) Discovering a Pull-Up Device

B) Designing a Pull-Up Device

C) EE 42 Pull-Up Device Model (42PU)

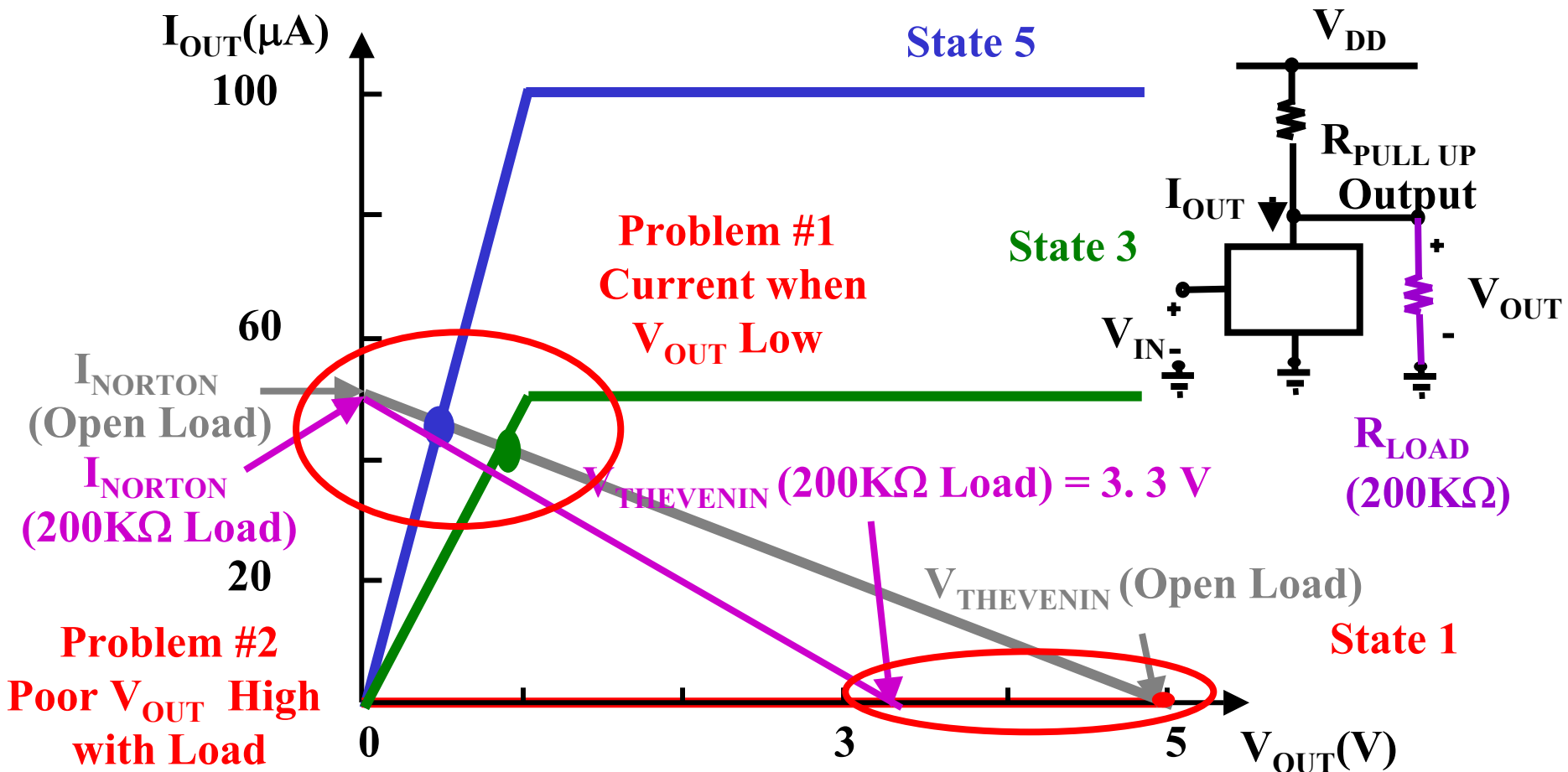
D) Composite  $I_{OUT}$  vs.  $V_{OUT}$

E) Voltage Transfer Function and  $V_M$

### Reading:

Schwarz and Oldham pp. 607-611 (read for graphs and not device equations) and lecture viewgraphs

# Composite Current Plot for the 42PD Circuit with 200kΩ Load to Ground



# Problems and Opportunities in Logic Circuit Design

**Problem #1: Significant wasted current and power when  $V_{OUT}$  is low.**

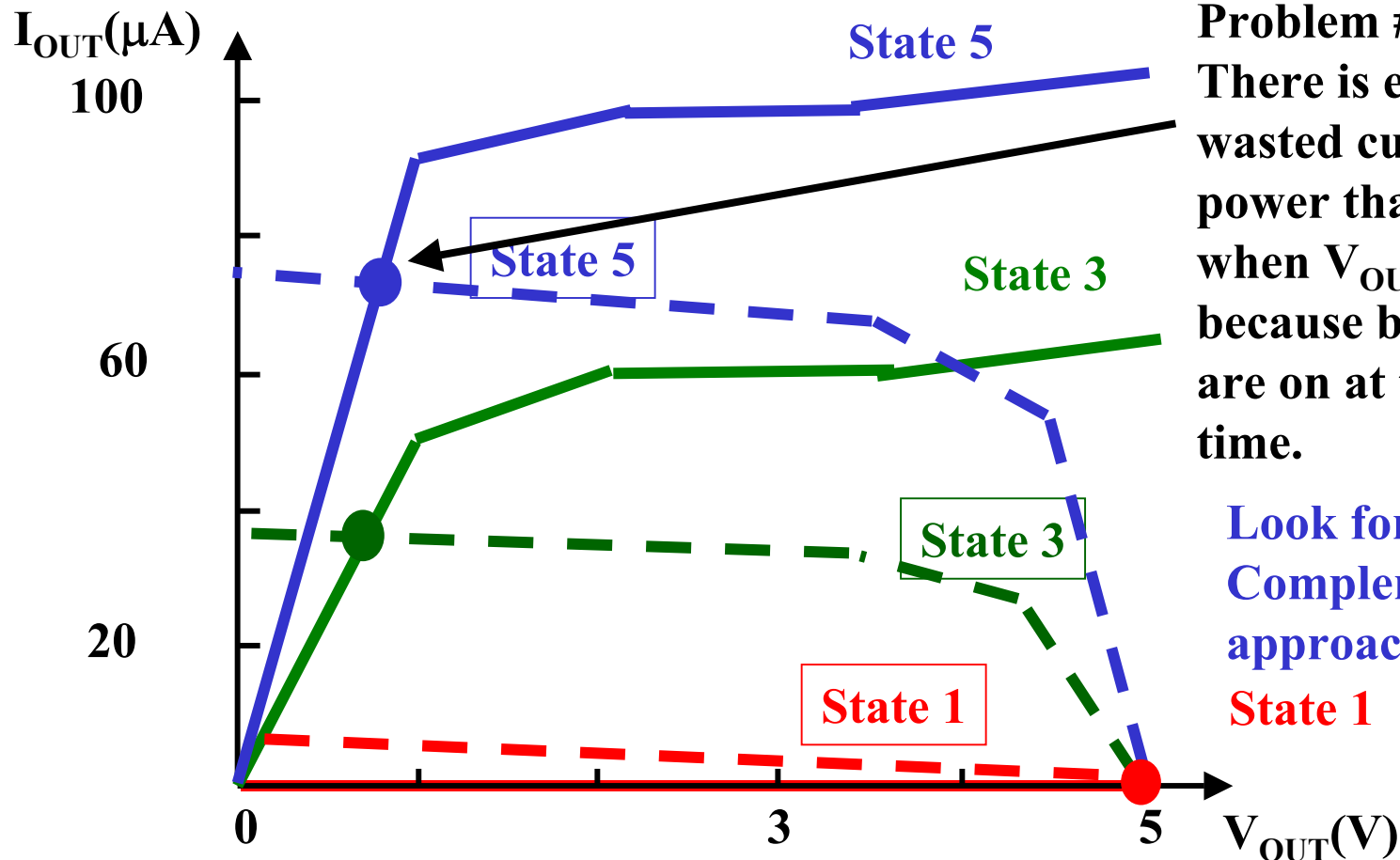
**Problem #2: High value of  $V_{OUT}$  is adversely affected by a load resistor.**

**Missed Opportunity: The value of the input control signal is not used to adjust the state of the pull-up device.**

**What if : If the pull-up device could be a state-dependent device what kind of device would we want?**

# Pull-Up Device Design: Trial 1

Similar pull-up and pull-down states



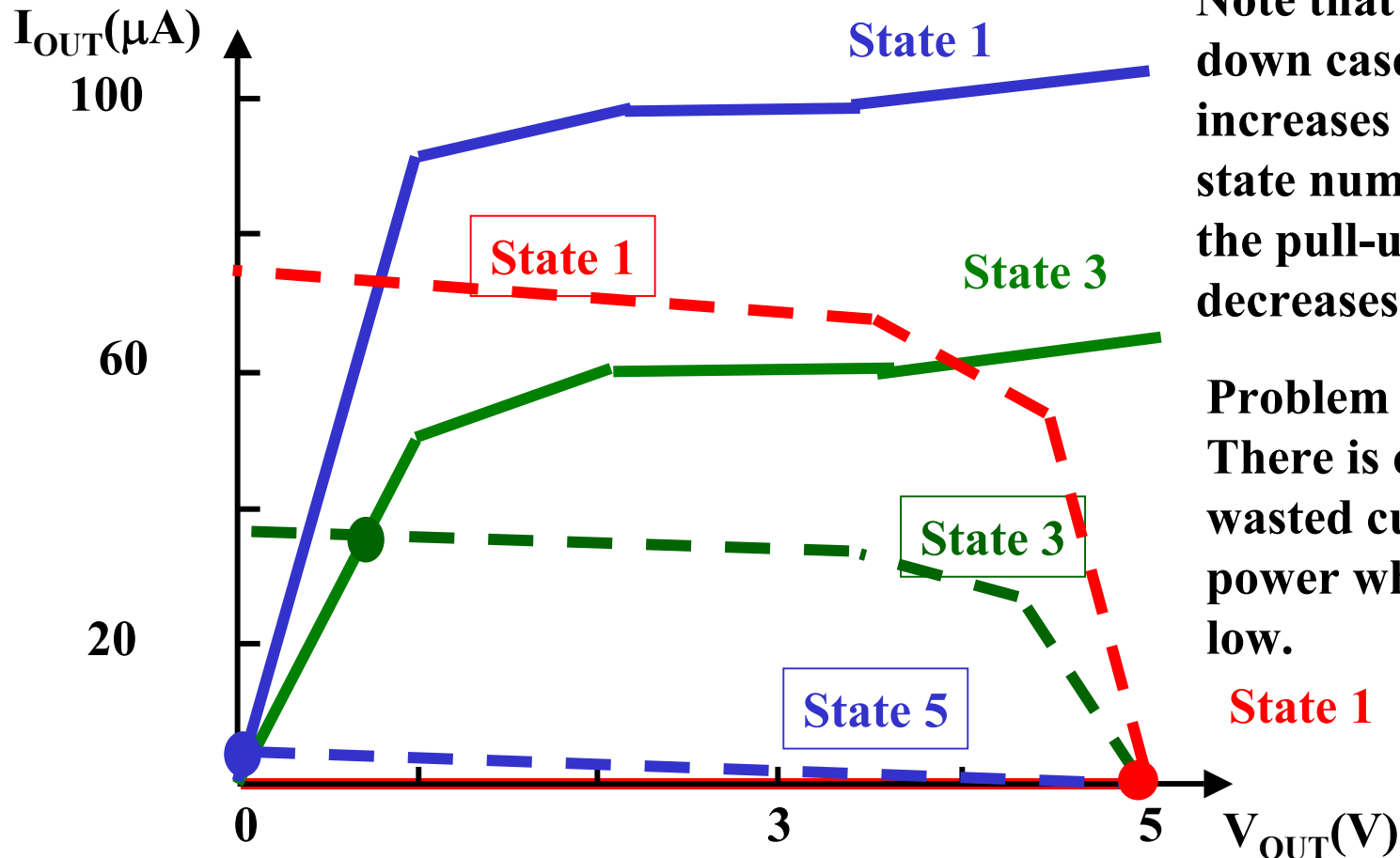
**Problem #1 is worse!**  
 There is even more wasted current and power than before when  $V_{OUT}$  is low because both devices are on at the same time.

**Look for a more Complementary approach.**

**State 1**

# Pull-Up Device Design: Trial 2

Complementary pull-up and pull-down states



Note that in the pull-down case the current increases with the state number and in the pull-up case it decreases.

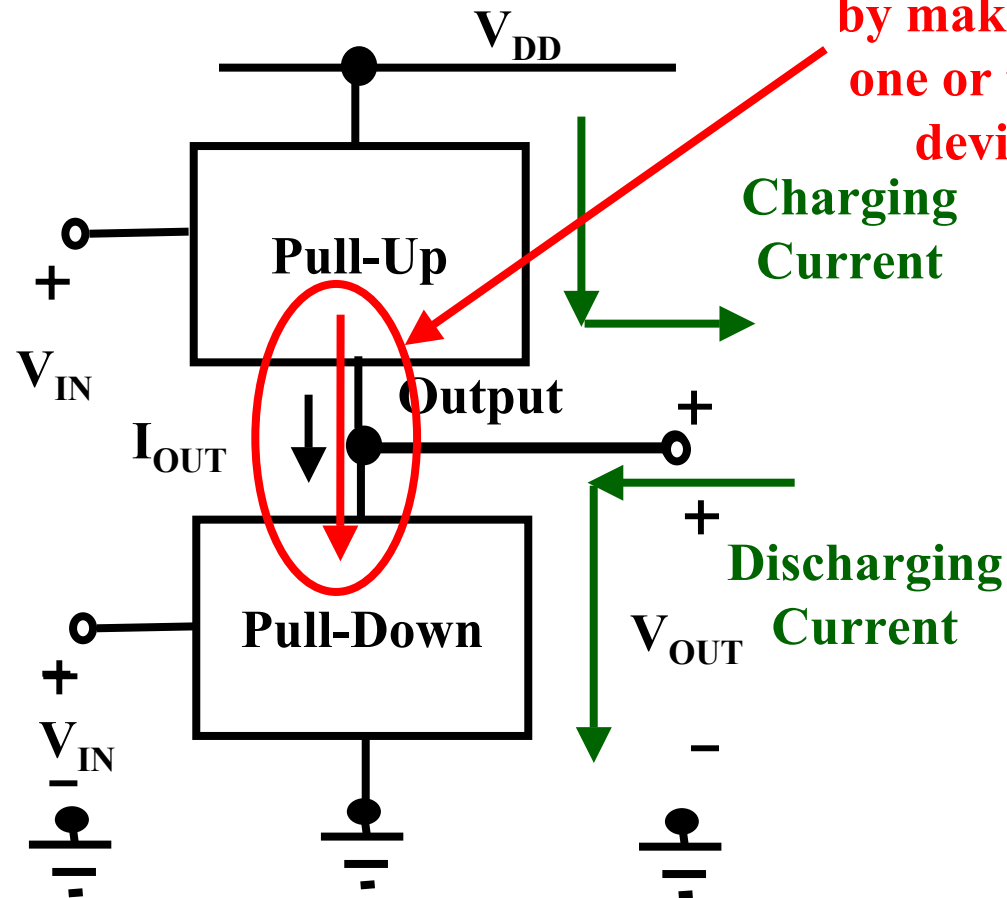
Problem #1 is solved. There is essentially no wasted current or power when  $V_{OUT}$  is low.

State 1

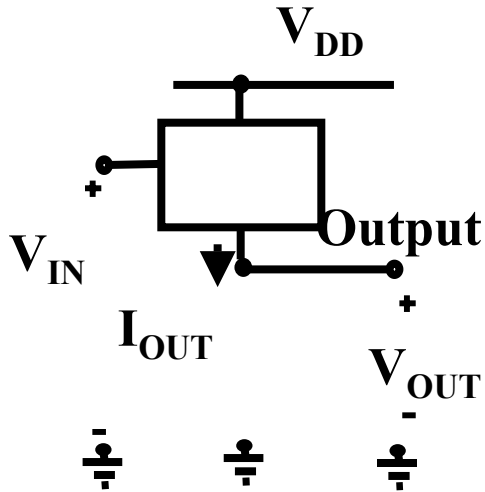
# Pull-Down and Pull-Up Must Complement Rather Than Fight Each Other

**Reduce the Short-Circuit Current by making either one or the other device off.**

Input for State Control Signal  
Share Same Signal  
Input for State Control Signal



# Desirable Complementary Device Characteristics

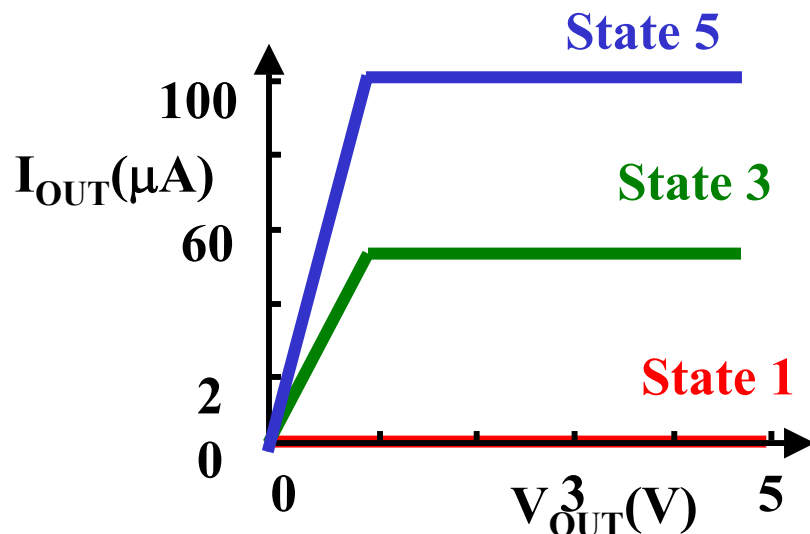


We desire characteristics that are **complementary** for the pull-down and pull-up state-dependent devices.

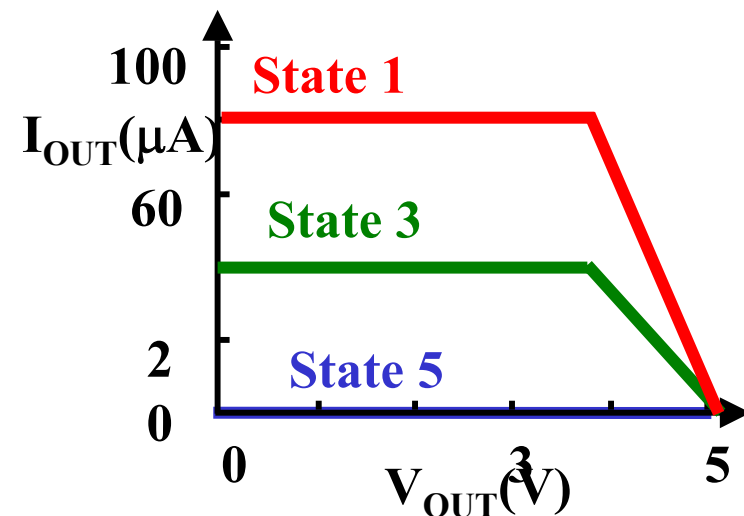
$V_{IN}$	Low	High
Pull-Down Current	Low not leak	High Discharge Output
Pull-Up Current	High Charge Output	Low not leak

# Designing the Complementary Device

**Make This**



**Into This**



The curve sets are very similar but have two key changes.

The creation of current with input State ( $V_{IN}$ ) is reverse ordered (and also shifted).

The dependence on  $V_{OUT}$  is reverse ordered and shifted by  $V_{DD}$



# 42 Pull-Down Device Equations

Describe  $I_{OUT}$  as function of  $V_{IN}$  and  $V_{OUT}$

**Cut-off**       $V_{IN} \leq V_{TD}$

$$I_{OUT-PD} = 0$$

**Linear (with  $V_{OUT}$ )**       $V_{IN} \geq V_{TD}$        $V_{OUT} \leq V_{TD}$

$$I_{OUT-PD} = k_D (V_{IN} - V_{TD}) V_{OUT}$$

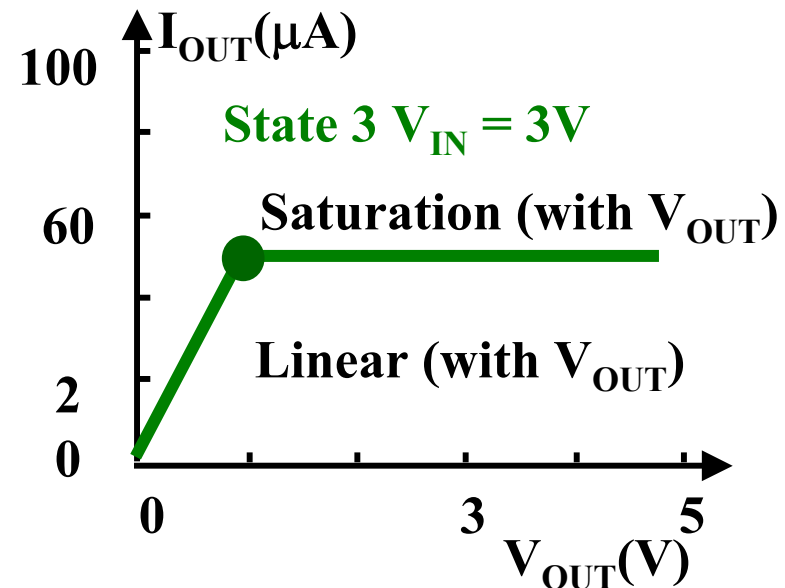
**Saturation (with  $V_{OUT}$ )**       $V_{IN} \geq V_{TD}$        $V_{OUT} \geq V_{TD}$

$$I_{OUT-PD} = k_D (V_{IN} - V_{TD}) V_{TD}$$

# Drawing $I_{OUT}$ as function of $V_{IN}$ and $V_{OUT}$ for the 42Pull-Down Device Equations

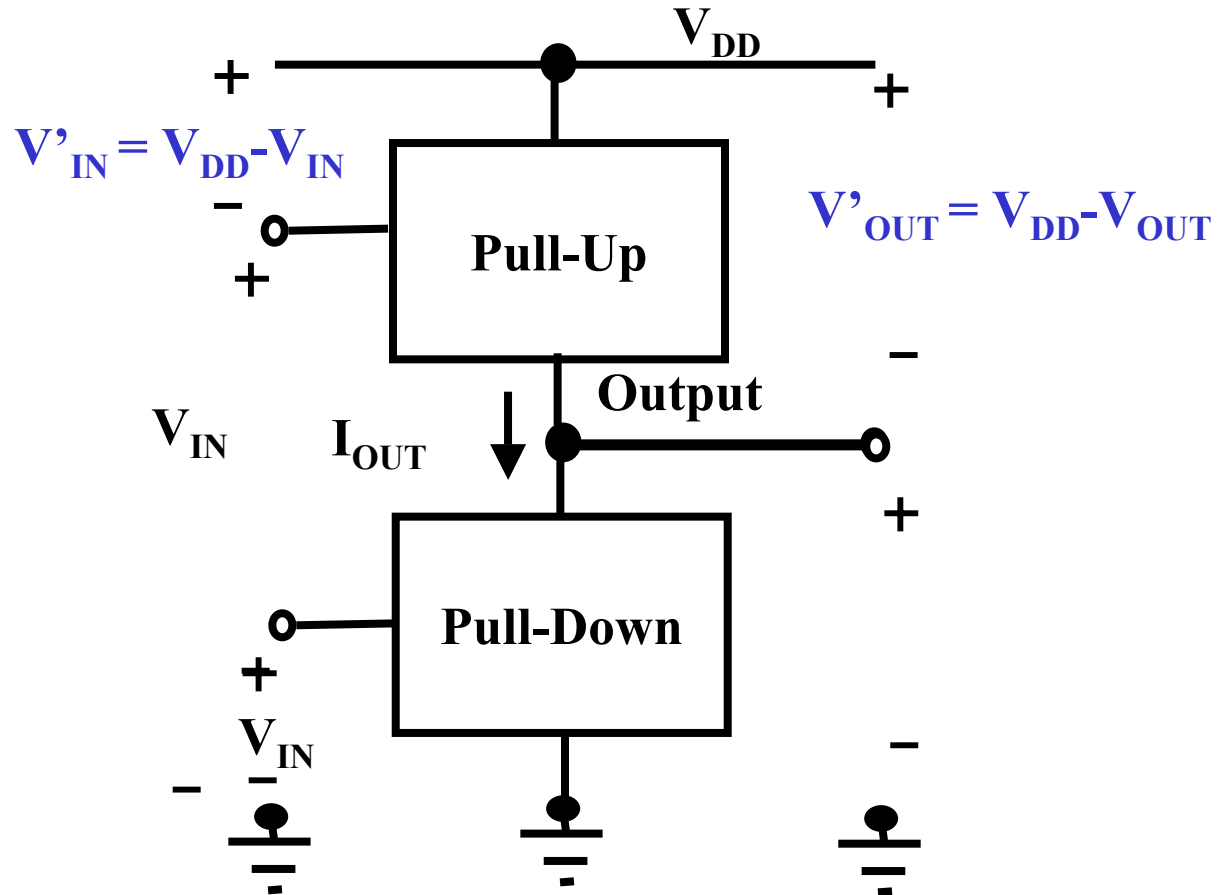
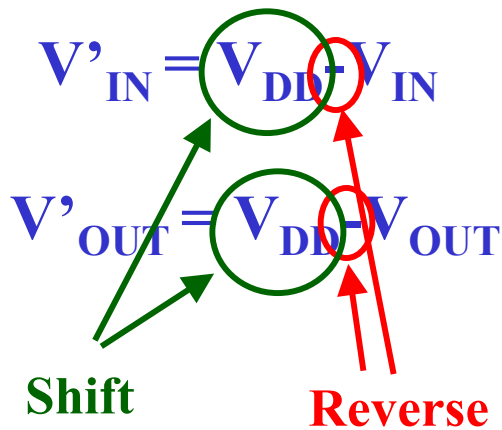
The equations are expressly designed for EE42 to make it very simple to draw  $I_{OUT}$  vs.  $V_{OUT}$

- 1) For  $V_{IN} < V_{TD}$ , the current is zero.
- 2) For  $V_{IN} > V_{TD}$ , first evaluate the current  $I_{OUT}$  at  $V_{OUT} = V_{TD}$  and plot the single point  $(I_{OUT}, V_{OUT})$
- 3) Draw a line from this point to the origin to create the linear region.
- 4) Draw a horizontal line from this point to create the saturation region



# $V_{DD} - V_X$ Gives Complementary Characteristics

Physical Interpretation as device related rather than logic circuit related voltages.



# 42 Pull-Up Device Equations

$I_{OUT}$  as function of  $V_{IN}$  and  $V_{OUT}$  in the Logic Circuit

Based on:  $V_{TU}$  and  $K_U$

**Cut-off**  $V_{DD} - V_{IN} \leq V_{TU}$

$$I_{OUT-PU} = 0$$

**Note:**  $V'_{IN} = V_{DD} - V_{IN}$

$$V'_{OUT} = V_{DD} - V_{OUT}$$

**Linear (with  $V_{OUT}$ )**  $V_{DD} - V_{IN} \geq V_{TU}$        $V_{DD} - V_{OUT} \leq V_{TU}$

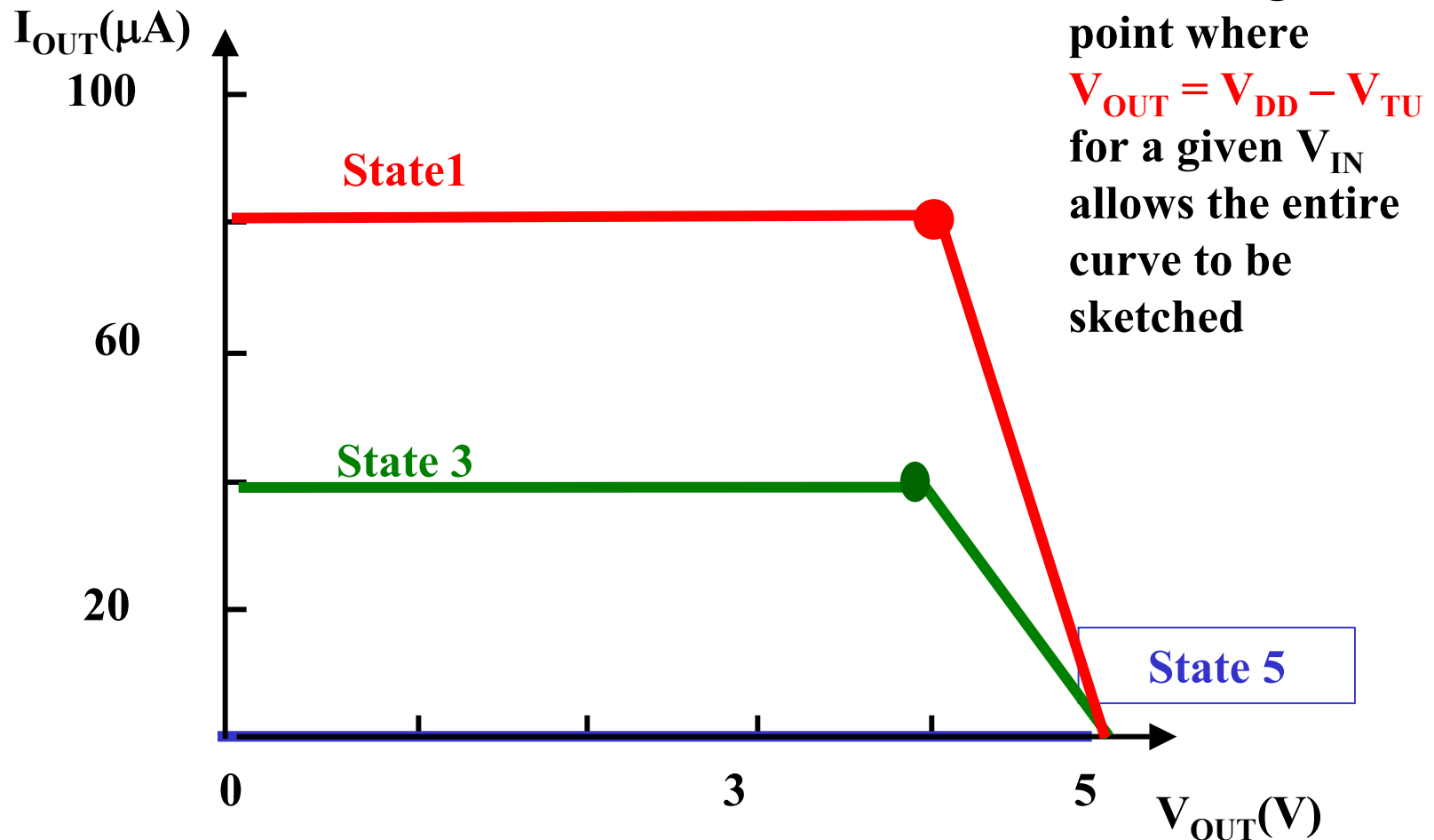
$$I_{OUT-PU} = k_U (V'_{IN} - V_{TU}) V'_{OUT} = k_U (V_{DD} - V_{IN} - V_{TU}) (V_{DD} - V_{OUT})$$

**Saturation (with  $V_{OUT}$ )**  $V_{DD} - V_{IN} \geq V_{TU}$        $V_{DD} - V_{OUT} \geq V_{TU}$

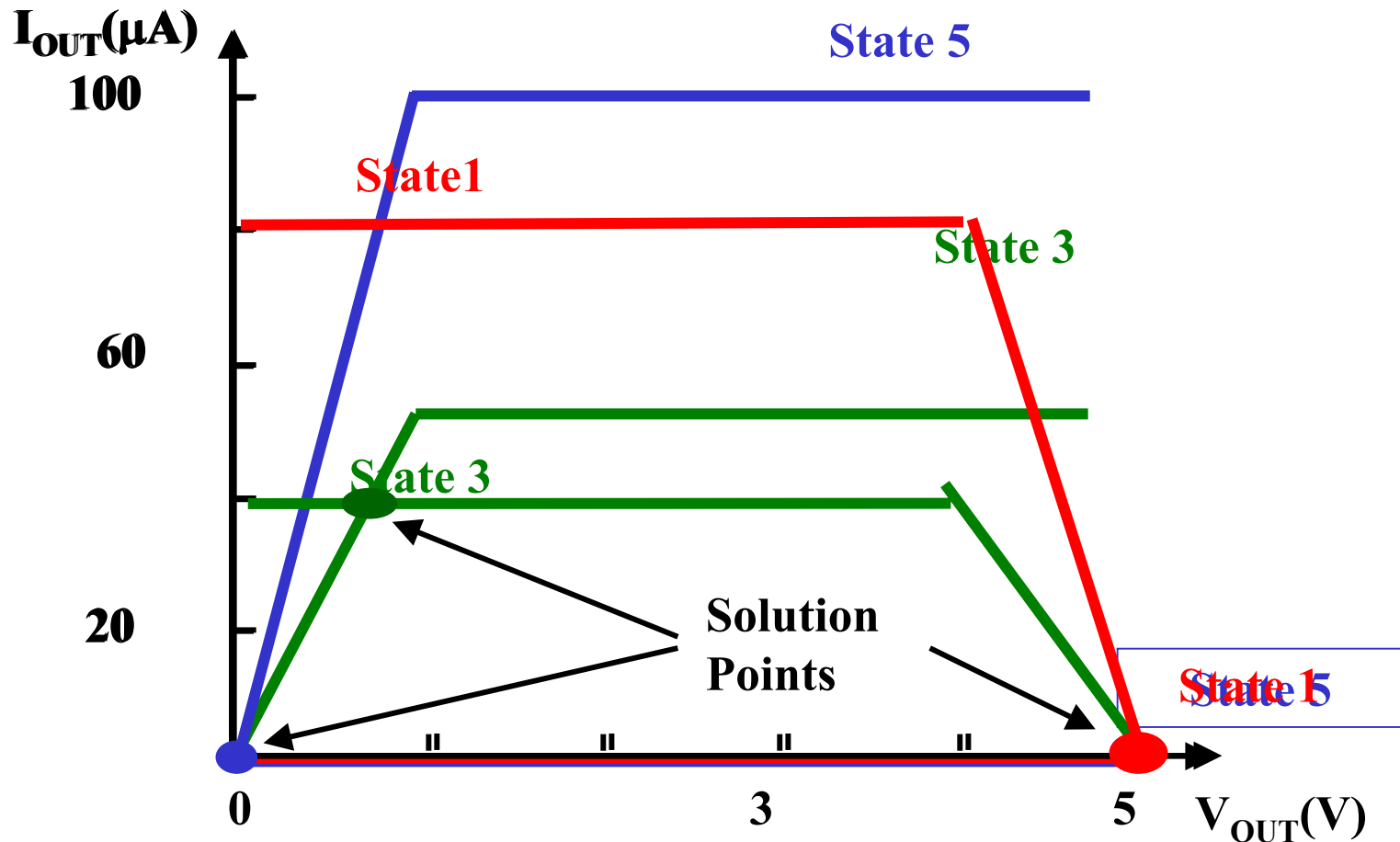
$$I_{OUT-PU} = k_U (V'_{IN} - V_{TU}) V'_{TU} = k_U (V_{DD} - V_{IN} - V_{TU}) V_{TU}$$

# 42Pull-UP Device Model

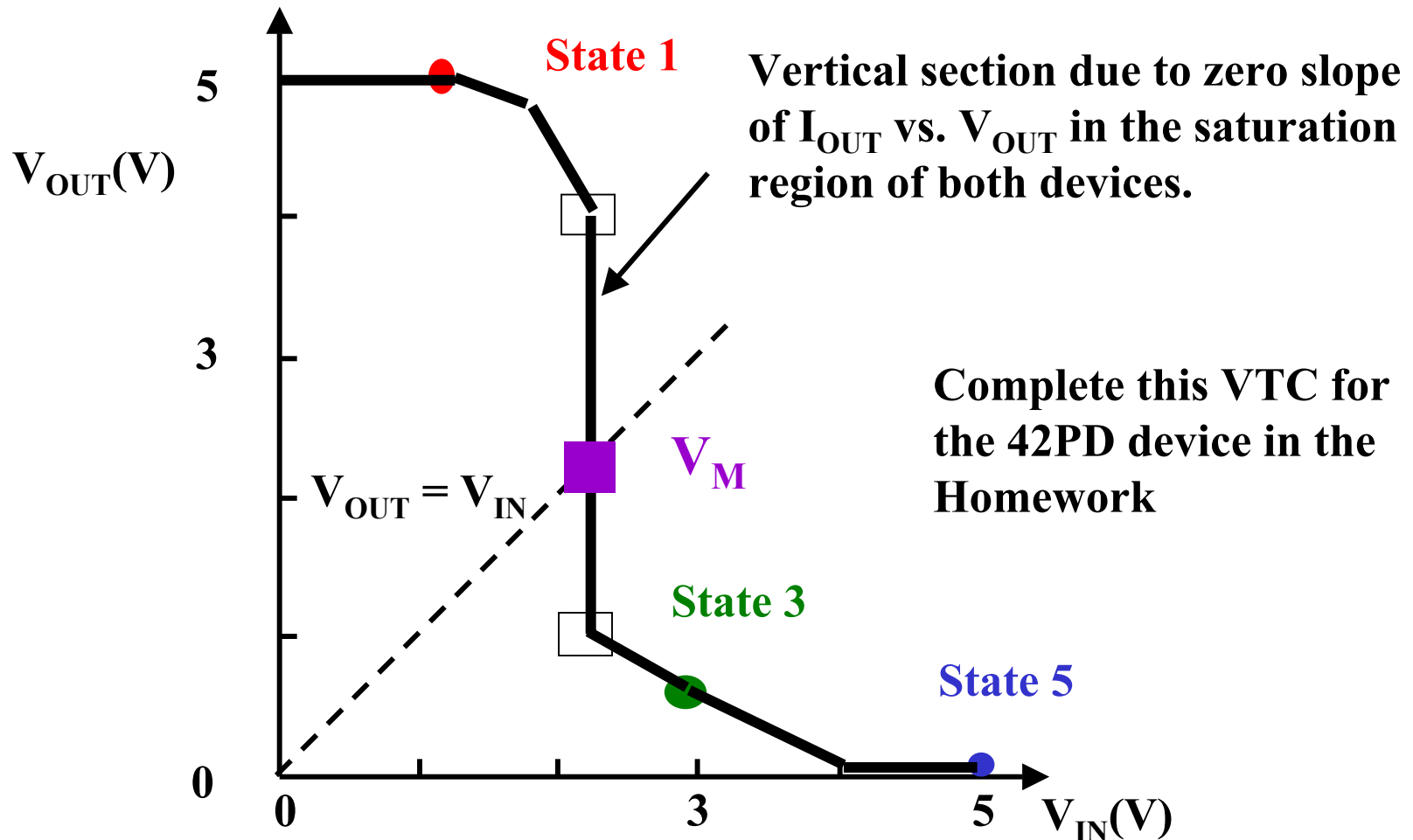
## $I_{OUT}$ vs. $V_{OUT}$



# Composite $I_{OUT}$ vs. $V_{OUT}$ to Find Points That Satisfies Both Devices for Each $V_{IN}$



# Voltage Transfer Function for the Complementary Logic Circuit



# Method for Finding $V_M$

At  $V_M$ ,

1)  $V_{OUT} = V_{IN} = V_M$

2) Both devices are in saturation

3)  $I_{OUT-PD} = I_{OUT-PU}$

$$I_{OUT-PD} = k_D (V_{IN} - V_{TD}) V_{TD} = I_{OUT-PU} = k_U (V_{DD} - V_{IN} - V_{TU}) V_{TU}$$

Substitute  $V_M$

**Solve for  $V_M$**

**Example Result: When  $k_D = k_P$  and  $V_{TD} = V_{TU}$ ,  $V_M = V_{DD}/2$**