

MORE NODAL ANALYSIS

Lecture 10 review:

- Ideal and real instruments
- Series and parallel elements
- Nodal analysis with floating voltage sources

Today:

- Special properties of linear circuits:
 - Thevenin and Norton Equivalents
- Examples

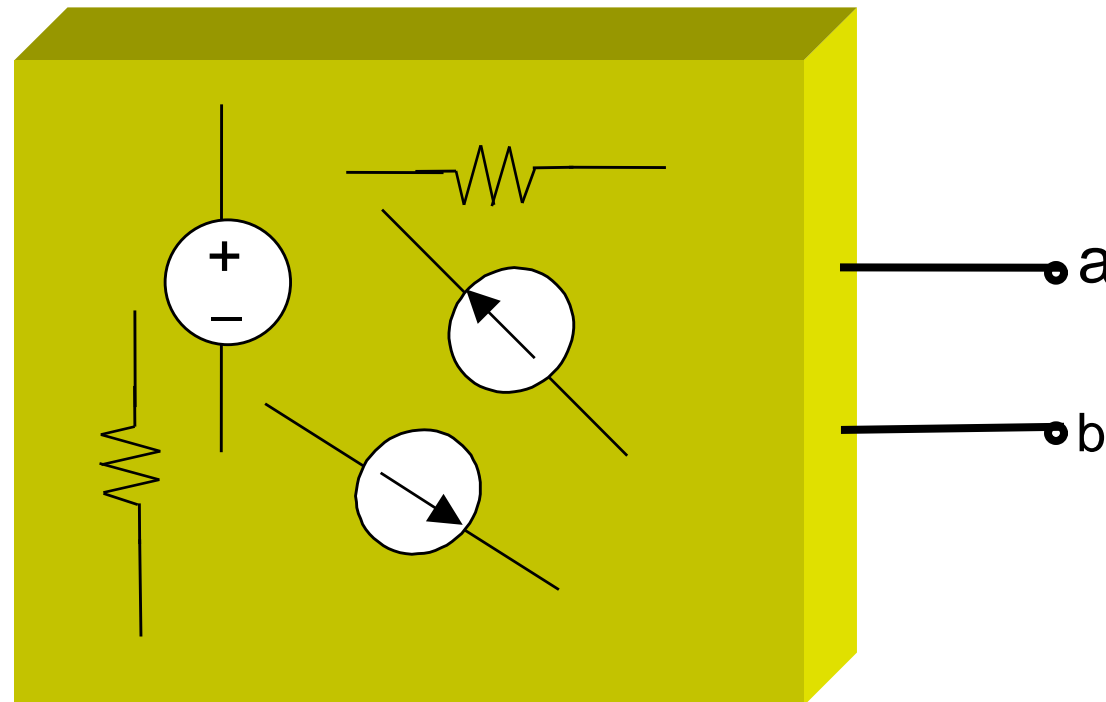
Linear Circuits -Special Properties

- Circuits consisting only of linear elements are linear circuits.
- There are simple “equivalent circuits” for “one-port” linear circuits.

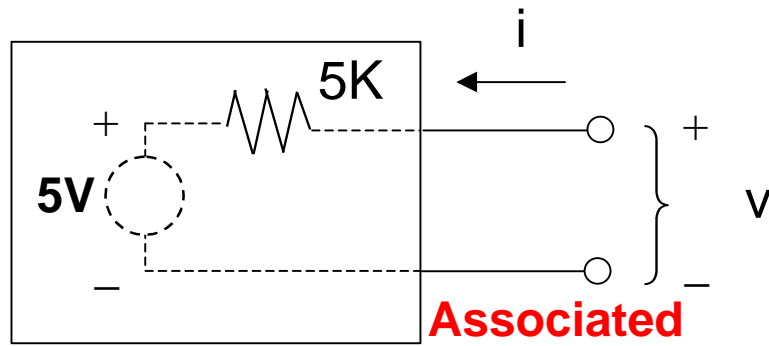
TWO-TERMINAL **LINEAR** RESISTIVE NETWORKS

("One Port" Circuit)

Interconnection of two-terminal linear resistive elements with only two "accessible" terminals



I-V CHARACTERISTICS OF LINEAR TWO-TERMINAL NETWORKS



What is the easy way to find the I-V graph?

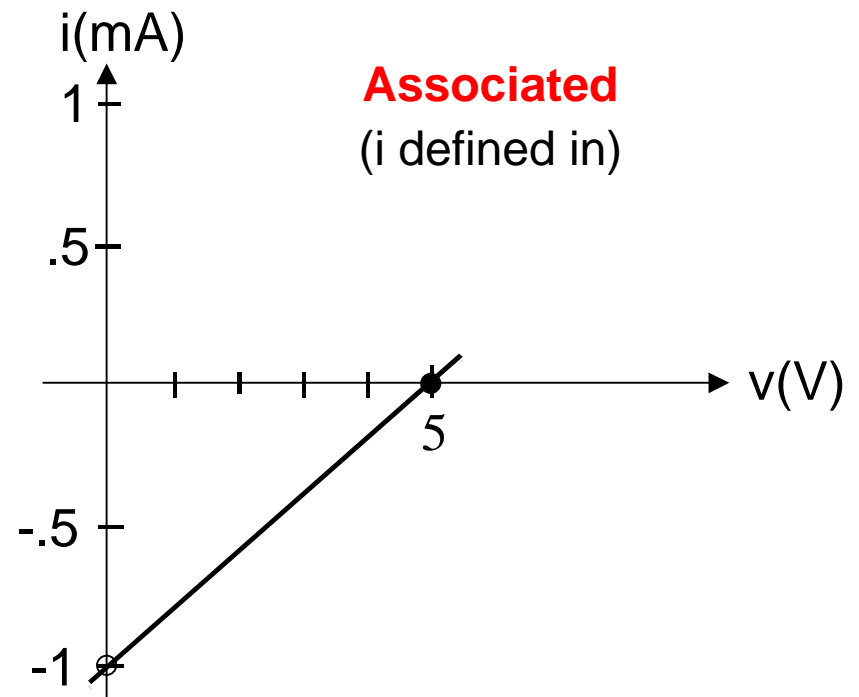
Apply v , measure i ,
or vice versa

First find open-circuit V

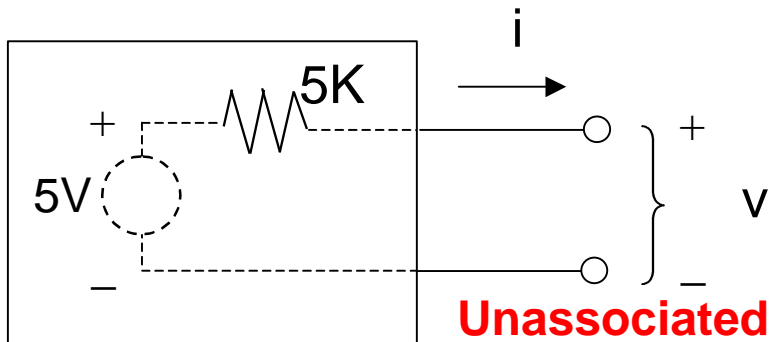
$$v = 5V \text{ if } i = 0$$

Now find Short-circuit I

$$i = -1\text{mA if } v = 0$$



I-V CHARACTERISTICS OF LINEAR TWO-TERMINAL NETWORKS



Lets do same thing but with *unassociated* signs

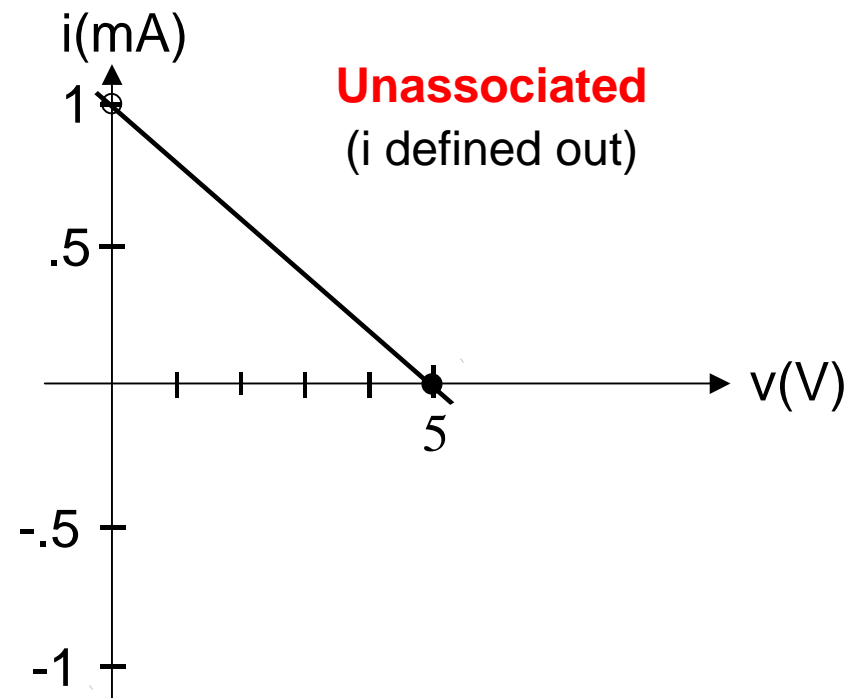
Apply v , measure i ,
or vice versa

First find open-circuit V

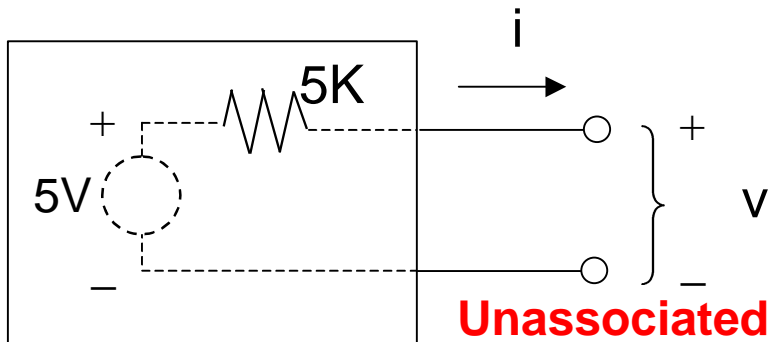
$$v = 5V \text{ if } i = 0$$

Now find Short-circuit I

$$i = +1\text{mA if } v = 0$$



I-V CHARACTERISTICS OF LINEAR TWO-TERMINAL NETWORKS



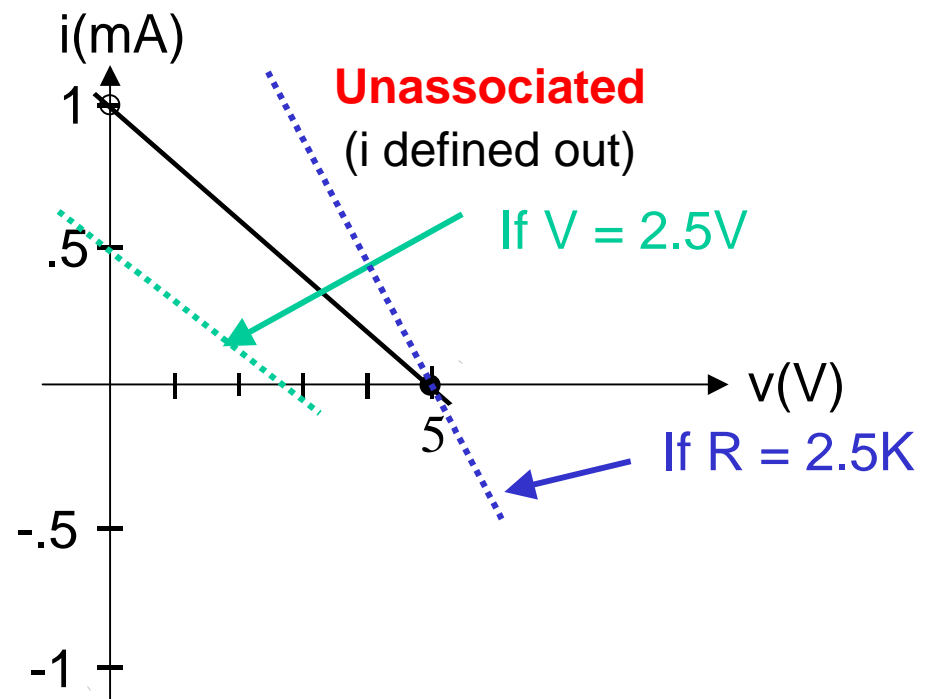
Apply v , measure i ,
or vice versa

First consider change in
 V , eg $V = 2.5V$, not $5V$

Now consider change in R
(with V back at $5V$)

Clearly by varying V and R we can produce an arbitrary linear graph
... in other words this circuit can produce *any* linear graph

Consider how the graph
changes with differences in V
and R .



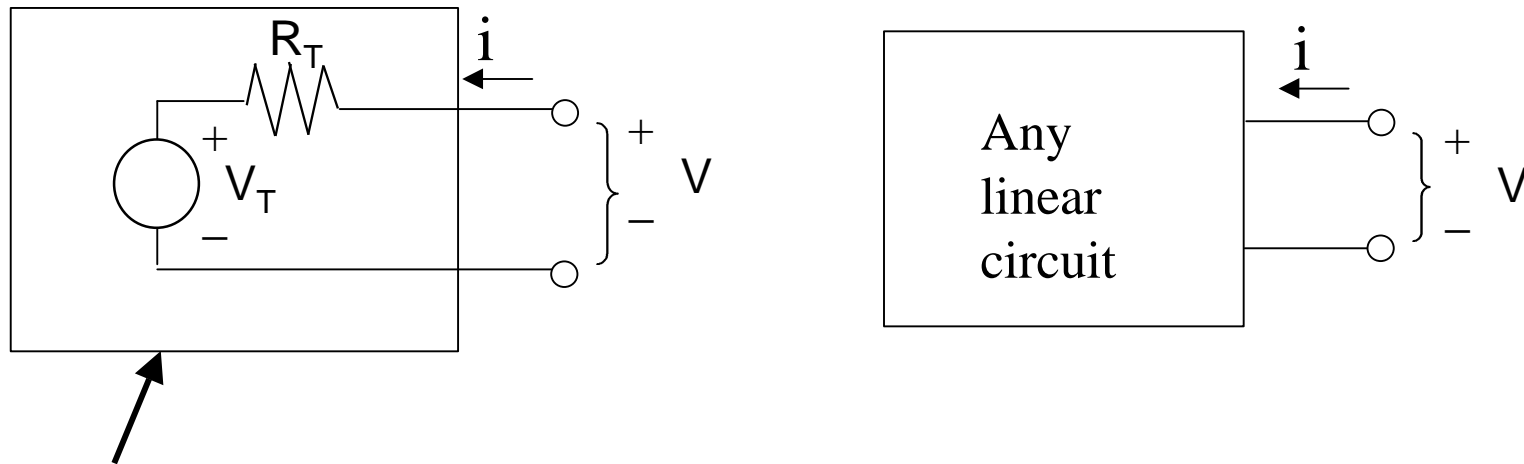
BASIS OF THÉVENIN THEOREM

- All **linear** one-ports have linear I-V graph
- A voltage source in series with a resistor can produce any linear I-V graph by suitably adjusting V and I

THUS

We define the voltage-source/resistor combination that replicates the I-V graph of a linear circuit to be the Thévenin equivalent of the circuit. The voltage source V_T is called the Thévenin equivalent voltage and the resistance R_T is called the Thévenin equivalent resistance.

Thévenin Equivalent Circuit

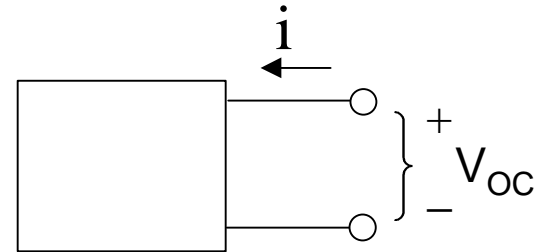
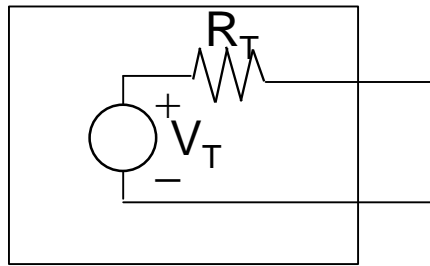


This circuit is equivalent to any circuit, that is by suitably choosing V_T and R_T it will have the same I-V graph

So how do we choose V_T and R_T ?

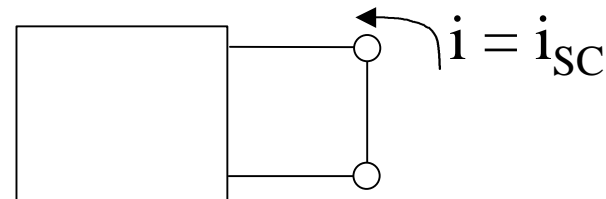
FINDING V_T , R_T BY MEASUREMENT

1 V_T is the open-circuit voltage V_{OC} (i.e., $i = 0$)



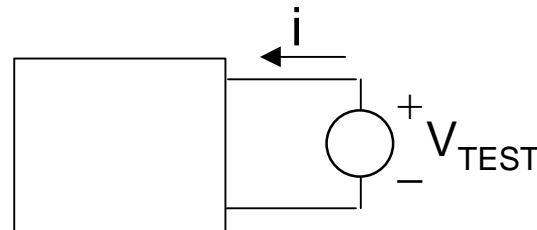
2a) If we short the output clearly $I = -V_T / R_T$ thus R_T is the ratio of V_{OC} to $-i_{SC}$, the short-circuit current

$$R_T = -\frac{V_{OC}}{I_{SC}}$$



2b) If $V_T = 0$, you need to apply test voltage, then

$$R_T = \frac{V_{TEST}}{i}$$



FINDING V_T , R_T BY ANALYSIS

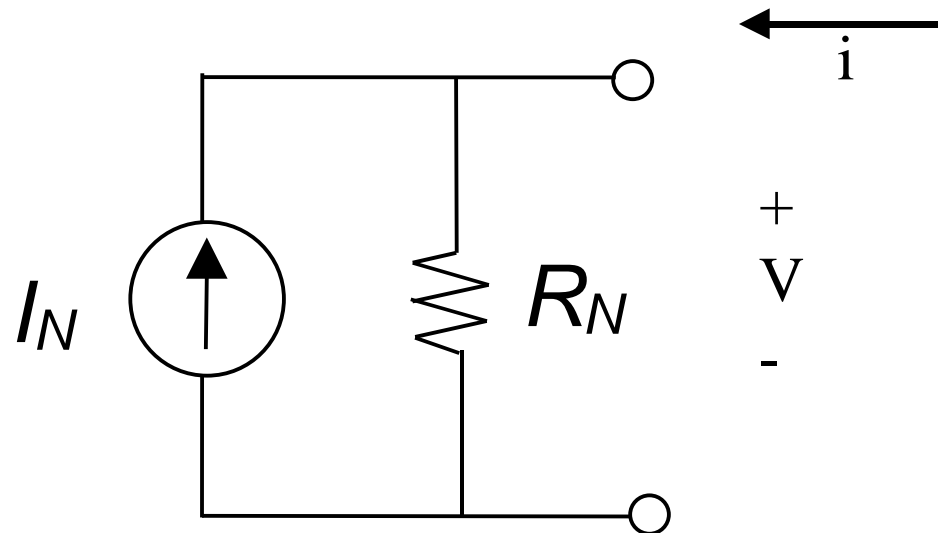
1 Calculate V_{OC} . $V_T = V_{OC}$

2 Turn off all independent sources and find equivalent R at terminals

NORTON EQUIVALENT CIRCUIT

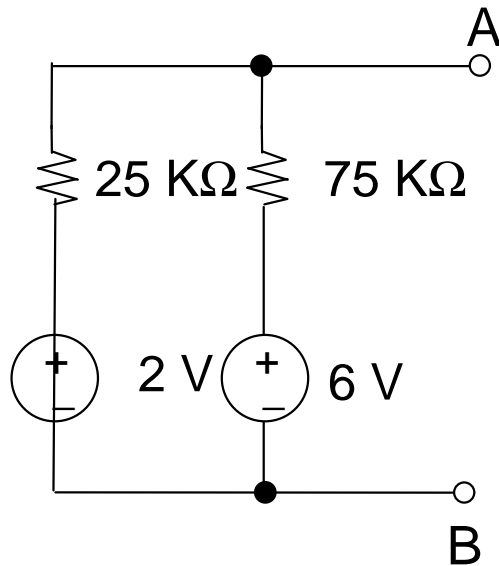
Corollary to Thévenin: $I_N = -I_{SC}$ (short - circuit current) (associated)

R_N is found the same way as for Thévenin equivalent



EXAMPLE

Find the Thévenin and Norton equivalents of:



Find $V_{AB} = V_{OC}$ from voltage divider. Left to right:

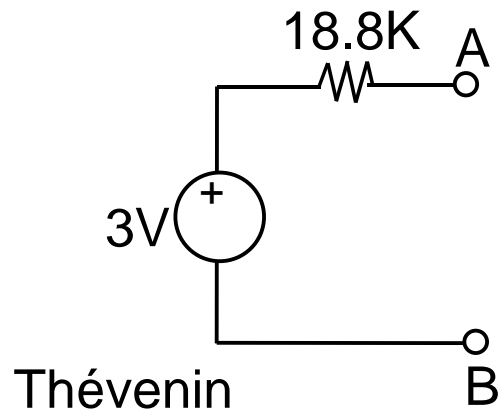
(4 V rise across 25K + 75K) \Rightarrow

3 V across 75K, 1 V across 25k.

So, $V_{AB} = -3 + 6 = 3V = V_{OC}$

$$I_{SC} = -6V/75K + 2V/25K = -0.16 \text{ mA} \quad R_{TH} = \frac{3}{.16 \times 10^{-3}} = 18.8K$$

equivalent to



and equivalent to

