



EECS 42 – Introduction to Electronics for Computer Science

Spring 2003
Dept. EECS,
UC Berkeley
Course Web Site <http://www-inst.EECS.Berkeley.EDU/~ee42/>

Prof. A. R. Neureuther
510 Cory 642-4590
OH M, Tu, W, (Th), F 11

Midterm #1 March 5th, 2003

Closed Book, Closed Notes
Write on the Exam paper

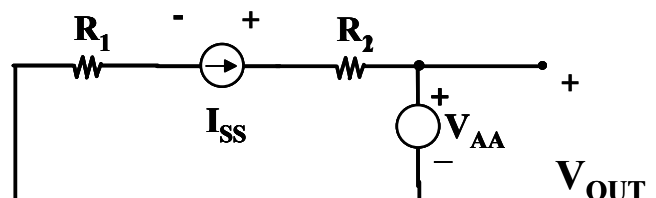
Print Your Name: _____ Solution _____

Sign Your Name: _____

Show your work so that the method as well as the answer can be graded for correctness and completeness. Correct answers alone are only worth 70% of full credit.

Problem	Possible	Score
I	28	
II	22	
III	25	
IV	25	
Total	100	

I (28 Points) Basic Circuit Analysis



$$V_{AA} = 2V \quad I_{ss} = 1 \text{ mA}$$

$$R_1 = 1k\Omega \quad R_2 = 2k\Omega \quad R_3 = 3k\Omega$$

a) (7 points) Find R_{TH} .

$$I_{ss} = 0 \Rightarrow R_1 \text{ and } R_2 \text{ disconnected}$$
$$R_{TH} = R_3$$

b) (7 points) Find V_{OC} .

$$V_{OC} = I_{ss} R_3 + V_{aa} = 1 \text{ mA } 3k\Omega + 2V = 5V$$

c) (7 points) Find the power delivered to the circuit by V_{AA} .

$$\text{Power} = - I_{ss} V_{aa} = - 1\text{mA } 2V = -2 \text{ mW}$$

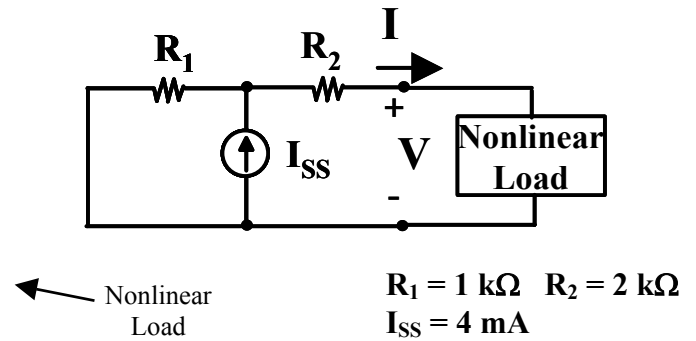
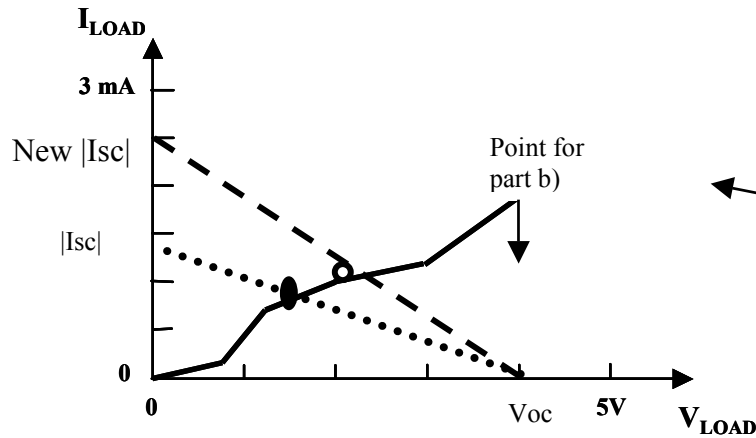
Note V_{aa} absorbs power from the circuit.

d) (7 points) Find the voltage on the current source I_{ss} in the direction shown on the diagram.

$$\text{Use a loop equation}$$
$$V_{ss} = I_{ss}R_2 + V_{aa} + I_{ss} R_3 - I_{ss} R_1 = 2V + 2V + 3V - 1V = 6V$$

II (22 Points) Load Lines

A linear circuit is connected to a nonlinear load.



- a) (12 points) Find the combination of current I and voltage V that satisfies both the circuit and the load.

$V_{oc} = I_{ss} R_1 = 1 \text{ mA} \cdot 4 \text{ k}\Omega = 4 \text{ V}$
 $|I_{sc}| = [R_1 / (R_1 + R_2)] I_{ss} = [1 \text{ k}\Omega / (1 \text{ k}\Omega + 2 \text{ k}\Omega)] \cdot 4 \text{ mA} = 1.33 \text{ mA}$
 Draw line from (4V, 0 mA) through (0V, 1.33 mA)
 Intersection is about (1.5V, 0.8 mA)

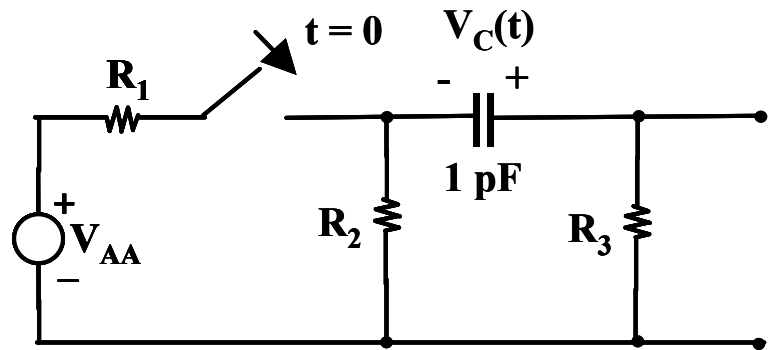
- b) (10 points) Adjust R_2 so that the solution passes through the point indicated on the device curve.

V_{oc} is unaffected by R_2 so still 4V.
 Draw a line from (4V, 0mA) through the given point which is approximately (2V, 1 mA) and hit $V = 0$ axis at about 2 mA.
 The new $R_{th} = 4 \text{ V} / 2 \text{ mA} = 2 \text{ k}\Omega$
 This gives the new $R_2 = R_{th} - R_1 = 2 \text{ k}\Omega - 1 \text{ k}\Omega = 1 \text{ k}\Omega$

III (25 Points) Transient

The switch in the circuit closes at $t = 0$. Just before switching the capacitor is charged to 2V.

a) (18 points) Find the voltage on the capacitor $V_C(t)$ for $t > 0$.



$$R_1 = 1\text{ k}\Omega \quad R_2 = 2\text{ k}\Omega \quad R_3 = 3\text{ k}\Omega$$

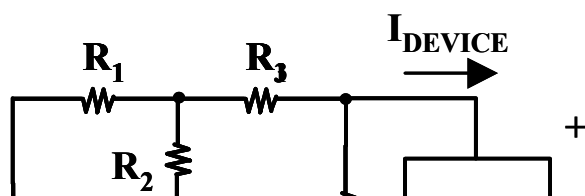
$$V_{AA} = 5\text{ V}$$

Given $V_{\text{initial}} = V_C(0) = 2\text{ V}$
 Find V_{final} as no current in C or R3 and R2 and R1 are voltage divider with voltage on C backward so
 $V_{oc}(\text{infinity}) = -[R_2/(R_1 + R_2)] V_{aa} = -[2\text{ k}\Omega/(1\text{ k}\Omega + 2\text{ k}\Omega)] 5\text{ V} = -3.33\text{ V}$
 Capacitor sees $R_{th} = R_1 \parallel R_2 + R_3 = 3.67\text{ k}\Omega$
 $\tau = 1\text{ pF} \cdot 3.67\text{ k}\Omega = 3.67\text{ ns}$
 $V_C(t) = A + B e^{-t/\tau}$
 $A = V_{\text{final}} = -3.33\text{ V}$
 $B = 2\text{ V} - A = 5.33\text{ V}$
 $V_C(t) = -3.33 + 5.33 e^{-t/3.67\text{ ns}}$

b) (7 points) Find $dV_C(t)/dt$ just prior to the switch closing at $t = 0$.

$i(t) = C \frac{dV}{dt} \Rightarrow \frac{dV}{dt} = i(t)/C$ where current is into the + terminal
 When $V_C = 2\text{ V}$ and the switch is open a current flows out of the positive terminal of C through R2 and R3 back to the negative terminal. This $i(0^-) = -V_C/(R_2 + R_3) = -2\text{ V}/(2\text{ k}\Omega + 3\text{ k}\Omega) = -0.4\text{ mA}$.
 $DV/dt = -0.4\text{ mA}/1\text{ pF} = -0.4\text{ V/ns}$

IV (25 Points) Node Equations



a) (15 points) Assign labels to the nodes and write a complete set of node equations for determining the node voltages. (These equations should contain only the node voltages themselves, resistances, source strengths and the device current.)

Assign bottom terminal to ground.
Label top of R1 as node a.
Label top of node R4 as node b.

$$\mathbf{R_1 = 1k\Omega \quad R_2 = 2 k\Omega \quad R_3 = 3 k\Omega \quad R_4 = 4 k\Omega}$$

$$\mathbf{V_{AA} = 5 V \quad I_{SS} = 1 mA}$$

$$\frac{V_{AA} - V_a}{R_1} + I_{SS} + \frac{V_b - V_a}{R_3} = 0$$

$$\frac{V_a - V_b}{R_3} - \frac{V_b}{R_4} - I_{DEVICE} = 0$$

b) (10 points) Use **one** of your node equations from above to find the voltage on I_{SS} when the voltage on the device is 2V. (Hint: Substitute the device voltage to break the equations apart to avoid excessive algebra).

Use top equation and plug in $V_b = 2V$.

$$\frac{5V - V_a}{1k\Omega} + 1mA + \frac{2V - V_a}{3k\Omega} = 0$$

$$V_a \left(\frac{1}{1k\Omega} + \frac{1}{3k\Omega} \right) = 5mA + 1mA + 0.67mA = 6.67mA$$

$$V_a = [6.67mA] / (0.75k\Omega) = 5V$$

$$V_{SS} = I_{SS} \cdot R_2 + V_a = 1mA \cdot 2k\Omega + 5V = 7V$$