Problem 1: Verilog

A) The following code describes a 3-bit linear-feedback shift register (LFSR), which generates a repeating pattern of pseudo-random numbers.

```verilog
module lfsr(
    input [2:0] R,
    input Load,
    input Clock,
    output reg [2:0] Q
);

always@ (posedge Clock)
    if (Load)
        Q <= R;
    else
        Q <= {Q[1], Q[0] ^ Q[2], Q[2]};
endmodule
```

(a) Draw the circuit that corresponds to the code, using combinational logic blocks (gates etc.) and state elements.

(b) If 100 is loaded into the LFSR initially, what is the sequence of numbers generated? List the binary numbers it generates, start from 001.

B) The code below is similar to the code in the previous, but blocking assignments are used. The example below should illustrate why blocking assignments for synchronous logic should be avoided if possible.

```verilog
module lfsr(R, Load, Clock, Q);
    input [2:0] R;
    input Load, Clock;
    output reg [2:0] Q;

    always@ (posedge Clock)
        if (Load)
            Q <= R;
        else begin
            Q[0] = Q[2];
            Q[1] = Q[0] ^ Q[2];
            Q[2] = Q[1];
        end
endmodule
```

end
endmodule

(a) Draw the circuit that corresponds to the code.
(b) If 001 is loaded initially, what is the sequence of numbers generated?

**Problem 2: Timing**

The timing parameters for the circuit below are as follows:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Setup time</td>
<td>50 ps</td>
</tr>
<tr>
<td>Hold time</td>
<td>45 ps</td>
</tr>
<tr>
<td>Clock-to-q delay</td>
<td>40 ps (min), 60 ps (max)</td>
</tr>
<tr>
<td>Propagation delay per gate</td>
<td>80 ps (min), 100 ps (max)</td>
</tr>
</tbody>
</table>

![Circuit Diagram]

A) Identify the critical path (i.e. the longest timing path) or paths in this circuit. You may make use of the register names (R1 and R2) and the gate names (G1, G2, G3, G4) to help you describe the critical path(s).

B) Use your answer in part (a) to calculate the maximum clock rate at which this circuit can be reliably run.

C) Can the register hold times ever be violated in this circuit? Why?

**Problem 3: Edge Detector Circuit**

Design a Verilog module to detect the falling edge of an input signal. The input signal is synchronous to the clock, and when a falling edge is seen, a 1 clock cycle pulse should be emitted as an output signal.

```verilog
module edge_detector (input signal, input clk, output falling_edge);
    /* Your code here */
endmodule
```

Draw your Verilog implementation of this circuit as a schematic of gates and flip-flops.
Problem 4: Build a Multiplier Using an Accumulator

Construct a multiplier by accumulating the results of an adder. Here is a Verilog template to complete.

```verilog
module multiplier (  
   input clk, input start, output done,  
   input [15:0] arg1, input [15:0] arg2,  
   output [31:0] product  
);  
   reg [15:0] counter;  
   reg [31:0] accumulator;  
   /* Your code here */
endmodule
```

You can assume that the `start` input is pulsed for one clock cycle and after it is pulsed the `arg1` and `arg2` inputs are held stable until the `done` output goes high. Also assume that the logic driving the multiplier is well behaved (it doesn’t toggle `start` until the multiplier is done with the last computation).