

**UNIVERSITY OF CALIFORNIA**  
**College of Engineering**  
**Department of Electrical Engineering and Computer Sciences**  
**NTU 247**

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**Homework 2**  
**Due Thursday, February 1, 2007**

**NTU 247**  
**Spring 2007**

1. Design a filter with the following response:

$$\frac{s(s^2 + 9.839 \times 10^{12})(s^2 + 2.081 \times 10^{13})}{(s + 2.34 \times 10^7)(s^2 + 5.831 \times 10^5 s + 4.066 \times 10^{13})(s^2 + 4.243 \times 10^6 s + 7.811 \times 10^{13})}$$

- a) What kind of a filter is this (low-pass, band-pass, etc)?
- b) Plot the magnitude response using MATLAB. What are the filter cutoff-frequency, pass-band ripple, and stop-band attenuation?
- c) Realize the filter with a cascade of Tow-Thomas biquads and a single first-order section (that you will have to “invent” yourself). Use  $C=100\text{pF}$  for all capacitors. Choose the amplifier gains such that the pass-band outputs of all amplifiers are equal to 1V for a 1V input. Show your result in SPICE and compare with MATLAB.
- d) Determine the total noise at the filter output in  $\mu\text{V rms}$ . Use SPICE and noiseless operational amplifiers with 1GHz unity-gain bandwidth.
- e) Rescale the capacitors to meet a  $100\mu\text{V rms}$  noise target.
- f) Re-simulate your filter with “real” opams with 20MHz unity-gain bandwidth and  $10\text{k}\Omega$  equivalent noise resistance. How do the amplitude response and total noise change? Change the specifications for the operational amplifier to get less than 1dB error in the magnitude response up to 10MHz and  $200\mu\text{V rms}$  noise. Are the new amplifier specs realistic? Check the web to find an appropriate part (Texas Instruments, Analog Devices, Maxim, Linear Technology, National Semiconductor ...).

2. Consider the analog signal  $x(t) = \cos(2\pi f_1 t) + \cos(2\pi f_2 t) + \cos(2\pi f_3 t)$  with  $f_1 = 0.5\text{MHz}$ ,  $f_2 = 3\text{MHz}$ ,  $f_3 = 6\text{MHz}$ .

- a) What is the minimum sampling frequency  $f_s$  that avoids aliasing?
- b) Assume that we sample  $x(t)$  at  $f_s = 5\text{MHz}$ . What is the discrete time signal obtained after sampling? Can we reconstruct the original signal from the discrete time sequence? Given an example of a signal  $x'(t)$  that has the same discrete time representation as  $x(t)$ .