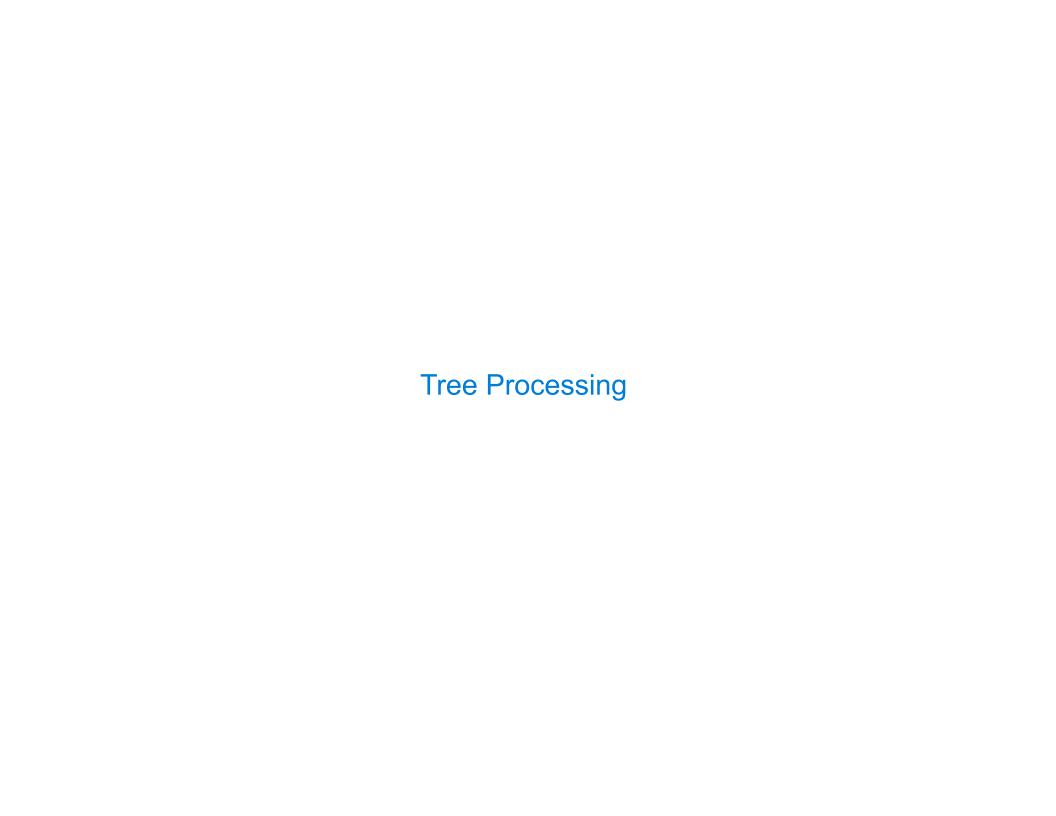




### **Tree-Structured Data**

```
def tree(label, branches=[]):
                                                         A tree can contains other trees:
   return [label] + list(branches)
                                                         [5, [6, 7], 8, [[9], 10]]
def label(tree):
   return tree[0]
                                                         (+5(-67)8(*(-9)10))
def branches(tree):
   return tree[1:]
                                                         (S
class Tree:
                                                           (NP (JJ Short) (NNS cuts))
   def init (self, label, branches=[]):
                                                          (VP (VBP make)
       self.label = label
                                                              (NP (JJ long) (NNS delays)))
       self.branches = list(branches)
                                                          (...))
class BTree(Tree):
                                                        <111>
   empty = Tree(None)
                                                          Midterm <b>1</b>
   def init (self, label, left=empty, right=empty):
                                                          Midterm <b>2</b>
       Tree. init (self, label, [left, right])
                                                        @property
   def left(self):
                                                        Tree processing often involves
       return self.branches[0]
                                                         recursive calls on subtrees
   @property
   def right(self):
       return self.branches[1]
```



### Solving Tree Problems

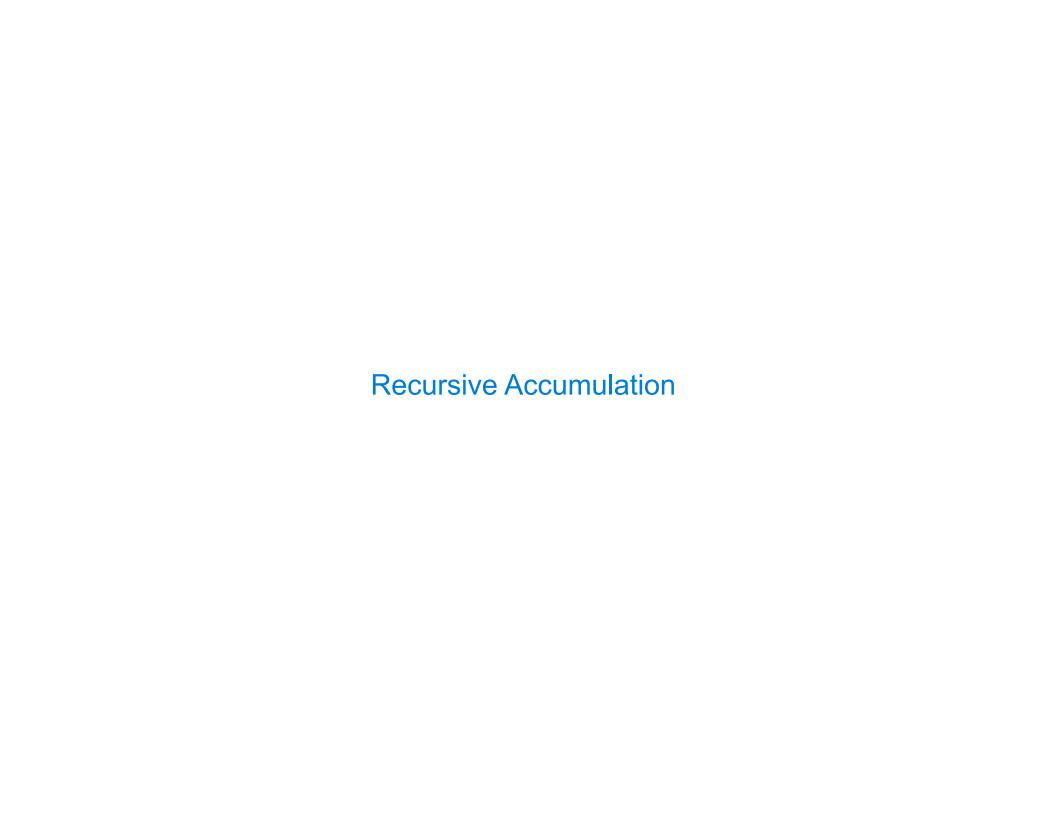
Implement **bigs**, which takes a Tree instance t containing integer labels. It returns the number of nodes in t whose labels are larger than any labels of their ancestor nodes.

```
def bigs(t):
    """Return the number of nodes in t that are larger than all their ancestors.
   >>> a = Tree(1, [Tree(4, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(2)])])])
   >>> bigs(a)
   11 11 11
                                                                                       5
  The root label is always larger than all of its ancestors
                                                                Somehow track a
  if t.is leaf():
                                                               list of ancestors
       return
  else:
                                                  if node.label > max(ancestors):
       return ([ for b in t.branches])
                                                               Somehow track the
                                                                largest ancestor
             Somehow increment
              the total count
                                                 if node.label > max ancestors:
```

### Solving Tree Problems

Implement bigs, which takes a Tree instance t containing integer labels. It returns the number of nodes in t whose labels are larger than any labels of their ancestor nodes.

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     """Return the number of nodes in t that are larger than all their ancestors.
     >>> a = Tree(1, [Tree(4, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(2)])])])
     >>> bigs(a)
                   Somehow track the
     11 11 11
                    largest ancestor
     def f(a, x):
A node in t max ancestor
                          node.label > max ancestors
            a.label > x
             return 1 + sum([f(b, a.label) for b in a.branches])
                        Somehow increment the total count
         else:
                        sum([f(b, x) for b in a.branches])
     return f(t, t.label - 1)
                                Root label is always larger than its ancestors
                   Some initial value for the largest ancestor so far...
```



# Solving Tree Problems

Implement bigs, which takes a Tree instance t containing integer labels. It returns the number of nodes in t whose labels are larger than any labels of their ancestor nodes.

9

Designing Functions

### How to Design Programs

### From Problem Analysis to Data Definitions

Identify the information that must be represented and how it is represented in the chosen programming language. Formulate data definitions and illustrate them with examples.

#### Signature, Purpose Statement, Header

State what kind of data the desired function consumes and produces. Formulate a concise answer to the question what the function computes. Define a stub that lives up to the signature.

#### **Functional Examples**

Work through examples that illustrate the function's purpose.

### **Function Template**

Translate the data definitions into an outline of the function.

#### **Function Definition**

Fill in the gaps in the function template. Exploit the purpose statement and the examples.

#### **Testing**

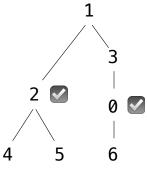
Articulate the <u>examples</u> as tests and ensure that the function passes all. Doing so discovers mistakes. Tests also supplement examples in that they help others read and understand the definition when the need arises—and it will arise for any serious program.

Applying the Design Process

# Designing a Function

Implement smalls, which takes a Tree instance t containing integer labels. It returns the non-leaf nodes in t whose labels are smaller than any labels of their descendant nodes.

```
Signature: Tree -> List of Trees
def smalls(t):
    """Return the non-leaf nodes in t that are smaller than all their descendants.
    >>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])])])
    >>> sorted([t.label for t in smalls(a)])
    [0, 2]
    11 11 11
                        Signature: Tree -> number
   result = []
                        "Find smallest label in t & maybe add t to result"
    def process(t):
       if t.is leaf():
           return t.label
       else:
           return min(...)
   process(t)
    return result
```





# Designing a Function

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   def smalls(t):
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       >>> sorted([t.label for t in smalls(a)])
       [0, 2]
       11 11 11
                            Signature: Tree -> number
       result = []
                            "Find smallest label in t & maybe add t to result"
       def process(t):
           if t.is leaf():
                                      t.label
               return
           else:
smallest labelsmallest =
                             min([process(b) for b in t.branches])
                       t.label < smallest</pre>
in a branch of t
                     result.append( t )
               return min(smallest, t.label)
       process(t)
       return result
```