

Designing Functions

Describing Functions

A function's *domain* is the set of all inputs it might possibly take as arguments.

A function's *range* is the set of output values it might possibly return.

A pure function's *behavior* is the relationship it creates between input and output.

def square(x):
 """Return X * X."""

x is a number

square returns a nonnegative real number

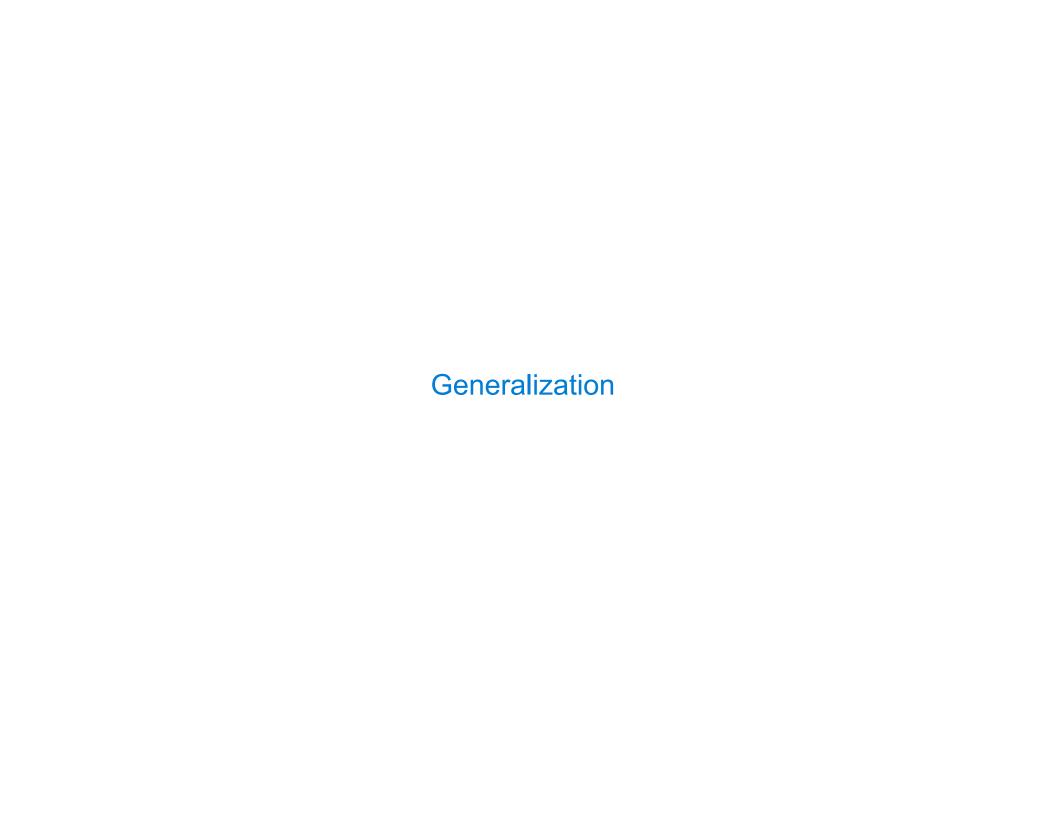
square returns the square of x

A Guide to Designing Function

Give each function exactly one job, but make it apply to many related situations

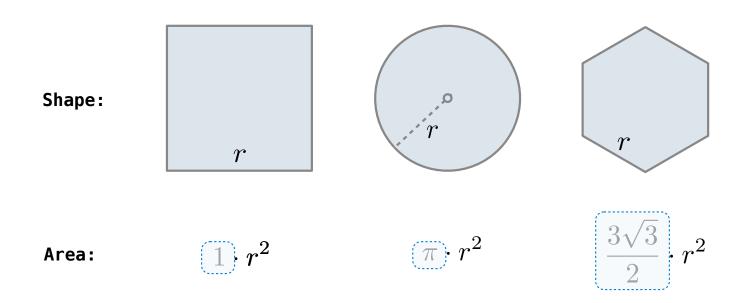
Don't repeat yourself (DRY). Implement a process just once, but execute it many times.



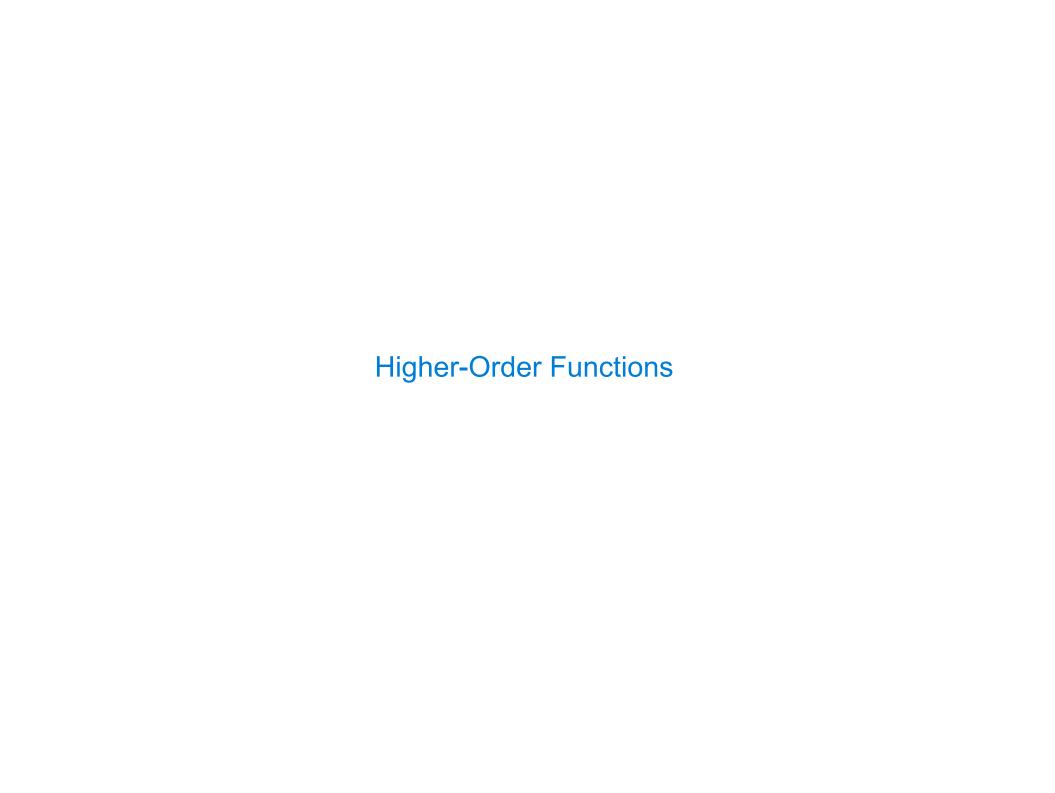


Generalizing Patterns with Arguments

Regular geometric shapes relate length and area.



Finding common structure allows for shared implementation



Generalizing Over Computational Processes

The common structure among functions may be a computational process, rather than a number.

$$\sum_{k=1}^{5} (k) = 1 + 2 + 3 + 4 + 5 = 15$$

$$\sum_{k=1}^{5} k^{3} = 1^{3} + 2^{3} + 3^{3} + 4^{3} + 5^{3} = 225$$

$$\sum_{k=1}^{5} \frac{8}{(4k-3)\cdot(4k-1)} = \frac{8}{3} + \frac{8}{35} + \frac{8}{99} + \frac{8}{195} + \frac{8}{323} = 3.04$$

(Demo)

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Summation Example

```
Function of a single argument
def cube(k):
                                 (not called "term")
    return pow(k, 3)
                            A formal parameter that will
def summation(n, term)
                               be bound to a function
     """Sum the first n terms of a sequence.
    >>> summation(5, cube)
     225
                           The cube function is passed
     11 11 11
                              as an argument value
    total, k = 0, 1
    while k <= n:
          total, k = total + term(k), k + 1
    return total
                             The function bound to term
  0 + 1 + 8 + 27 + 64 + 125
                                 gets called here
```

Functions as Return Values

Locally Defined Functions

Functions defined within other function bodies are bound to names in a local frame

```
A function that returns a function

def make adder(n):

"""Return a function that takes one argument k and returns k + n.

>>> add_three = make_adder(3)

>>> add_three(4)

The name add_three is bound to a function

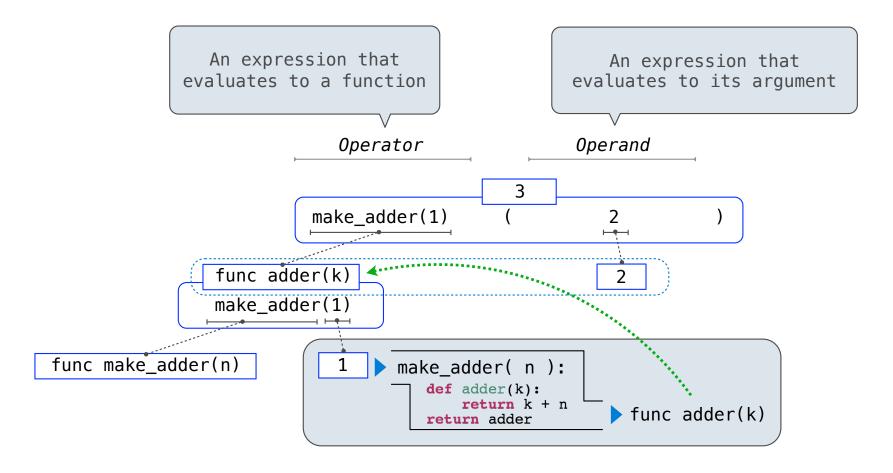
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"""

def adder(k):
    return(k + n)
    A def statement within another def statement

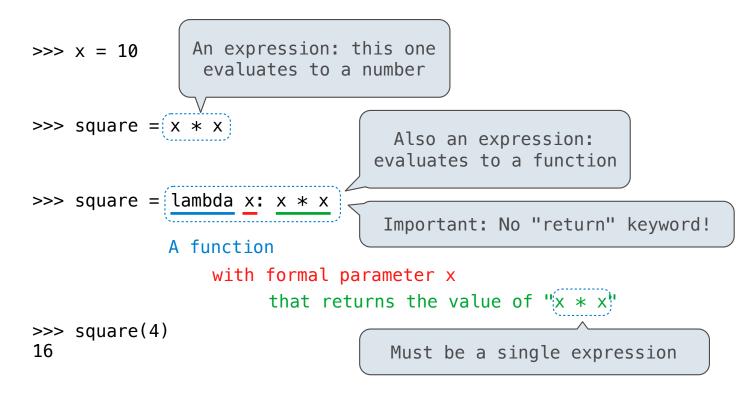
Can refer to names in the enclosing function
```

Call Expressions as Operator Expressions



Lambda Expressions

Lambda Expressions



Lambda expressions are not common in Python, but important in general Lambda expressions in Python cannot contain statements at all!

Lambda Expressions Versus Def Statements



- Both create a function with the same domain, range, and behavior.
- Both bind that function to the name square.
- Only the def statement gives the function an intrinsic name, which shows up in environment diagrams but doesn't affect execution (unless the function is printed).

