

## 1 Control

**Control structures** direct the flow of logic in a program. For example, conditionals (if-elif-else) allow a program to skip sections of code, while iteration (**while**), allows a program to repeat a section.

### If statements

**Conditional statements** let programs execute different lines of code depending on certain conditions. Let's review the if- elif-else syntax.

Recall the following points:

- The **else** and **elif** clauses are optional, and you can have any number of **elif** clauses.
- A **conditional expression** is a expression that evaluates to either a true value (True, a non-zero integer, etc.) or a false value (False, 0, None, "", [], etc.).
- Only the **suite** that is indented under the first if/elif with a **conditional expression** evaluating to a true value will be executed.
- If none of the **conditional expressions** evaluate to a true value, then the **else** suite is executed. There can only be one **else** clause in a conditional statement!

```
if <conditional expression>:  
    <suite of statements>  
elif <conditional expression>:  
    <suite of statements>  
else:  
    <suite of statements>
```

### Boolean Operators

Python also includes the **boolean operators** **and**, **or**, and **not**. These operators are used to combine and manipulate boolean values.

- **not** returns the opposite truth value of the following expression.
- **and** stops evaluating any more expressions (short-circuits) once it reaches the first false value and returns it. If all values evaluate to a true value, the last value is returned.
- **or** short-circuits at the first true value and returns it. If all values evaluate to a false value, the last value is returned.

```
>>> not None  
True  
>>> not True  
False  
>>> -1 and 0 and 1  
0  
>>> False or 9999 or 1/0  
9999
```

## Questions

- 1.1 Alfonso will only wear a jacket outside if it is below 60 degrees or it is raining.

Write a function that takes in the current temperature and a Boolean value telling if it is raining and returns `True` if Alfonso will wear a jacket and `False` otherwise.

This should only take one line of code!

```
def wears_jacket(temp, raining):  
    """  
    >>> wears_jacket(90, False)  
    False  
    >>> wears_jacket(40, False)  
    True  
    >>> wears_jacket(100, True)  
    True  
    """
```

- 1.2 To handle discussion section overflow, TAs may direct students to a more empty section that is happening at the same time.

Write a function that takes in the number of students in two sections and prints out what to do if either section exceeds 30 students.

```
def handle_overflow(s1, s2):  
    """  
    >>> handle_overflow(27, 15)  
    No overflow  
    >>> handle_overflow(35, 29)  
    Move to Section 2: 1  
    >>> handle_overflow(20, 32)  
    Move to Section 1: 10  
    >>> handle_overflow(35, 30)  
    No space left in either section  
    """
```

## While loops

Iteration lets a program repeat statements multiple times. A common iterative block of code is the **while loop**.

As long as `<conditional clause>` evaluates to a true value, `<body of statements>` will continue to be executed. The conditional clause gets evaluated each time the body finishes executing.

```
while <conditional clause>:
    <body of statements>
```

## Questions

- 1.3 What is the result of evaluating the following code?

```
def square(x):
    return x * x

def so_slow(num):
    x = num
    while x > 0:
        x = x + 1
    return x / 0

square(so_slow(5))
```

- 1.4 Write a function that returns `True` if `n` is a prime number and `False` otherwise. After you have a working solution, think about potential ways to make your solution more *efficient*.

**Hint:** use the `%` operator: `x % y` returns the remainder of `x` when divided by `y`.

```
def is_prime(n):
    """
    >>> is_prime(10)
    False
    >>> is_prime(7)
    True
    """
```

## 2 Higher Order Functions

A **higher order function** (HOF) is a function that manipulates other functions by taking in functions as arguments, returning a function, or both.

### Functions as Arguments

One way a higher order function can manipulate other functions is by taking functions as input (an argument). Consider this higher order function called `negate`.

```
def negate(f, x):
    return -f(x)
```

`negate` takes in a function `f` and a number `x`. It doesn't care what exactly `f` does, as long as `f` is a function, takes in a number and returns a number. Its job is simple: call `f` on `x` and return the negation of that value.

### Questions

- 2.1 Write a function that takes in a function `cond` and a number `n` and prints numbers from 1 to `n` where calling `cond` on that number returns `True`.

```
def keep_ints(cond, n):
    """Print out all integers 1..i..n where cond(i) is true

    >>> def is_even(x):
    ...     # Even numbers have remainder 0 when divided by 2.
    ...     return x % 2 == 0
    >>> keep_ints(is_even, 5)
    2
    4
    """
```

## Functions as Return Values

Often, we will need to write a function that returns another function. One way to do this is to define a function inside of a function:

The return value of `outer` is the function `inner`. This is a case of a function returning a function. In this example, `inner` is defined inside of `outer`. Although this is a common pattern, we can also define `inner` outside of `outer` and still use the same return statement. However, note that in this second example (unlike the first example), `inner` doesn't have access to variables defined within the `outer` function, like `x`.

```
def outer(x):
    def inner(y):
        ...
    return inner
```

```
def inner(y):
    ...
def outer(x):
    return inner
```

## Questions

- 2.2 Use this definition of `outer` to fill in what Python would display when the following lines are evaluated.

```
>>> def outer(n):
...     def inner(m):
...         return n - m
...     return inner
```

```
>>> outer(61)
```

```
>>> f = outer(10)
>>> f(4)
```

```
>>> outer(5)(4)
```

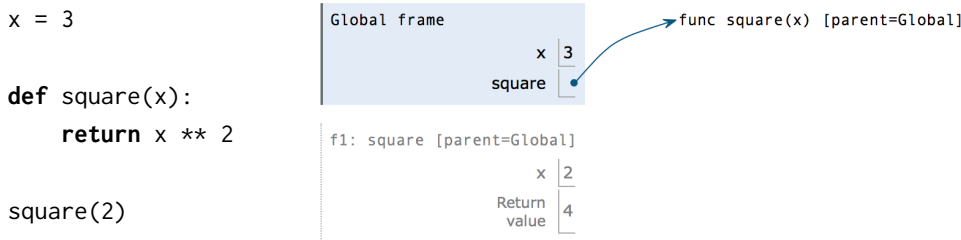
- 2.3 Write a function similar to `keep_ints` like before, but now it takes in a number `n` and returns a function that has one parameter `cond`. The returned function prints out numbers from 1 to `n` where calling `cond` on that number returns `True`.

```
def keep_ints(n):
    """Returns a function which takes one parameter cond and prints out
    all integers 1..i..n where calling cond(i) returns True.

    >>> def is_even(x):
    ...     # Even numbers have remainder 0 when divided by 2.
    ...     return x % 2 == 0
    >>> keep_ints(5)(is_even)
    2
    4
    """
```

### 3 Environment Diagrams

An **environment diagram** keeps track of all the variables that have been defined and the values they are bound to.



When you execute *assignment statements* in an environment diagram (like `x = 3`), you need to record the variable name and the value:

1. Evaluate the expression on the right side of the = sign
2. Write the variable name and the expression's value in the current frame.

When you execute *def statements*, you need to record the function name and bind the function object to the name.

1. Write the function name (e.g., `square`) in the frame and point it to a function object (e.g., `func square(x) [parent=Global]`). The `[parent=Global]` denotes the frame in which the function was *defined*.

When you execute a *call expression* (like `square(2)`), you need to create a new frame to keep track of local variables.

1. Draw a new frame. <sup>a</sup> Label it with
  - a unique index (`f1`, `f2`, `f3` and so on)
  - the **intrinsic name** of the function (`square`), which is the name of the function object itself. For example, if the function object is `func square(x) [parent=Global]`, the intrinsic name is `square`.
  - the parent frame (`[parent=Global]`)
2. Bind the formal parameters to the arguments passed in (e.g. bind `x` to 3).
3. Evaluate the body of the function.

If a function does not have a return value, it implicitly returns `None`. Thus, the "Return value" box should contain `None`.

<sup>a</sup>Since we do not know how built-in functions like `add(...)` or `min(...)` are implemented, we do *not* draw a new frame when we call built-in functions.

## Questions

- 3.1 Draw the environment diagram that results from executing the code below.

```
a = 1
def b(b):
    return a + b
a = b(a)
a = b(a)
```

- 3.2 Draw the environment diagram that results from executing the code below. What will be the output (note this separately from the diagram)?

```
from operator import add
def sub(a, b):
    sub = add
    return a - b
add = sub
sub = min
print(add(2, sub(2, 3)))
```