1 Introduction

In the next part of the course, we will be working with the **Scheme** programming language. In addition to learning how to write Scheme programs, we will eventually write a Scheme interpreter in Project 4!

Scheme is a dialect of the **Lisp** programming language, a language dating back to 1958. The popularity of Scheme within the programming language community stems from its simplicity – in fact, previous versions of CS 61A were taught in the Scheme language.

2 Primitives

Scheme has a set of *atomic* primitive expressions. Atomic means that these expressions cannot be divided up.

```
scm> 123
123
scm> 123.123
123.123
scm> #t
True
scm> #f
False
```

Unlike in Python, the only primitive in Scheme that is a false value is **#f** and its equivalents, **false** and **False**. The **define** special form defines variables and procedures by binding a value to a variable, just like the assignment statement in Python. When a variable is defined, the **define** special form returns a symbol of its name. A procedure is what we call a function in Scheme!

The syntax to define a variable and procedure are:

- (define <variable name> <value>)
- (define (<function name> <parameters>) <function body>)

Questions

2.1 What would Scheme display?

```
scm> (define a 1)
```

scm> a

scm> (define b a)

scm> b

scm> (define c 'a)

scm> c

3 Call Expressions

To call a function in Scheme, you first need a set of parentheses. Inside the parentheses, you specify an operator expression, then zero or more oprand subexpressions (remember the spaces!).

Operators may be symbols, such as + and * or more complex expressions, as long as they evaluate to procedure values.

```
scm> (- 1 1) ; 1 - 1
0
scm> (/ 8 4 2) ; 8 / 4 / 2
1
scm> (* (+ 1 2) (+ 1 2)) ; (1 + 2) * (1 + 2)
9
```

Evaluating a Scheme function call works just like Python:

- 1. Evaluate the operator (the first expression after the (), then evaluate each of the operands.
- 2. Apply the operator to those evaluated operands.

When you evaluate (+ 1 2), you evaluate the + symbol, which is bound to a built-in addition function. Then, you evaluate 1 and 2, which are primitives. Finally, you apply the addition function to 1 and 2.

Questions

3.1 What would Scheme display?

```
scm> (+ 1)
```

scm> (* 3)

```
scm> (+ (* 3 3) (* 4 4))
```

```
scm> (define a (define b 3))
```

scm> a

scm> b

4 Special Forms

There are certain expressions that look like function calls, but *don't* follow the rule for order of evaluation. These are called *special forms*. You've already seen one — define, where the first argument, the variable name, doesn't actually get evaluated to a value.

4.1 If Expression

Another common special form is the **if** form. An **if** expression looks like: (**if** <condition> <then> <**else**>)

where <condition>, <then> and <else> are expressions. First, <condition> is evaluated. If it evaluates to #t, then <then> is evaluated. Otherwise, <else> is evaluated.

Remember that only **#f** is a false-y value (also False for our interpreter); everything else is truth-y.

```
scm> (if (< 4 5) 1 2)
1
scm> (if #f (/ 1 0) 42)
42
```

4.2 Boolean Operators

Much like Python, Scheme also has the boolean operators **and**, **or**, and **not**. In addition, **and** and **or** are also special forms because they are short-circuiting operators.

```
scm> (and 25 32)
32
scm> (or 1 2)
1
```

Questions

4.1 What would Scheme display?

scm> (if (or #t (/ 1 0)) 1 (/ 1 0))

scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))

```
scm> ((if (< 4 3) + -) 4 100)
```

scm> (if 0 1 2)

4.3 Lambdas and Defining Functions

Scheme has lambdas too! The syntax is (lambda (<PARAMETERS>) <EXPR>)

Like in Python, lambdas are function values. Also like in Python, when a lambda expression is called in Scheme, a new frame is created where the parameters are bound to the arguments passed in. Then, < EXPR > is evaluated in this new frame. Note that < EXPR > is not evaluated until the lambda function is called.

Like in Python, lambda functions are also values! So you can do this to define functions:

```
scm> (define (square x) (* x x)) ; Create function square using define special form
square
scm> (define square (lambda (x) (* x x))) ; Equivalently, bind the name square to a lambda function
square
scm> (square 4)
16
```

let is another special form based around lambda. The structure of let is as follows:

This binds the results of evaluating expressions 1 through n to their associated symbols, creating temporary variables. Finally, the body of the let is evaluated.

This special form is really just equivalent to:

((lambda (<SYMBOL1> ... <SYMBOLN>) <BODY>) <EXPR1> ... <EXPRN>)

Think of the temporary variables as being the parameters of a lambda function. Then, the arguments are the values of the expressions, which we bind to the temporary variables by calling the lambda.

Consider the following example:

(let ((x 1) (y 2)) (+ x y))

This is equivalent to:

((**lambda** (x y) (+ x y)) 1 2)

Questions

4.1 Write a function that returns the factorial of a number.

```
(define (factorial x)
```

4.2 Write a function that returns the n^{th} Fibonacci number.

```
(define (fib n)
(if (or (= n 0) (= n 1))
n
```

5 Pairs and Lists

To construct a (linked) list in Scheme, you can use the constructor **cons** (which takes two arguments). nil represents the empty list. If you have a linked list in Scheme, you can use selector **car** to get the first element and selector **cdr** to get the rest of the list. (**car** and **cdr** don't stand for anything anymore, but if you want the history go to http://en.wikipedia.org/wiki/CAR_and_CDR).

```
scm> nil
()
scm> (null? nil)
#t
scm> (cons 2 nil)
(2)
scm> (cons 3 (cons 2 nil))
(3 2)
scm> (define a (cons 3 (cons 2 nil)))
а
scm> (car a)
3
scm> (cdr a)
(2)
scm> (car (cdr a))
2
scm> (define (len a)
       (if (null? a)
         0
         (+ 1 (len (cdr a))))
len
scm> (len a)
2
```

If a list is a "good looking" list, like the ones above where the second element is always a linked list, we call it a **well-formed list**. Interestingly, in Scheme, the second element does not have to be a linked list. You can supply something else instead, creating a **malformed list**. The difference is shown with a dot:

```
scm> (cons 2 3)
(2 . 3)
scm> (cons 2 (cons 3 nil))
(2 3)
scm> (cdr (cons 2 3))
3
scm> (cdr (cons 2 (cons 3 nil)))
(3)
```

In general, the rule for displaying a pair is as follows: use the dot to separate the car and cdr fields of a pair, but if the dot is immediately followed by an open

parenthesis, then remove the dot and the parenthesis pair. Thus, $(0\ .\ (1\ .\ 2))$ becomes $(0\ 1\ .\ 2)$

There are many useful operations and shorthands on lists. list takes zero or more arguments and returns a list of its arguments.

This typically behaves much like quoting a list, except that quoting will not evaluate the list you have quoted which can result in some different outcomes.

```
scm> (list 1 2 3)
(1 2 3)
scm> '(1 2 3)
(1 2 3)
scm> (car '(1 2 3))
1
scm> (equal? '(1 2 3) (list 1 2 3))
#t
scm> '(1 . (2 3))
(1 2 3)
scm> '(define (square x) (* x x))
(define (square x) (* x x))
scm> square ; We didn't actually define square above because of the quote
Error
scm> (list (cons 1 2))
((1 . 2))
scm> '((cons 1 2))
((cons 1 2))
```

=, eq?, equal?

- = can only be used for comparing numbers.
- eq? behaves like == in Python for comparing two non-pairs (numbers, booleans, etc.). Otherwise, eq? behaves like is in Python.
- equal? compares pairs by determining if their cars are equal? and their cdrs are equal?(that is, they have the same contents). Otherwise, equal? behaves like eq?.

```
scm> (define a '(1 2 3))
a
scm> (= a a)
Error
scm> (equal? a '(1 2 3))
#t
scm> (eq? a '(1 2 3))
#f
scm> (define b a)
b
scm> (eq? a b)
#t
```

Questions

5.1 Write a function which takes two lists and concatenates them.

Notice that simply calling (cons a b) would not work because it will create a deep list.

(define (concat a b)

scm> (concat '(1 2 3) '(2 3 4))
(1 2 3 2 3 4)

5.2 Write a function that takes an element x and a non-negative integer n, and returns a list with x repeated n times.

(define (replicate x n)

scm> (replicate 5 3)
(5 5 5)

5.3 A **run-length encoding** is a method of compressing a sequence of letters. The list (a a a b a a a a) can be compressed to ((a 3) (b 1) (a 4)), where the compressed version of the sequence keeps track of how many letters appear consecutively.

Write a function that takes a compressed sequence and expands it into the original sequence. *Hint:* You may want to use concat and replicate.

(define (uncompress s)

```
scm> (uncompress '((a 1) (b 2) (c 3)))
(a b b c c c)
```

5.4 Write a function that takes a procedure and applies it to every element in a given list.

```
(define (map fn lst)
```

```
scm> (map (lambda (x) (* x x)) '(1 2 3))
(1 4 9)
```

5.5 Write a function that takes a procedure and applies to every element in a given nested list.

The result should be a nested list with the same structure as the input list, but with each element replaced by the result of applying the procedure to that element.

Use the built-in list? procedure to detect whether a value is a list.

(define (deep-map fn lst)

```
scm> (deep-map (lambda (x) (* x x)) '(1 2 3))
(1 4 9)
scm> (deep-map (lambda (x) (* x x)) '(1 ((4) 5) 9))
(1 ((16) 25) 81)
```

6 Extra Questions

6.1 Fill in the following to complete an abstract tree data type:

(define (make-tree label branches) (cons label branches))

(define (label tree)

(define (branches tree)

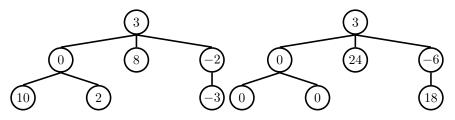
6.2 Using the abstract data type above, write a function that sums up the entries of a tree, assuming that the entries are all numbers.

Hint: you may want to use the map function you defined above, and also write a helper function for summing up the entries of a list.

(define (tree-sum tree)

6.3 Using the abstract data type above, write a function that creates a new tree where the entries are the product of the entries along the path to the root in the original tree.

Hint: you may want to write a helper function that keeps track of the current product.



(define (path-product-tree t)