1 More Running Time

Give the worst case and best case running time in $\Theta(\cdot)$ notation in terms of M and N.

(a) Assume that slam() $\in \Theta(1)$ and returns a boolean.

2 Recursive Running Time

For the following recursive functions, give the worst case and best case running time in $\Theta(\cdot)$ notation.

(a) Give the running time in terms of N.

(b) Give the running time for andwelcome (arr, 0, N) where N is the length of the input array arr.

```
public static void andwelcome(int[] arr, int low, int high) {
       System.out.print("[ ");
2
       for (int i = low; i < high; i += 1) {</pre>
            System.out.print("loyal ");
4
       System.out.println("]");
7
       if (high - low > 0) {
           double coin = Math.random();
8
           if (coin > 0.5) {
               andwelcome(arr, low, low + (high - low) / 2);
10
               andwelcome(arr, low, low + (high - low) / 2);
12
               andwelcome(arr, low + (high - low) / 2, high);
```

```
14 }
15 }
16 }
```

(c) Give the running time in terms of N.

```
public int tothe(int N) {
    if (N <= 1) {
      return N;
    }
    return tothe(N - 1) + tothe(N - 1);
}</pre>
```

(d) Give the running time in terms of N

```
public static void spacejam(int n) {
    if (n == 1) {
        return;
    }
    for (int i = 0; i < n; i += 1) {
            spacejam(n-1);
        }
    }
}</pre>
```

3 Hey you watchu gon do?

For each example below, there are two algorithms solving the same problem. Given the asymptotic runtimes for each, is one of the algorithms **guaranteed** to be faster? If so, which? And if neither is always faster, explain why. Assume the algorithms have very large input (so N is very large).

- (a) Algorithm 1: $\Theta(N)$, Algorithm 2: $\Theta(N^2)$
- (b) Algorithm 1: $\Omega(N)$, Algorithm 2: $\Omega(N^2)$
- (c) Algorithm 1: O(N), Algorithm 2: $O(N^2)$
- (d) Algorithm 1: $\Theta(N^2)$, Algorithm 2: $O(\log N)$
- (e) Algorithm 1: $O(N \log N)$, Algorithm 2: $\Omega(N \log N)$

Would your answers above change if we did not assume that N was very large?