

Recreation

Prove that for every acute angle $\alpha > 0$,

$$\tan \alpha + \cot \alpha \geq 2$$

CS61B Lecture #5: Simple Pointer Manipulation

Announcement

- **Today:** More pointer hacking.
- **Handing in labs and homework:** We'll be lenient about accepting late homework and labs for the first few. Just get it done: part of the point is getting to understand the tools involved. We will *not* accept submissions by email.

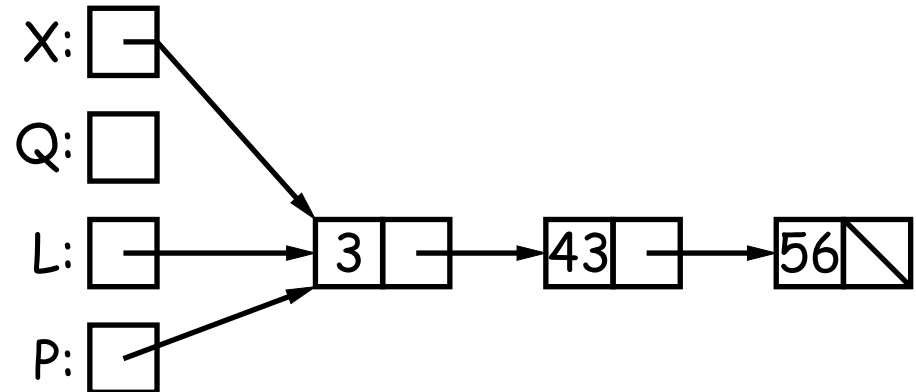
Destructive Incrementing

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}
```

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/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
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    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
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```

```
X = IntList.list(3, 43, 56);
/* IntList.list from HW #1 */
Q = dincrList(X, 2);
```



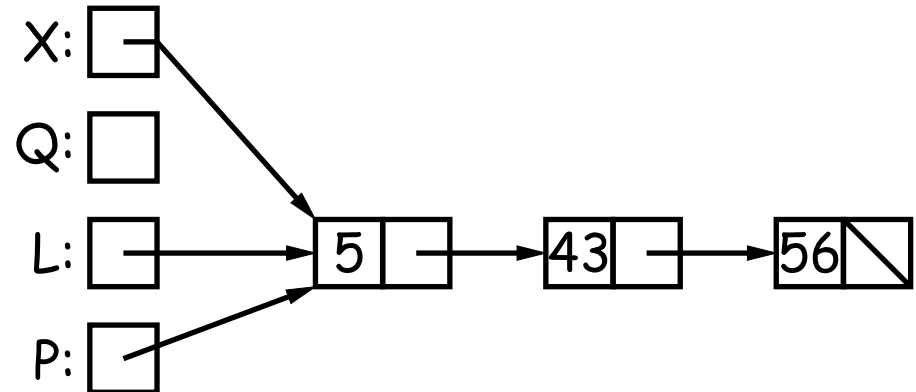
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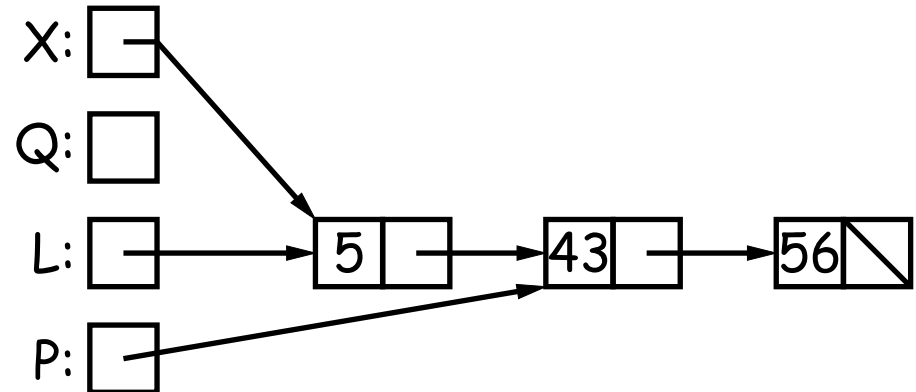
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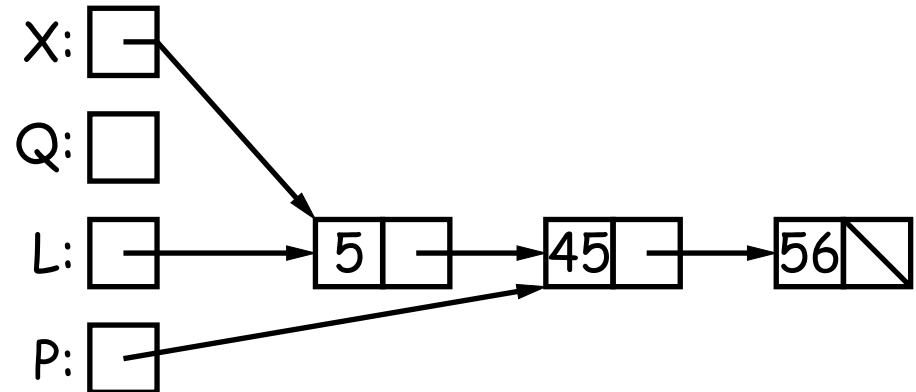
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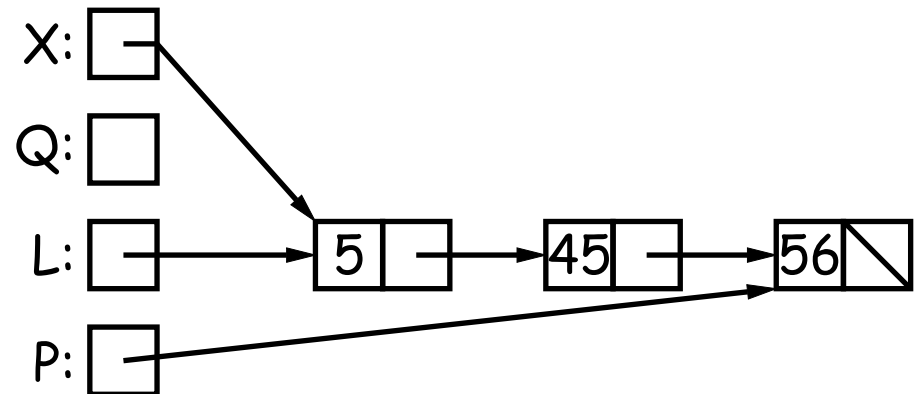
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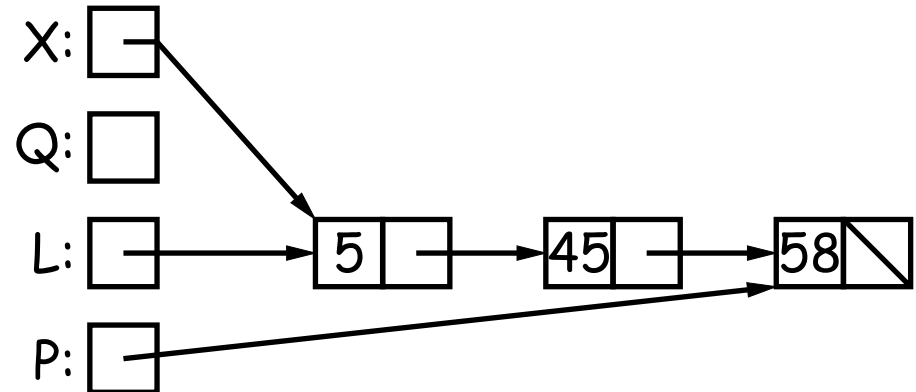
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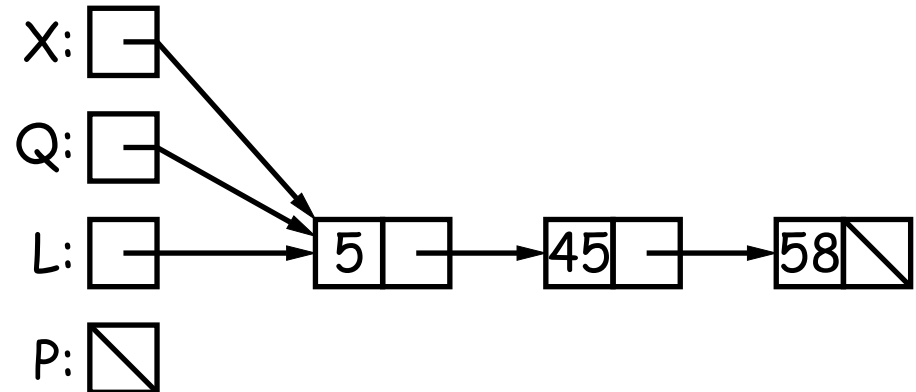
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    }
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        p.head += n;
    return L;
}
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```



Another Example: Non-destructive List Deletion

If L is the list $[2, 1, 2, 9, 2]$, we want `removeAll(L, 2)` to be the new list $[1, 9]$.

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else
        return /*( L with all x's removed (L != null, L.head!=x) )*/;
}
```

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static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return new IntList(L.head, removeAll(L.tail, x));
}
```

Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    for ( ; L != null; L = L.tail) {
        if (x == L.head)
            continue;
        else if (last == null)
            result = last = new IntList(L.head, null);
        else
            last = last.tail = new IntList(L.head, null);
    }
    return result;
}
```

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```

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```

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    IntList result, last;
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```
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```

```
    for ( ; L != null; L = L.tail) {
```

```
        if (x == L.head)
```

```
            continue;
```

```
        else if (last == null)
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```
            result = last = new IntList(L.head, null);
```

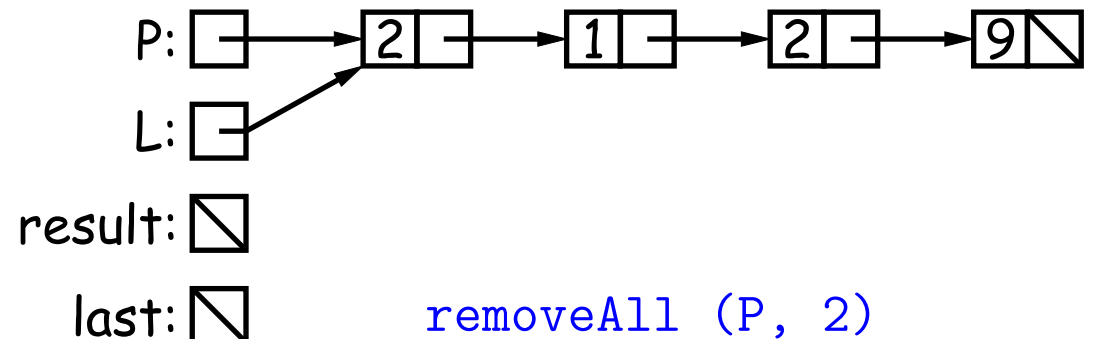
```
        else
```

```
            last = last.tail = new IntList(L.head, null);
```

```
    }
```

```
    return result;
```

```
}
```

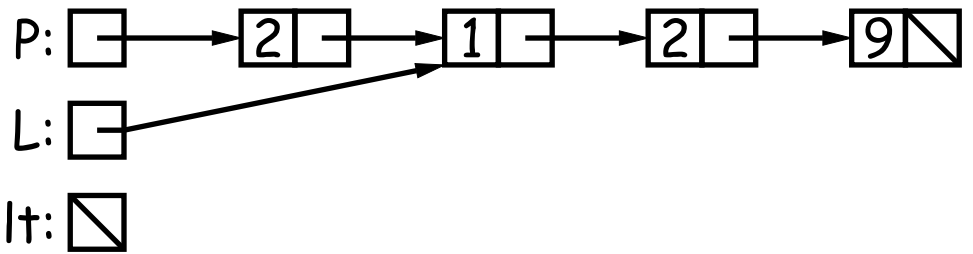


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}
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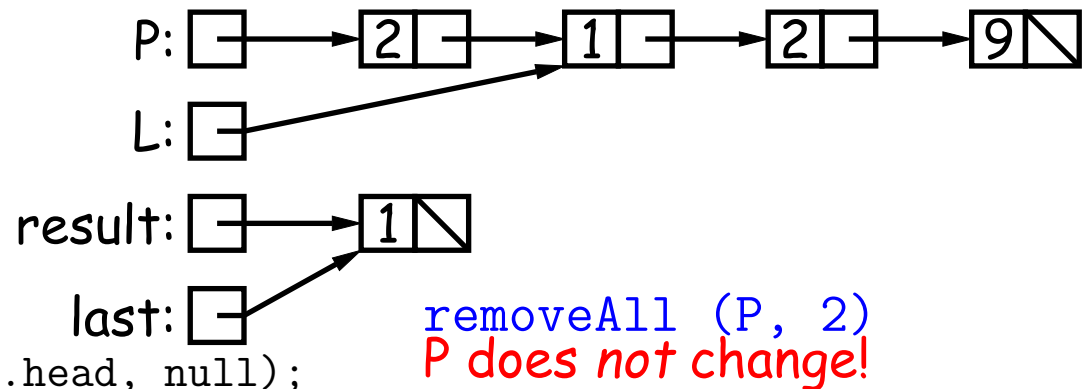
removeAll (P, 2)
P does not change!

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        else  
            last = last.tail = new IntList(L.head, null);  
    }  
    return result;  
}
```

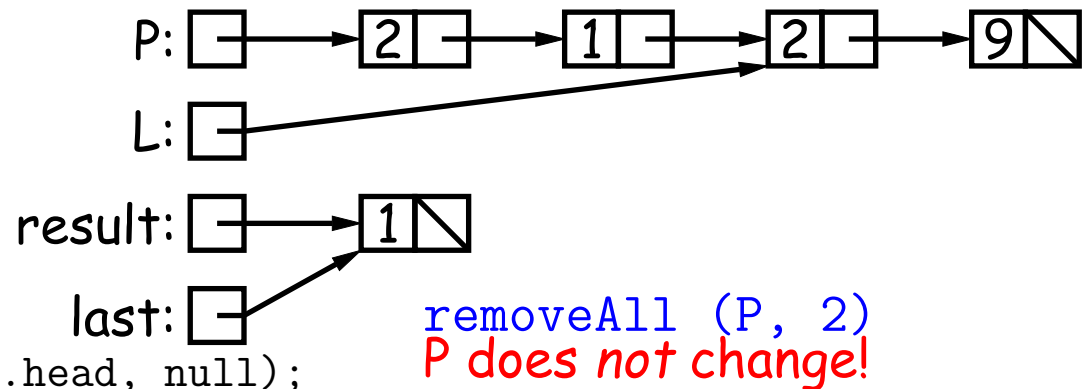


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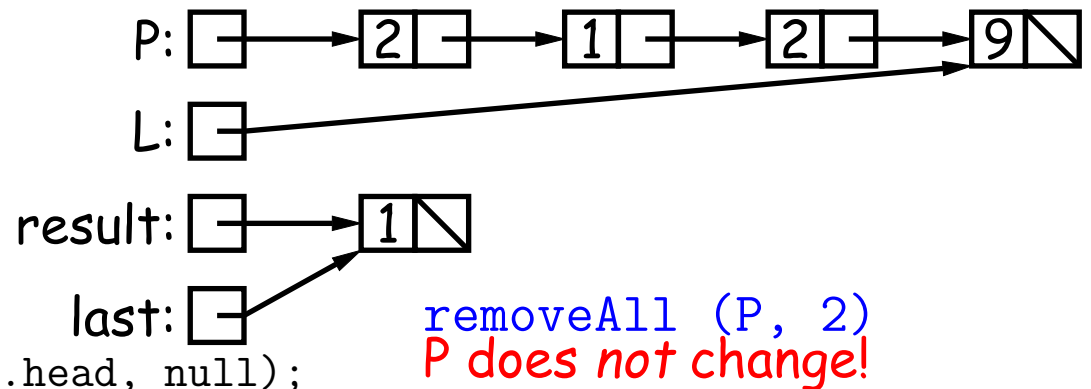
`removeAll (P, 2)`
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    }  
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}
```

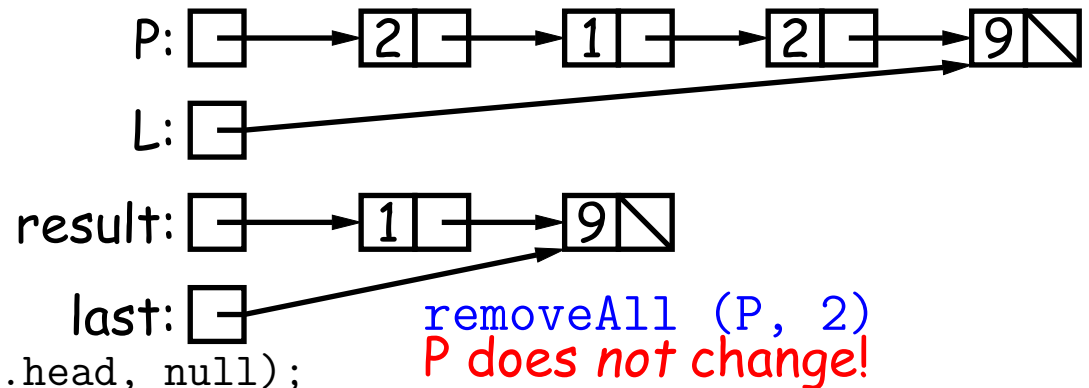


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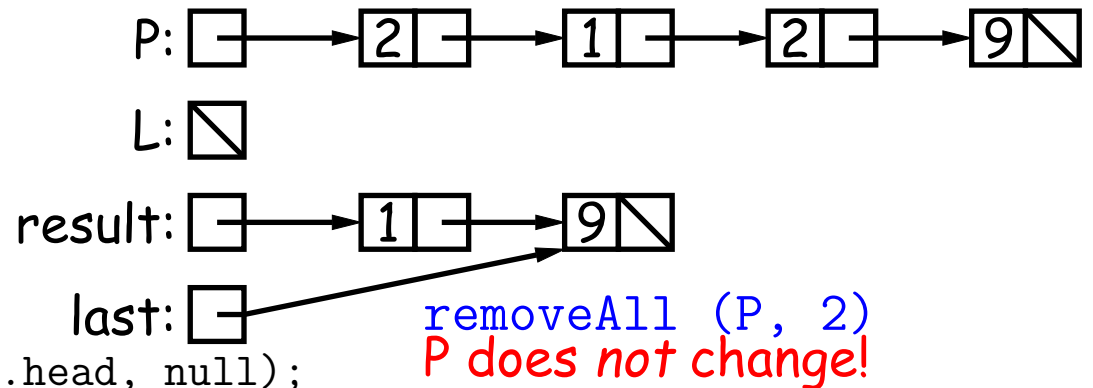


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Destructive Deletion

→ : Original

..... : after Q = dremoveAll (Q,1)

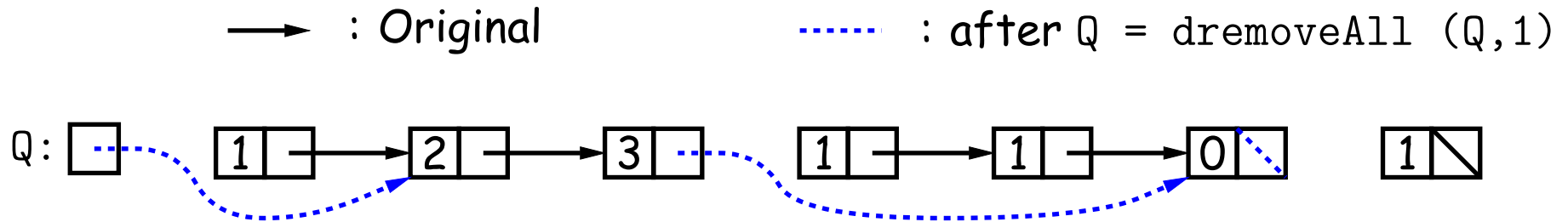


```
/** The list resulting from removing all instances of X from L.
```

```
 * The original list may be destroyed. */
```

```
static IntList dremoveAll(IntList L, int x) {  
    if (L == null)  
        return /*( null with all x's removed )*/;  
    else if (L.head == x)  
        return /*( L with all x's removed (L != null) )*/;  
    else {  
        /*{ Remove all x's from L's tail. }*/;  
        return L;  
    }  
}
```

Destructive Deletion



`/** The list resulting from removing all instances of X from L.`

`* The original list may be destroyed. */`

```

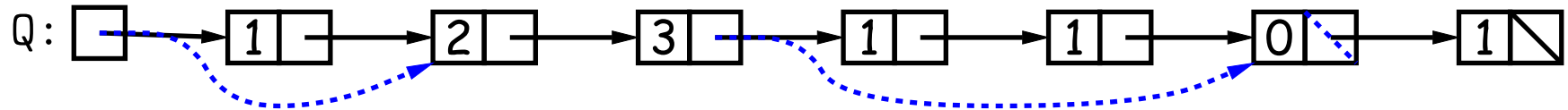
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```

Destructive Deletion

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/** The list resulting from removing all instances of X from L.
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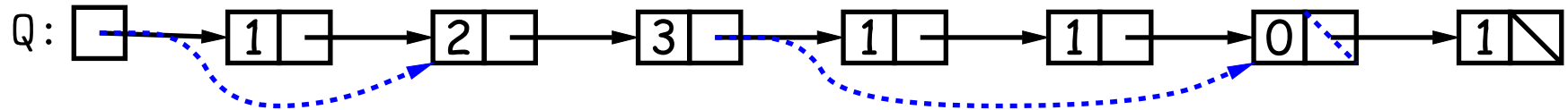
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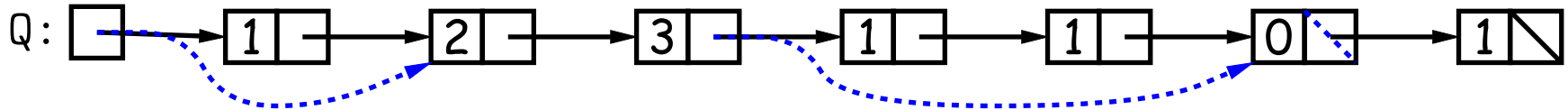
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/** The list resulting from removing all instances of X from L.
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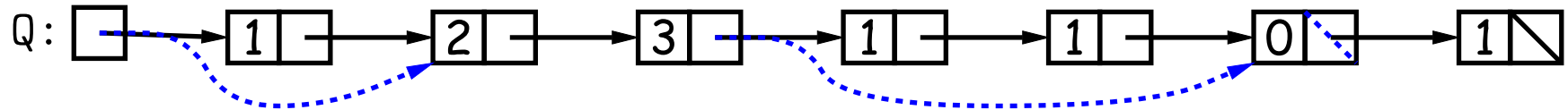
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Destructive Deletion

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/** The list resulting from removing all instances of X from L.
```

```
 * The original list may be destroyed. */
```

```
static IntList dremoveAll(IntList L, int x) {
```

```
    if (L == null)
```

```
        return
```

```
    else if (L.head == x)
```

```
        return dremoveAll(L.tail, x);
```

```
    else {
```

```
        /*{ Remove all x's from L's tail. }*/;
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```
        return L;
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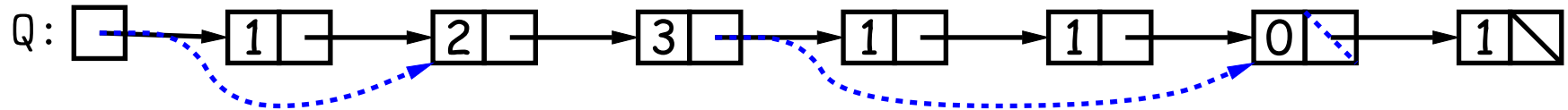
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```
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    if (L == null)
        return
    else if (L.head == x)
        return dremoveAll(L.tail, x);
    else {
        L.tail = dremoveAll(L.tail, x);
        return L;
    }
}
```

Iterative Destructive Deletion

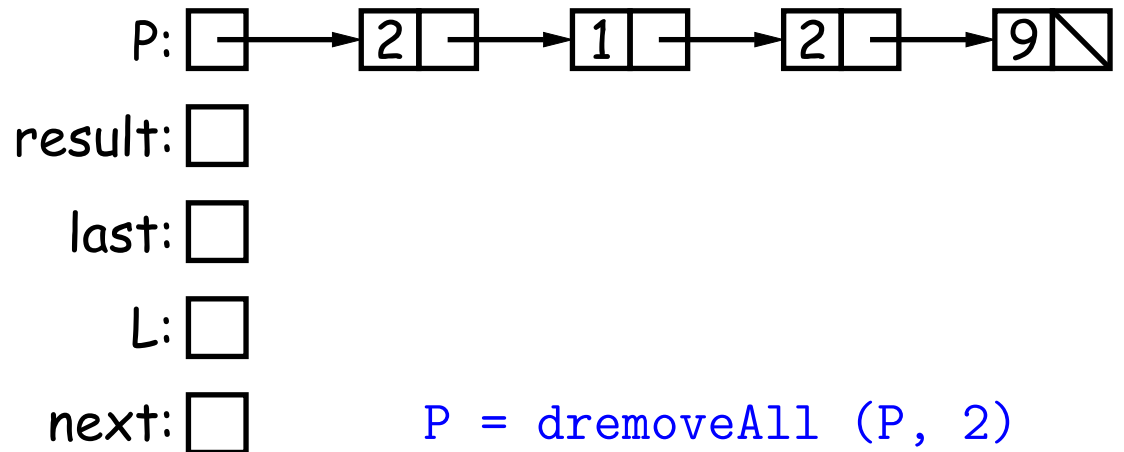
```
/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```

Iterative Destructive Deletion

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/** The list resulting from removing
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            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



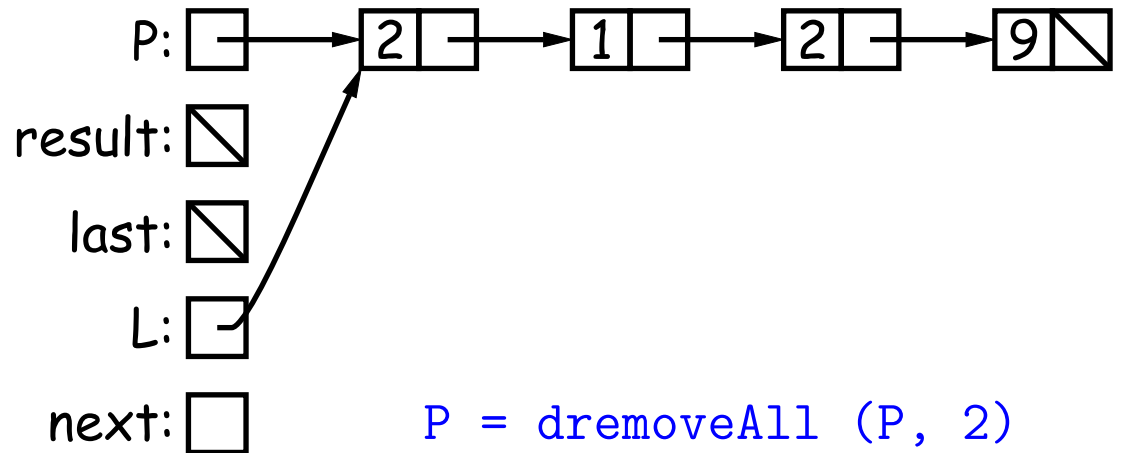
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                last = last.tail = L;
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        L = next;
    }
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```



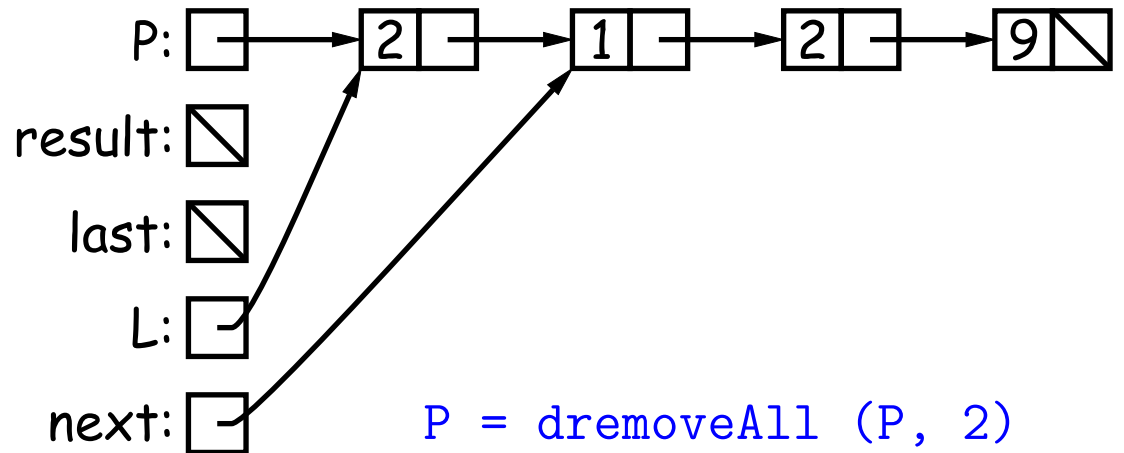
Iterative Destructive Deletion

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static IntList dremoveAll(IntList L,
                          int x) {

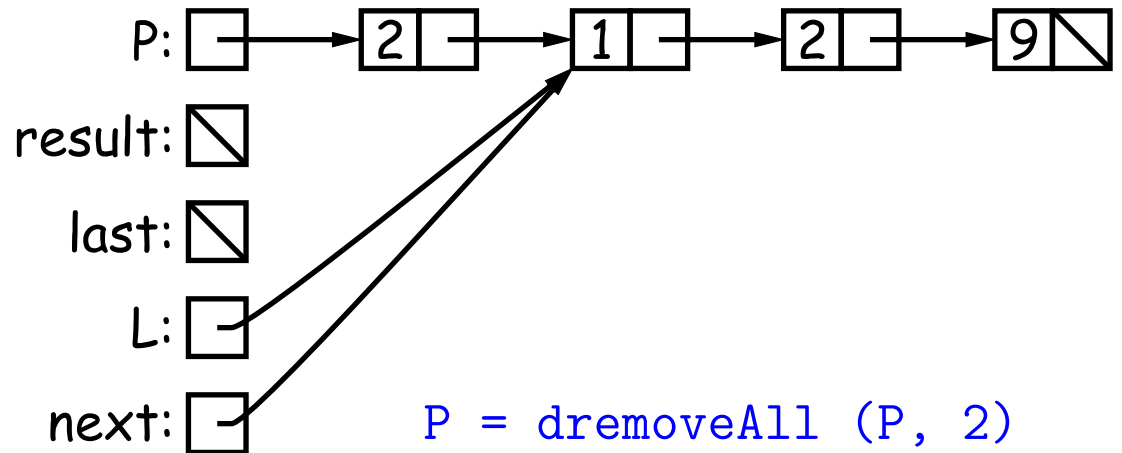
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



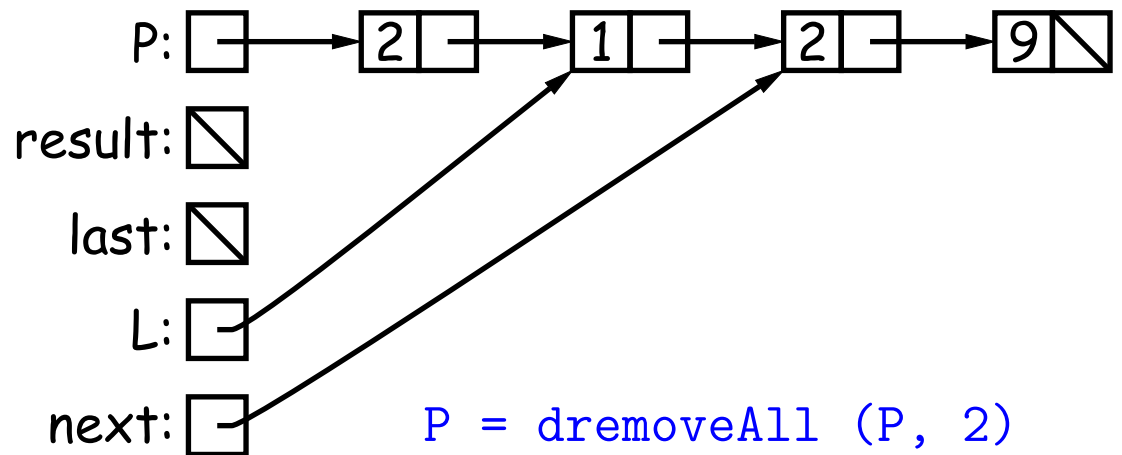
Iterative Destructive Deletion

```
/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



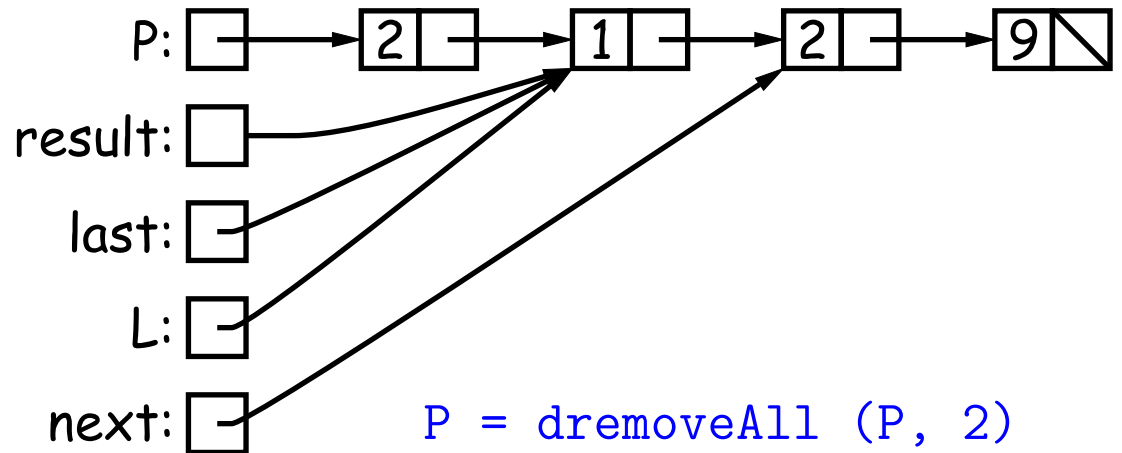
Iterative Destructive Deletion

```
/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



Iterative Destructive Deletion

```
/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```



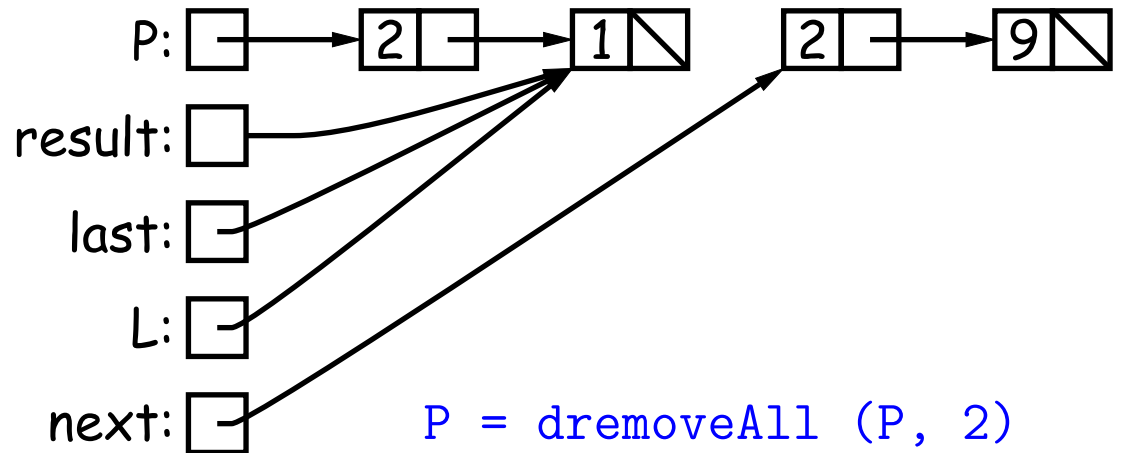
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



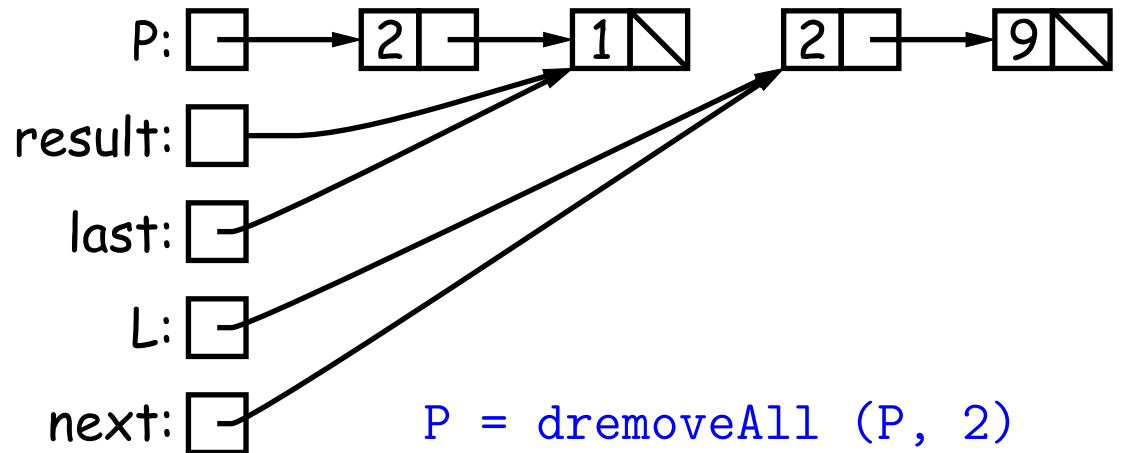
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



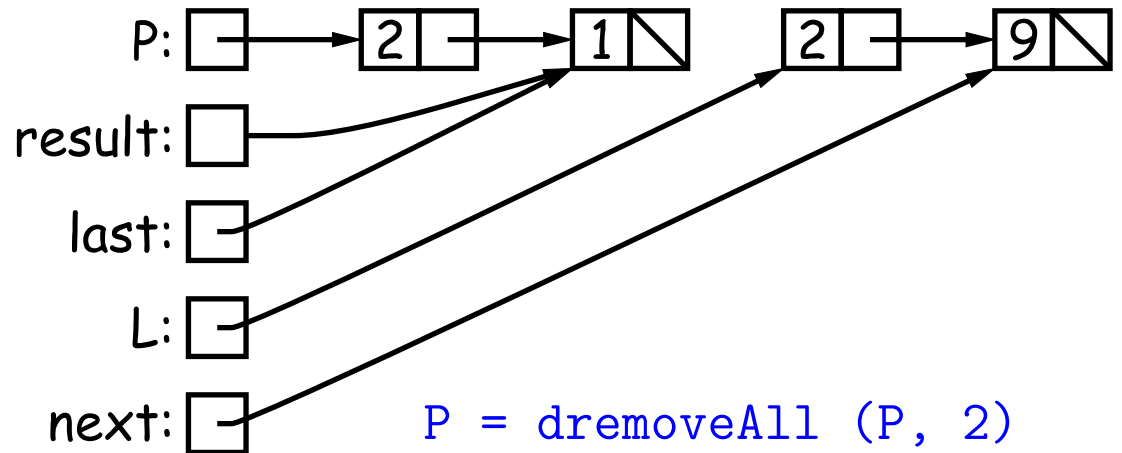
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



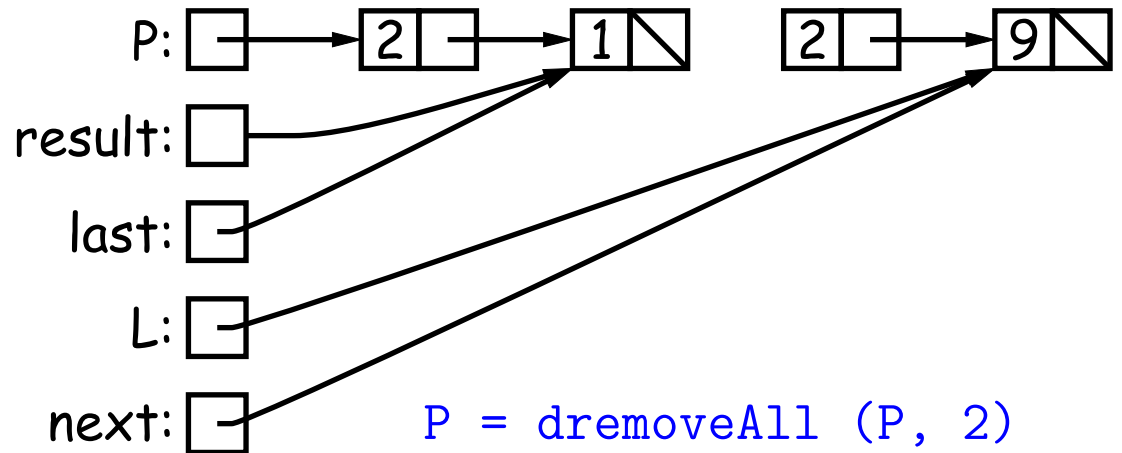
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



`P = dremoveAll (P, 2)`

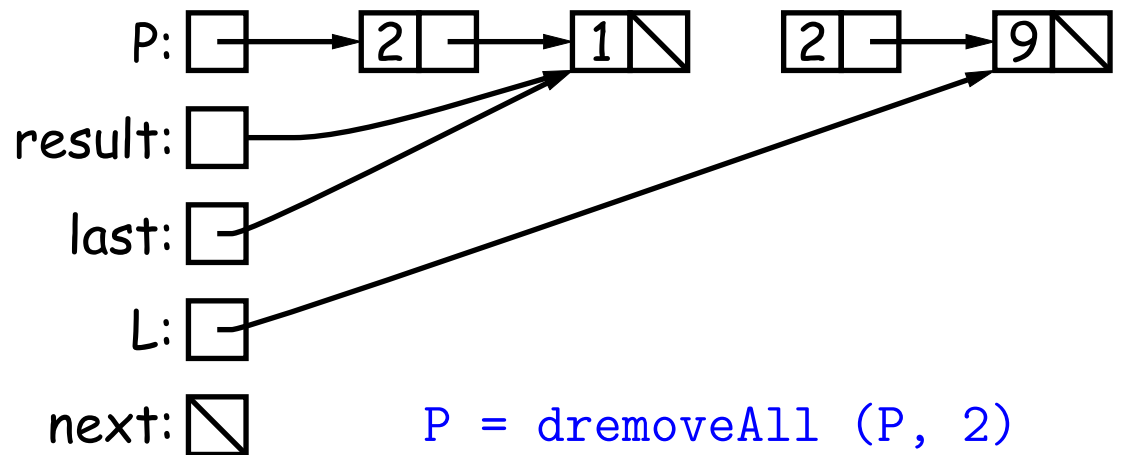
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



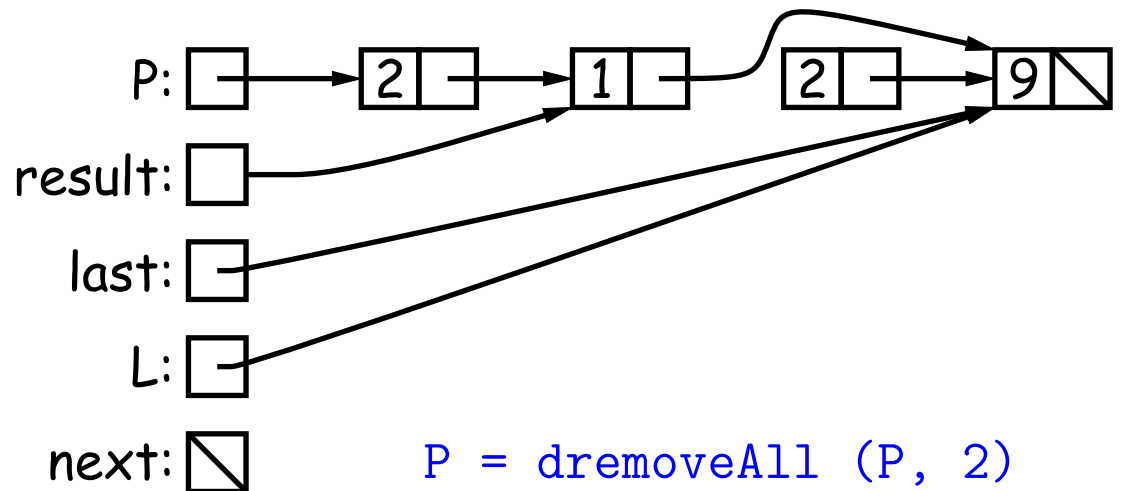
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



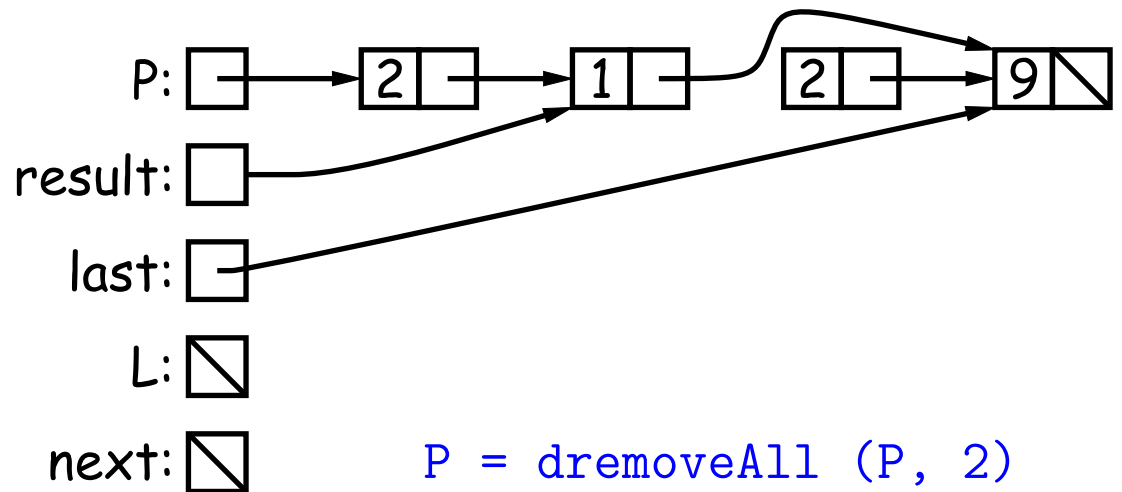
Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```



Iterative Destructive Deletion

```

/** The list resulting from removing
 * all X's from L destructively. */
static IntList dremoveAll(IntList L,
                          int x) {

    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}

```

