1 Fill in the Blanks

Fill in the following blanks related to min-heaps. Let N is the number of elements in the min-heap. For the entirety of this question, assume the elements in the min-heap are **distinct**.

1. removeMin has a best case runtime of _____ and a worst case runtime of _____.

2. insert has a best case runtime of _____ and a worst case runtime of _____.

3. A _____ or _____ traversal on a min-heap *may* output the elements in sorted order. Assume there are at least 3 elements in the min-heap.

4. The fourth smallest element in a min-heap with 1000 elements can appear in _____ places in the heap.

5. Given a min-heap with $2^N - 1$ distinct elements, for an element

   - to be on the second level it must be less than _____ element(s) and greater than _____ element(s).

   - to be on the bottommost level it must be less than _____ element(s) and greater than _____ element(s).

   Hint: A complete binary tree (with a full last-level) has $2^N - 1$ elements, with N being of levels.

2 Heap Mystery

We are given the following array representing a min-heap where each letter represents a **unique** number. Assume the root of the min-heap is at index zero, i.e. `A` is the root. Note that there is **no** significance of the alphabetical ordering, i.e. just because B precedes C in the alphabet, we do not know if B is less than or greater than C.

Array: [A, B, C, D, E, F, G]

Four unknown operations are then executed on the min-heap. An operation is either a `removeMin` or an `insert`. The resulting state of the min-heap is shown below.

Array: [A, E, B, D, X, F, G]

(a) Determine the operations executed and their appropriate order. The first operation has already been filled in for you!

    1. `removeMin()`

    2. _____

    3. _____

    4. _____

(b) Fill in the following comparisons with either >, <, or ? if unknown. We recommend considering which elements were compared to reach the final array.

    1. X _____ D

    2. X _____ C

    3. B _____ C

    4. G _____ X

3 Hashing Gone Crazy

For this question, use the following TA class for reference.

```java
public class TA {
    int charisma;
    String name;
    TA(String name, int charisma) {
        this.name = name;
        this.charisma = charisma;
    }
    @Override
    public boolean equals(Object o) {
        TA other = (TA) o;
        return other.name.charAt(0) == this.name.charAt(0);
    }
    @Override
    public int hashCode() {
        return charisma;
    }
}
```

Assume that the hashCode of a TA object returns charisma, and the equals method returns true if and only if two TA objects have the same first letter in their name.

Assume that the ECHashMap is a HashMap implemented with external chaining as depicted in lecture. The ECHashMap instance begins at size 4 and, for simplicity, does not resize. Draw the contents of map after the executing the insertions below:

```java
ECHashMap<TA, Integer> map = new ECHashMap<>();
TA sohum = new TA("Sohum", 10);
TA vivant = new TA("Vivant", 20);
map.put(sohum, 1);
map.put(vivant, 2);

vivant.charisma += 2;
map.put(vivant, 3);

sohum.name = "Vohum";
map.put(vivant, 4);

sohum.charisma += 2;
map.put(sohum, 5);

sohum.name = "Sohum";
TA shubha = new TA("Shubha", 24);
map.put(shubha, 6);
```

4   Buggy Hash

The following classes may contain a bug in one of its methods. Identify those errors and briefly explain why they are incorrect and in which situations would the bug cause problems.

```java
1    class Timezone {
2        String timeZone; // "PST", "EST" etc.
3        boolean dayLight;
4        String location;
5        ...
6        public  int currentTime() {
7            // return the current time in that time zone
8        }
9        public int hashCode() {
10           return currentTime();
11       }
12       public boolean equals(Object o) {
13           Timezone tz = (Timezone) o;
14           return tz.timeZone.equals(timeZone);
15       }
16   }
```

```java
1    class Course {
2        int courseCode;
3        int yearOffered;
4        String[] staff;
5        ...
6        public int hashCode() {
7            return yearOffered + courseCode;
8        }
9        public boolean equals(Object o) {
10           Course c = (Course) o;
11           return c.courseCode == courseCode;
12       }
13   }
```