Print your name: $\qquad$

Print your student ID: $\qquad$

You have 110 minutes. There are 7 questions of varying credit (100 points total).

| Question: | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Total |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Points: | 13 | 20 | 14 | 19 | 15 | 18 | 1 | 100 |

For questions with circular bubbles, you may select only one choice.

O Unselected option (completely unfilled)
Only one selected option (completely filled)
O Don't do this (it will be graded as incorrect)

For questions with square checkboxes, you may select one or more choices.
$\square$ You can select
$\square$ multiple squares
$\square$ (completely filled)

Anything you write outside the answer boxes or you eross-out will not be graded. If you write multiple answers, your answer is ambiguous, or the bubble/checkbox is not entirely filled in, we will grade the worst interpretation. For coding questions with blanks, you may write at most one statement per blank and you may not use more blanks than provided.

If an answer requires hex input, you must only use capitalized letters ( $0 x \operatorname{DEADBEEF}$ instead of 0xdeadbeef). For hex and binary, please include prefixes in your answers unless otherwise specified, and do not truncate any leading 0 's. For all other bases, do not add any prefixes or suffixes.

Write the statement below in the same handwriting you will use on the rest of the exam.
I have neither given nor received help on this exam (or quiz), and have rejected any attempt to cheat; if these answers are not my own work, I may be deducted up to $0 \times 01234567$ 89AB CDEF points.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

SIGN your name: $\qquad$

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The exam begins on the next page.

For Q1.1-Q1.3, convert the 8-bit binary Ob0100 1011 to decimal, treating it as...
Q1.1 (1 point) ...an unsigned integer.


Q1.2 (1 point) ...a two's complement integer.


Q1.3 (1 point) ...a sign-magnitude integer.


Q1.4 (2.5 points) What is the decimal value of $\mathbf{z}$ in the snippet of C code below?

```
int8_t x = 101;
int8_t y = 77;
int8_t z = x + y;
```



Q1.5 (3 points) Translate the following RISC-V instruction to hexadecimal: sw s0 10(s2)


For Q1.6-Q1.8, indicate the stage of CALL that...
Q1.6 (1.5 points) ...converts pseudoinstructions into equivalent instructions.
O Compiler
○ Assembler
○ Linker
○ Loader

Q1.7 (1.5 points) ...determines if functions are called with valid variable types.
O Compiler
O Assembler
○ Linker
O Loader

Q1.8 (1.5 points) ...jumps execution to the start of the program.
O Compiler
○
Assembler
○ Linker
O Loader
(C)

Recall in lab, we implemented some functions for a vector_t struct. In this question, we will add support for slicing a vector_t.

To do so, we've made some updates to the vector_t type from lab. You may assume that all necessary standard libraries are included.

```
typedef struct vector_t {
    // Number of elements in the vector; you may assume size > 0
    size_t size;
    // Pointer to the start of the vector
    int* data;
    // Number of child slices
    size_t num_slices;
    // Array of the vector's child slices, or NULL if num_slices == 0
    struct vector_t** slices;
    // true if the vector is a child slice of another vector, otherwise false
    bool is_slice;
} vector_t;
```

Useful C function prototypes:

```
void* malloc(size_t size);
void free(void *ptr);
void* calloc(size_t num_elements, size_t size);
void* realloc(void *ptr, size_t size);
size_t strlen(char* s);
char* strcpy(char* dest, char* src);
```

Implement the function vector_slice, which should return a slice of a vector_t at the given indices, with the following signature:

- vector_t* v: A pointer to the parent vector to create the slice from.
- int start_index: The beginning index of the new slice's data (inclusive)
- int end_index: The ending index of the new slice's data (exclusive). You may assume that end_index > start_index.
- Return value: A vector_t* representing data as described by start_index and end_index. A parent vector_t shares (portions of) its data array with all of its descendant slices.
For example:

```
// vec_a has the elements [0, 1, 2, 3, 4]
vector_t* vec_a = /* omitted */;
// vec_b should be of size 2 and have the elements [1, 2]
vector_t* vec_b = vector_slice(vec_a, 1, 3);
vec_b->data[1] = 10;
// At this point, vec_a should be [0, 1, 10, 3, 4]
// vec_b should be [1, 10]
```

```
1 vector_t* vector_slice(vector_t* v, int start_index, int end_index) {
2 vector_t* slice = 工 Q2.1 ;
3 if (slice == NULL) { allocation_failed(); }
5 slice->__ Q2.3 ;
6 slice-> __ Q2.4 ;
7 v->slices = _ Q2.5
8 if (v->slices == NULL) { allocation_failed(); }
9 v->slices[_] [_ Q2.6 % [
lurlor
```

The vector_t struct definition is repeated below for your convenience:

```
typedef struct vector_t {
    // Number of elements in the vector; you may assume size > 0
    size_t size;
    // Pointer to the start of the vector
    int* data;
    // Number of child slices
    size_t num_slices;
    // Array of the vector's child slices, or NULL if num_slices == 0
    struct vector_t** slices;
    // true if the vector is a child slice of another vector, otherwise false
    bool is_slice;
} vector_t;
```

To accommodate these changes to the vector_t type, we need to update the vector_delete function to properly free our new data structure. When a vector_t is deleted, all descendant slices of the vector_t should also be freed. You may assume that vector_delete is only called on a vector_t that is not a slice.


For the entirety of this question, assume that we are using an IEEE 754 standard floating-point representation with 16 bits: 1 sign bit, 7 exponent bits (with a standard bias of -63 ), and 8 significand bits.

For questions Q3.1 and Q3.2, convert the value to hexadecimal, using the floating-point representation above.

Q3.1 (2 points) -2.25

## 0x

Q3.2 (2 points) $1.75 \times 2^{-63}$

0x

For questions Q3.3 and Q3.4, what is the value of the floating-point number? Express your answer as $x \times 2^{y}$, where $x$ is a decimal such that $1 \leq|x|<2$ and $y$ is an integer. For NaN, write "NaN"; for positive infinity, write " $+\infty$ "; for negative infinity, write " $-\infty$ ".

Q3.3 (2 points) 0x7F9A


Q3.4 (2 points) 0x7000


Q3.5 (3 points) List all numbers $k$ in this floating-point representation such that the smallest floatingpoint number strictly greater than $k$ is exactly $2 k$. Express your answer as $x \times 2^{y}$, where $x$ is a decimal such that $1 \leq|x|<2$ and $y$ is an integer. If there are no such numbers, write "None".
$\square$
Q3.6 (3 points) Express, in hexadecimal, the smallest strictly positive representable number $k$ such that $k+1$ is also representable in this floating-point representation.
$\square$

The Jetidiah Propulsion Laboratory (JPL) is planning to race some vehicles around Jezero crater, including PersevRyance, CuriosEddy, and Bengenuity. They would like to write some RISC-V code to determine the best vehicle, and they need your help!
The race function, which has been correctly implemented for you, is defined as follows:

- Input in aO: id, the ID of a vehicle. You may assume that $0 \leq i d<200$.
- Output in a0: The distance traveled (in nanometers) by the vehicle in a sprint as an unsigned integer. You may assume that this value is less than $2^{32}$.

Implement best_vehicle as follows, using the race function:

- Input in aO: num_vehicles, the total number of vehicles being raced. The function should race vehicles with IDs between 0 and num_vehicles - 1 (inclusive).
You may assume that $0<$ num_vehicles $\leq 200$.
- Output in aO: The vehicle ID that traveled the farthest.
- best_vehicle should race the vehicles and return the ID of the vehicle that traveled the farthest. In case of a tie between multiple vehicles, return the lowest ID among those vehicles.

For example, given the following return values from the race function, best_vehicle(5) should race 5 vehicles (IDs $0,1,2,3$, and 4 ) and return 2, and best_vehicle( 2 ) should race 2 vehicles (IDs 0 and 1 ) and return 0 .

| ID | race(ID) |
| :--- | ---: |
| 0 | $600,000,000$ |
| 1 | 100,000 |
| 2 | $3,000,000,000$ |
| 3 | 1,564 |
| 4 | $3,000,000,000$ |


| 1 best_vehicle: |  |
| :---: | :---: |
| 2 | $\mathrm{Q} 4.1$ |
| 3 | sw $\qquad$ Q4. 2 |
| 4 | sw $\qquad$ |
| 5 | sw $\qquad$ |
| 6 | sw $\qquad$ Q4. 5 |
| 7 | mv s0 a0 |
| 8 | addi s1 x0 0 \# The best distance so far |
| 9 | addi s2 x0 0 \# The index of the best vehicle so far |
| 10 | addi to x0 0 \# The index of the vehicle being tested |
| 11 Loop: |  |
| 12 | Q4.6 |
| 13 | Q4.7 $0(\mathrm{sp})$ |
| 14 | $\ldots$ Q4.8 race |
| 15 | $0 \text { Q4.9 } 0(\mathrm{sp})$ |
| 16 | Q4.10 Continue |
| 17 | mv s1 a0 |
| 18 | mv s2 to |
| 19 Continue: |  |
| 20 | Q4.11 |
| 21 | Q4.12 Loop |
| 22 | ——_ |
| 23 | ```# Epilogue Omitted # You may assume that the epilogue has been correctly # implemented based on your prologue.``` |
| 24 |  |
| 25 |  |
| 26 | jr ra |
| 27 |  |

Consider the following circuit and timings:


Q5.1 (2.5 points) What is the minimum clock period, in nanoseconds, for the circuit above such that it will always exhibit well-defined behavior?


Q5.2 (2.5 points) What is the maximum hold time, in nanoseconds, for the circuit above such that it will always exhibit well-defined behavior?
$\square$

For the rest of this question, consider the updated circuit diagram and timings below. Subcircuits 1 and 2 are black-boxes that compute the Boolean expressions shown in the diagram. Regardless of your previous answers, assume the clock period is 80 ns , and for subcircuits 1 and 2 , their respective minimum and maximum combinational logic delays are equal. For example, if the input to subcircuit 1 changed at $t=0$ (and no other changes occur), then the output to subcircuit 1 will change at $t=13$ only.


Until this circuit settles at the correct input, it calculates two other Boolean expressions at the tunnel circ_out. Assume that register outputs are all 0 at $t=0$, and that there are no setup or hold time violations.

Q5.3 (2 points) Let $t_{1}$ be the first time that circ_out changes. What is $t_{1}$ in nanoseconds? Clarified during exam: $t_{1}$ is the first time that circ_out may change.


Q5.4 (2 points) Let $t_{2}$ be the second time that circ_out changes. What is $t_{2}$ in nanoseconds?


Q5.5 (2 points) What simplified Boolean expression does the circuit calculate while $0 \mathrm{~ns} \leq t<t_{1}$ ?


Q5.6 (2 points) What simplified Boolean expression does the circuit calculate while $t_{1} \leq t<t_{2}$ ?
$\square$
Q5.7 (2 points) What simplified Boolean expression does the circuit calculate while $t_{2} \leq t<80 \mathrm{~ns}$ ?
$\square$

Heracles has been tasked with yet another labour: taming the CS61Cerberus, the three-headed guard dog of Hades. Each head of CS61Cerberus has a favorite number (independent of the other heads), which is represented as an $n$-bit unsigned integer. In order to tame him, Heracles must determine the favorite numbers of all heads, by saying numbers and seeing how the heads respond.
Heracles can say any $n$-bit unsigned integer to any head, and the head will respond either true or false according to its rule and favorite number:

- The left head (Orion) receives its input and performs a bitwise OR on it with its favorite number. If the result is 0 , Orion returns true. Otherwise, Orion returns false.
- The middle head (Andy) receives its input and performs a bitwise AND on it with its favorite number. If the result is 0 , Andy returns true. Otherwise, Andy returns false.
- The right head (Luxor) receives its input and performs a bitwise XOR on it with its favorite number. If the result is 0 , Luxor returns true. Otherwise, Luxor returns false.

Q6.1 Write a function andy, which receives an unsigned integer as input and returns a bool according to how Andy would react to that integer, assuming $n=32$.

```
bool andy(uint32_t input) {
    // Andy's favorite number has been omitted.
    uint32_t andnum = /* omitted */;
    return __;
5}
```

Heracles writes three algorithms, solve_orion, solve_andy, and solve_luxor to find and return the favorite number of each head. Each of the three solver functions accepts one argument: a function that accepts a number and returns the response from the corresponding head.
Write solve_orion, solve_andy, and solve_luxor (for simplicity, your code only needs to work when $n=32$ ). Your solution must be asymptotically optimal for full credit.

Additionally, write the worst-case asymptotic time complexity of the optimal solver function in $\Theta$ notation with respect to $n$, the number of bits that the head accepts. The $\Theta$ bound must hold for all values of $n$, not just when $n=32$.
If no such algorithm exists, write "Impossible" in the code block, and leave the $\Theta$ bound blank.

```
Q6.2 uint32_t solve_orion(bool(*orion)(uint32_t)) \{
    // Your code here or Impossible
\}
```



```
Q6.3 uint32_t solve_andy (bool(*andy) (uint32_t)) \{ // Your code here or Impossible
\}
```



```
Q6. 4 uint32_t solve_luxor(bool(*luxor)(uint32_t)) \{ // Your code here or Impossible
\}
```



Everyone will receive credit for this question, even if you leave it blank.
Q7.1 (1 point) CS 61A defeated the Lambdanean Hydra in Fall 2022, CS 61B cleaned the Javaugean Stables in Spring 2023, and you've just tamed(?) CS61Cerberus. What are the 9 other labours of Heracles? Express your answer in emoji drawings.
$\square$
Q7.2 (0 points) Is there anything you want us to know?

