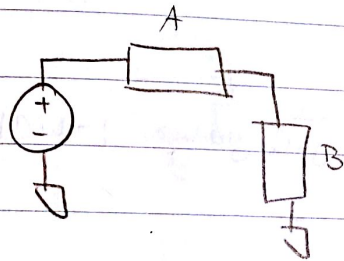


## Discussion 10

Options of things to go over:

- Solving for a transfer function
- Finding a 3dB point
- Resonance
- eigenvector/value review
- More filter design



-  $\frac{B}{A+B}$  large = pass,  $\frac{B}{A+B}$  small = stop

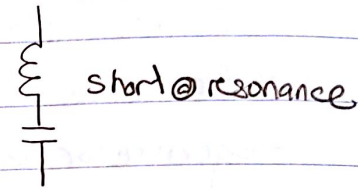
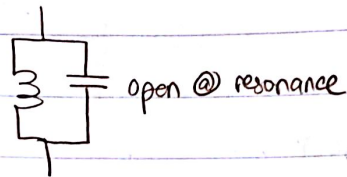
- Can choose values of B relative to something, usually freq. for filters

High pass, given a capacitor?

Lowpass, given an inductor?



What about band pass?  
want B acts different at a single freq.



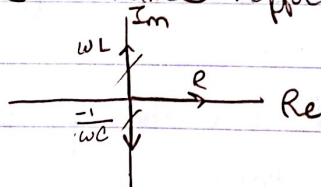
(Open & short are only for ideal cases)

Find impedance yourself:

$$\frac{1}{j\omega C + \frac{1}{j\omega L}} = \frac{j\omega L}{1 - \omega^2 LC}$$

$$\frac{1}{j\omega C + j\omega L} = 1 - \omega^2 LC$$

Where does resonance happen?



Where  $L$  &  $C$  are equal & the circuit becomes entirely real.

Solve for this point:

$$\omega L - \frac{1}{\omega C} = 0$$

$$\omega L = \frac{1}{\omega C}$$

$$\omega^2 = \frac{1}{LC}$$

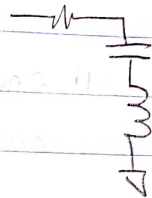
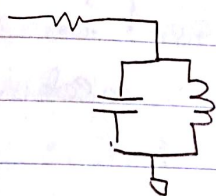
$$\omega = \frac{1}{\sqrt{LC}}$$

Plug in @  $\omega = \frac{1}{\sqrt{LC}}$

$$\frac{j\omega L}{1 - (\frac{1}{\sqrt{LC}})^2 LC} = \infty$$

$$1 - (\frac{1}{\sqrt{LC}})^2 LC = 0$$

So, given a  $\parallel LC$ , make a bandpass  
given a series LC, make a notch filter



You have seen all of these circuits on your HW, but this should give you the tools to quickly identify what a filter is doing on your own.

eigen matrices:

$$A = \begin{bmatrix} 10 & -9 \\ 4 & -2 \end{bmatrix} \quad \lambda = 4, 4$$

$$A = \begin{bmatrix} .8 & .3 \\ .2 & .7 \end{bmatrix} \quad \lambda = 1, \frac{1}{2}$$

Given a system:

$$x[k+1] = Ax[k]$$

↑  
some matrix

Draw the system



What if  $x_0$  is an eigenvector of  $A$ ?

$x_{k+1}$  is still eigenvector, but is scaled by eigenvalues each time.