

## Week of September 24, 2018

**Question 1** *Diffie–Hellman key exchange* (15 min)

Recall that in a Diffie-Hellman key exchange, there are values  $a$ ,  $b$ ,  $g$  and  $p$ . Alice computes  $g^a \bmod p$  and Bob computes  $g^b \bmod p$ .

- (a) Which of these values are publicly known and which must be kept private?
- (b) Eve can eavesdrop on everything sent between Alice and Bob, but can't change anything. Alice and Bob run Diffie-Hellman and have agreed on a shared symmetric key  $K$ . However, Bob accidentally sent his  $b$  to Alice in plain text. If Eve viewed all traffic since the beginning of the exchange, can she figure out what  $K$  is?
- (c) Mallory can not only view all Alice—Bob communications but also intercept and modify it. Alice and Bob perform Diffie-Hellman to agree on a shared symmetric key  $K$ . After the exchange, Bob gets the feeling something went wrong and calls Alice. He compares his value of  $K$  to Alice's and realizes that they are different. Explain what Mallory has done and what she can now do.

**Question 2 Perfect Forward Secrecy****(15 min)**

Alice (A) and Bob (B) want to communicate using some shared symmetric key encryption scheme. Consider the following key exchange protocols which can be used by A and B to agree upon a shared key,  $K_{ab}$ .

<b>El Gamal-Based Key Exchange</b>			<b>Diffe-Hellman Key Exchange</b>		
Message 1	<b>Protocol</b> $A \rightarrow B:$	$\{K_{ab}\}_{K_B^{pub}}$	Message 1	$A \rightarrow B:$	$g^a \text{ mod } p$
	Key exchanged		Message 2	$A \leftarrow B:$	$g^b \text{ mod } p$
				Key exchanged	$K_{ab} = g^{ab} \text{ mod } p$
Message 2	$A \leftarrow B:$	$\{secret1\}_{K_{ab}}$	Message 3	$A \leftarrow B:$	$\{secret1\}_{K_{ab}}$
Message 3	$A \rightarrow B:$	$\{secret2\}_{K_{ab}}$	Message 4	$A \rightarrow B:$	$\{secret2\}_{K_{ab}}$

Some additional details:

- $K_B^{pub}$  is Bob's long-lived public key.
- All messages are destroyed immediately after reading them.
- $K_{ab}$  and DH exponents  $a$  and  $b$  are destroyed once all messages are sent.

Eavesdropper Eve records all communications between Alice and Bob, but is unable to decrypt them. At some point in the future, Eve is lucky and manages to compromise Bob's computer.

(a) Is the confidentiality of Alice and Bob's prior El Gamal-based communication in jeopardy?

(b) What about Alice and Bob's Diffe-Hellman-based communication?



- (c) Is the attack in part (b) possible against the real RSA signature scheme (the one that includes the cryptographic hash function)? Why or why not? Assume the cryptographic hash function can be treated as a random oracle. (Do not worry if you do not know what this means).