Popa & Weaver Spring 2019

CS 161 Computer Security

Homework 2

Due: Sunday, 17 February 2019, at 11:59pm

Instructions. This homework is due Sunday, 17 February 2019, at 11:59pm. No late homeworks will be accepted unless you have prior accommodations from us. This assignment must be done on your own.

Create an EECS instructional class account if you have not already. To do so, visit https://inst.eecs.berkeley.edu/webacct/, click "Login using your Berkeley CalNet ID," then find the cs161 row and click "Get a new account." Be sure to take note of the account login and password, and log in to your instructional account.

Make sure you have a Gradescope account and are joined in this course. The homework must be submitted electronically via Gradescope (not by any other method). Your answer for each question, when submitted on Gradescope, should be written in the space provided on this PDF form. You may either use the LaTeX form provided to fill out your responses, use Adobe Acrobat to fill in this fillable PDF, or print this paper out and handwrite your solutions, but please make sure your responses do not overflow the box provided before submitting to ensure that you get full credit for your response.

Problem 1 True-or-False Questions

(45 points)

Answer each question. You don't need to justify or explain your answer.

- (a) Select if true : The Diffie-Hellman key exchange protocol protects against eavesdroppers but is vulnerable to man-in-the-middle attacks.
- (b) Select if true : Suppose there is a transmission error in a block B of ciphertext using CBC mode. This error propagates to every block in decryption, which means that the block B and every block after B cannot be decrypted correctly.
- (c) Select if true : The IV for CBC mode must be kept secret.
- (d) Select if true : The random number r in El Gamal must be kept secret.
- (e) Select if true : The best way to be confident in the cryptography that you use is to write your own implementation.
- (f) Select if true : (OPTIONAL) Alice and Bob share a symmetric key k. Alice sends Bob a message encrypted with k stating, "I owe you \$100", using AES-CBC encryption. Assuming AES is secure, we can be confident that an active attacker cannot tamper with this message; its integrity is protected.
- (g) Select if true : If the daily lottery numbers are truly random, then they can be used as the entropy for a one-time-pad since a one-time-pad needs to be random.
- (i) Select if true : (OPTIONAL) Alice and Bob share a secret symmetric key k which they use for calculating MACs. Alice sends the message M ="I, Alice, owe you, Bob, \$100" to Bob along with its message authentication code $MAC_k(M)$. Bob can present $(M, MAC_k(M))$ to a judge as proof that Alice owes him \$100 since a MAC provides integrity.

Problem 2 New Block Cipher Mode

(35 points)

Nick decides to invent a new block cipher mode, called NBC. It is defined as follows:

$$C_i = E_k(C_{i-1}) \oplus P_i$$
$$C_0 = IV$$

Here (P_1, \ldots, P_n) is the plaintext message, E_k is block cipher encryption with key k.

(a) Given (C_0, C_1, \ldots, C_n) and the key k, explain how to recover the original message (P_1, \ldots, P_n) .

(b) Is NBC encryption parallelizable? How about decryption? Provide a short justification for each.

(c) As we saw in discussion, CBC mode is vulnerable to a chosen plaintext attack when the IV which will be used to encrypt the message is known in advance. Is NBC vulnerable to the same issue?

(d) Say that Alice means to send the message (P_1, \ldots, P_n) to Bob using NBC mode. By accident, Alice typos and encrypts $(P_1 \oplus 1, \ldots, P_n)$ instead (i.e., she accidentally flips the last bit of the first block).

True or False: after Bob decrypts the resulting ciphertext, every block after the first is incorrect. Explain your answer.

(e) Alice encrypts the message (P_1, \ldots, P_5) . Unfortunately, the block C_3 of the ciphertext is lost in transmission, so that Bob receives $(C_0, C_1, C_2, C_4, C_5)$. Assuming that Bob knows that he is missing C_3 , which blocks of the original plaintext can Bob recover?

Select if the block is recoverable: P_1 P_2 P_3 P_4 P_5

Problem 3 Hashing Functions

(15 points)

Recall the definition of "one-way functions" and "collision-resistance" from lecture. We say a function f is one-way if given f(x) it is hard to find x' such that f(x') = f(x). Likewise, we say a function f is "collision-resistant" if it is hard to find two inputs x, y such that f(x) = f(y) but $x \neq y$. For each of the given functions H below, determine if it is one-way or not, and if it is collision-resistant or not. (State any assumptions that you make in the margin.)

- (a) Select if H(x) = x is: One-way Collision-resistant
- (b) Select if $H(x) = x \mod 2$ is: One-way Collision-resistant
- (c) Select if $H(x) = E_k(x)$ is: One-way Collision-resistant , where E_k is a ideally secure block cipher with a known and published key k.

Caltopia has two hospitals: Bear Hospital and Tree Hospital, each of which has a database of patient medical records that contain highly sensitive, confidential patient information. For both hospitals, each medical record is a tuple (p_i, m_i) , where p_i and m_i are strings that correspond to the patient's full name and medical record respectively; assume that every person in Caltopia has a unique full name. Thus, we can think of Bear Hospital's patient database as a list of tuples $(x_1, m_1), (x_2, m_2), ..., (x_n, m_n)$, where m_i is the medical information that Bear Hospital has for patient x_i . Similarly, we can think of Tree Hospital's database as a list $(y_1, m'_1), (y_2, m'_2), ..., (y_m, m'_m)$, where m'_i is a string that encodes the medical information that Tree Hospital has for the patient named y_i . Note that for a given patient, Tree Hospital and Bear Hospital might have different medical information.

The two hospitals want to collaborate on a way to identify which Caltopia citizens are patients at both hospitals. However, due to privacy laws, the two hospitals cannot share any plaintext information about patients (including their names) unless both hospitals know *a priori* that a patient has used both hospitals.

Thus, the two hospitals decide to build a system that will allow them to identify common patients of both hospitals. They enlist the help of Lady Olenna, who provides them with a trusted, third-party server S, which they will use to discover the names of patients who use both hospitals. Specifically, Bear Hospital will take some information from its patient database and transform it into a list $(x_1^*), (x_2^*), ..., (x_n^*)$ (where (x_i^*) is somehow derived from x_i (the patient's full name) and upload it to S. Similarly, Tree Hospital will take information from its patient database, transform it into a list $(y_1^*), (y_2^*), ..., (y_m^*)$, and upload this transformed list to S. Finally, S will compute a set of tuples $P = (i, j) : x_i = y_j$ of all pairs (i, j) such that $x_i^* = y_j^*$ and send P to both Bear Hospital and Tree Hospital. The two hospitals can then take their respective indices from the tuples in P to identify patients who use both hospitals.

We want to ensure three requirements with the above scheme: (1) if $x_i = y_j$, then $(i,j) \in P$, (2) if $x_i \neq y_j$, then it is very unlikely that $(i,j) \in P$, (3) even if Eve (an attacker) compromises S, she cannot learn the name of any patient at either hospital or the medical information for any patient. For this question, assume that Eve is a passive attacker who cannot conduct Chosen Plaintext Attacks; however, she does know the names of everyone in Caltopia, and there are citizens whose full names are a unique length.

Your solution can use the cryptographic hash SHA-256 and/or AES with one of the three block cipher encryption modes discussed in class; keep in mind that Eve can also compute SHA-256 hashes and use AES with any block cipher mode. You can assume that Bear Hospital and Tree Hospital share a key k that is not known to anyone else. You cannot use public-key cryptography or modular arithmetic.

(a) In the collaboration scheme described above, how should Bear Hospital compute x_i^* (as a function of x_i)? How should Tree Hospital compute y_i^* (as a function of y_i)? Specifically, your solution should define a function F that Bear Hospital will use to

transform x_i into x_i^* , and if relevant, a function G that Tree Hospital will use to transform y_i into y_i^* .

- (b) Explain why requirement (1) is met by your solution, i.e., explain why it is guaranteed that if $x_i = y_j$, then $x_i^* = y_j^*$ will hold. Explain your answer in one or two sentences.
- (c) Explain why requirement (2) is met by your solution, i.e., if $x_i \neq y_j$, explain why it is unlikely that $x_i^* = y_j^*$. Explain your answer in one or two sentences.
- (d) Explain why requirement (3) is met by your solution, i.e., if S is compromised by Eve, then the information known to S does not let Eve learn any patient information (neither the names of patients at a particular hospital nor the medical history for any patient). Explain your answer in one or two sentences.

Problem 5 El Gamal Encryption

(30 points)

Recall the definition of El Gamal encryption from lecture. Bob publishes a large prime p, and an integer g with 1 < g < p-1. To generate a key, Bob chooses a random value $0 \le b \le p-2$, and computes $B = g^b \mod p$. Bob's public key is B, and his private key is b. If Alice wants to send a message m to Bob, she begins by generating a random r such that $0 \le r \le p-2$, and creates the ciphertext $(c_1, c_2) = (g^r \mod p, m \cdot B^r \mod p)$. To decrypt the ciphertext, Bob calculates $c_1^{-b}c_2 \equiv m \pmod p$.

Note: As mentioned in the notes, this simplified El Gamal scheme is actually not semantically secure.

- (a) Suppose you intercept a ciphertext (c_1, c_2) that Alice has encrypted for Bob, which is the encryption for some message m. Construct a ciphertext (c'_1, c'_2) which is the encryption of 2m. Answer Format: $(\underline{\hspace{1cm}}, \underline{\hspace{1cm}})$
- (b) Suppose you intercept two ciphertexts (c_1, c_2) and (c'_1, c'_2) that Alice has encrypted for Bob. Assume they are encryptions of some unknown messages m_1 and m_2 . Construct a ciphertext (c''_1, c''_2) which is a valid El Gamal encryption of the message $m_1 \cdot m_2 \mod p$. Answer Format: (_____, ____)
- (c) Consider a new scheme where the value r is not generated randomly every time. Instead, Alice begins by randomly generating an initial value r_0 , and then simply incrementing r_0 by 1 every time she needs to encrypt another message. Is the resulting encryption scheme IND-CPA?

Problem 6 Feedback (0 points)

Optionally, feel free to include feedback. What's the single thing we could do to make the class better? Or, what did you find most difficult or confusing from lectures or the rest of class, and what would you like to see explained better? If you have feedback, submit your comments as your answer to Q6.