

July 3rd: Cryptography I

Question 1 *Block Cipher Potpourri*

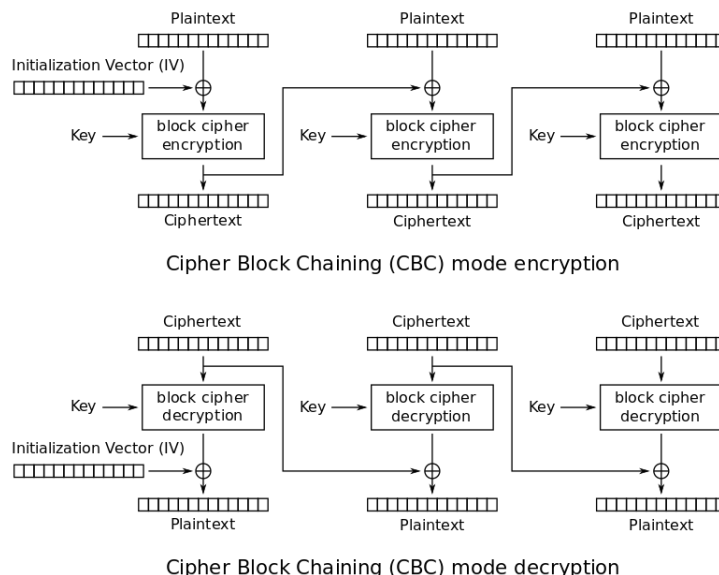
(20 min)

Answer the following short questions about block ciphers.

1. Are block ciphers IND-CPA?
2. Which of these are good possible sources of entropy for key generation for a block cipher?
 - The computer's clock time (assumed in seconds)
 - The Parent Process ID \oplus my Process ID \oplus time
 - Hardware noise generator
 - Hardware noise generator \oplus time
 - 101010101... \oplus Hardware noise generator
3. Why does a block cipher need to be a permutation?
4. Show that a random OTP (one-time pad) is IND-KPA.

Question 2 *Block cipher security and modes of operation* (20 min)

As a reminder, the cipher-block chaining (CBC) mode of operation works like this:



The output of the encryption is the ciphertext concatenated with the IV that was used.

1. Does the initialization vector (IV) have to be non-repeating? Why?
2. Is a non-repeating IV enough? Imagine you sequentially picked IVs from a list of non-repeating, but publicly-known, numbers, e.g., *A Million Random Digits with 100,000 Normal Deviates* (RAND, 1955).

Say Alice encrypts the one-block long message m_1 with initialization vector IV_1 to get C_1 and encrypts m_2 using IV_2 to get C_2 . She gives these to Mallory and challenges her to tell which C came from which m .

Mallory knows that Alice's next IV will be IV_3 , and can ask Alice to encrypt messages for her (a *chosen plaintext attack*). Can Mallory distinguish the two ciphertexts?

Question 3 *PRNGs and stream ciphers***(20 min)**

R is a pseudo-random number generator (PRNG), and f is a function that takes as input 128-bit seed s , an integer n , and an integer m , and outputs the m^{th} (inclusive) through m^{th} (exclusive) pseudo-random bits produced by R when it is seeded with seed s :

$$f(s, m, n) = R(s)[m : n]$$

1. Use f to make a secure symmetric-key encryption scheme. That is, define the key generation algorithm, the encryption algorithm, and the decryption algorithm. You have access to 128 bits of entropy. You may also store some small amount of state.
2. Explain how using a block cipher in counter (CTR) mode is similar to the scenario / scheme described above.