

Ambiguity, Precedence, Associativity & Top-Down Parsing

Lecture 9-10
(From slides by G. Necula & R. Bodik)

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Administrivia

- Please let me know if there are continued problems with being able to see other people's stuff.
- *Preliminary* run of test data against any projects handed in by midnight Wednesday.
 - Not final data sets, but may give you an indication.
 - You can submit early and often!
 - Will not test again until midnight Friday.

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Remaining Issues

- How do we *find* a derivation of s ?
- *Ambiguity*: what if there is *more than one parse tree* (interpretation) for some string s ?
- *Errors*: what if there is *no parse tree* for some string s ?
- Given a derivation, how do we *construct an abstract syntax tree* from it?

Today, we'll look at the first two.

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Ambiguity

- Grammar

$$E \rightarrow E + E \mid E * E \mid (E) \mid \text{int}$$

- Strings

$\text{int} + \text{int} + \text{int}$

$\text{int} * \text{int} + \text{int}$

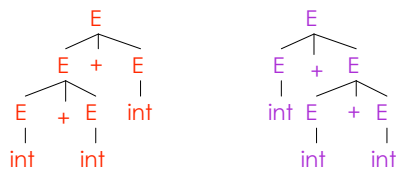
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Ambiguity. Example

The string $\text{int} + \text{int} + \text{int}$ has two parse trees



$+$ is left-associative

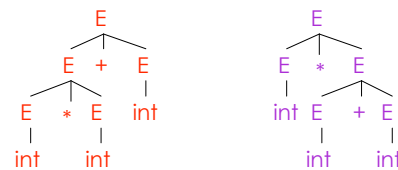
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Ambiguity. Example

The string $\text{int} * \text{int} + \text{int}$ has two parse trees



$*$ has higher precedence than $+$

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Ambiguity (Cont.)

- A grammar is *ambiguous* if it has more than one parse tree for some string
 - Equivalently, there is more than one rightmost or leftmost derivation for some string
- Ambiguity is *bad*
 - Leaves meaning of some programs ill-defined
- Ambiguity is *common* in programming languages
 - Arithmetic expressions
 - IF-THEN-ELSE

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Dealing with Ambiguity

- There are several ways to handle ambiguity
- Most direct method is to rewrite the grammar unambiguously

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * \text{int} \mid \text{int} \mid (E)$$
- Enforces precedence of $*$ over $+$
- Enforces left-associativity of $+$ and $*$

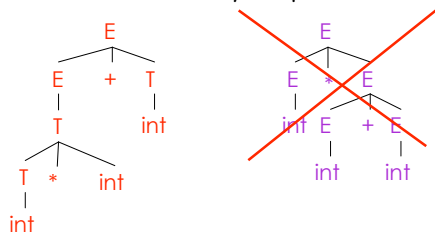
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Ambiguity. Example

The $\text{int} * \text{int} + \text{int}$ has only one parse tree now



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Ambiguity: The Dangling Else

- Consider the grammar

$$E \rightarrow \text{if } E \text{ then } E$$

$$| \text{if } E \text{ then } E \text{ else } E$$

$$| \text{OTHER}$$
- This grammar is also ambiguous

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The Dangling Else: Example

- The expression

$$\text{if } E_1 \text{ then if } E_2 \text{ then } E_3 \text{ else } E_4$$
 has two parse trees



- Typically we want the second form

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The Dangling Else: A Fix

- *else* matches the closest unmatched *then*
- We can describe this in the grammar (distinguish between matched and unmatched "then")

$$E \rightarrow MIF \quad /* \text{ all then are matched } */$$

$$| UIF \quad /* \text{ some then are unmatched } */$$

$$MIF \rightarrow \text{if } E \text{ then } MIF \text{ else } MIF$$

$$| \text{OTHER}$$

$$UIF \rightarrow \text{if } E \text{ then } E$$

$$| \text{if } E \text{ then } MIF \text{ else } UIF$$

- Describes the same set of strings

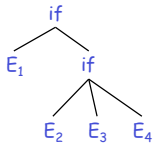
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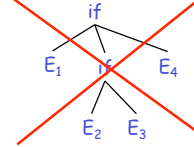
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The Dangling Else: Example Revisited

- The expression `if E1 then if E2 then E3 else E4`



- A valid parse tree (for a **UIF**)



- Not valid because the **then** expression is not a **MIF**

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Ambiguity

- Impossible to convert automatically an ambiguous grammar to an unambiguous one
- Used with care, ambiguity can simplify the grammar
 - Sometimes allows more natural definitions
 - But we need disambiguation mechanisms
- Instead of rewriting the grammar
 - Use the more natural (ambiguous) grammar
 - Along with disambiguating declarations
- Most tools allow *precedence and associativity declarations* to disambiguate grammars
- Examples ...

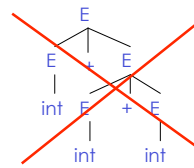
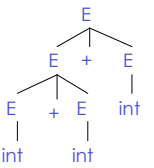
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Associativity Declarations

- Consider the grammar $E \rightarrow E + E \mid \text{int}$
- Ambiguous: two parse trees of `int + int + int`



- Left-associativity declaration: `%left '+'`

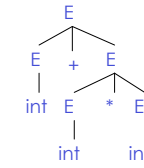
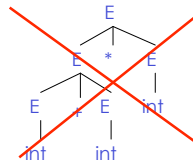
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Precedence Declarations

- Consider the grammar $E \rightarrow E + E \mid E * E \mid \text{int}$
- And the string `int + int * int`



- Precedence declarations: `%left '+'`
`%left '*'`

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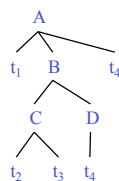
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How It's Done I: Intro to Top-Down Parsing

- Terminals are seen in order of appearance in the token stream:

$t_1 \ t_2 \ t_3 \ t_4 \ t_5$

- The parse tree is constructed
 - From the top
 - From left to right
- ... As for leftmost derivation



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Top-down Depth-First Parsing

- Consider the grammar

$$E \rightarrow T + E \mid T$$

$$T \rightarrow (E) \mid \text{int} \mid \text{int} * T$$
- Token stream is: `int * int`
- Start with top-level non-terminal **E**
- Try the rules for **E** in order

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Depth-First Parsing. Example $int * int$

- Start with start symbol E
- Try $E \rightarrow T + E$ $T + E$
- Then try a rule for $T \rightarrow (E)$ $(E) + E$
 - But (\neq input int); backtrack to $T + E$
- Try $T \rightarrow int$. Token matches. $int + E$
 - But $+ \neq$ input $*$; back to $T + E$
- Try $T \rightarrow int * T$ $int * T + E$
 - But (skipping some steps) $+ \text{ can't be matched}$
- Must backtrack to E

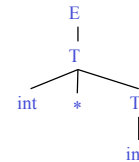
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Depth-First Parsing. Example $int * int$

- Try $E \rightarrow T$
- Follow same steps as before for T
 - And succeed with $T \rightarrow int * T$ and $T \rightarrow int$
 - With the following parse tree



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Depth-First Parsing

- Parsing: given a string of tokens $t_1 t_2 \dots t_n$, find a leftmost derivation (and thus, parse tree)
- Depth-first parsing: Beginning with start symbol, try each production exhaustively on leftmost non-terminal in current sentential form and recurse.

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Depth-First Parsing of $t_1 t_2 \dots t_n$

- At a given moment, have sentential form that looks like this: $t_1 t_2 \dots t_k A \dots$, $0 \leq k \leq n$
- Initially, $k=0$ and $A \dots$ is just start symbol
- Try a production for A : if $A \rightarrow BC$ is a production, the new form is $t_1 t_2 \dots t_k B C \dots$
- Backtrack when leading terminals aren't prefix of $t_1 t_2 \dots t_n$ and try another production
- Stop when no more non-terminals and terminals all matched (accept) or no more productions left (reject)

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When Depth-First Doesn't Work Well

- Consider productions $S \rightarrow S \alpha \mid \alpha$:
 - In the process of parsing S we try the above rules
 - Applied consistently in this order, get infinite loop
 - Could re-order productions, but search will have lots of backtracking and general rule for ordering is complex
- Problem here is *left-recursive grammar*: one that has a non-terminal S

$$S \rightarrow^* S \alpha \text{ for some } \alpha$$

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Elimination of Left Recursion

- Consider the left-recursive grammar

$$S \rightarrow S \alpha \mid \beta$$
- S generates all strings starting with a β and followed by a number of α
- Can rewrite using right-recursion

$$S \rightarrow \beta S'$$

$$S' \rightarrow \alpha S' \mid \epsilon$$

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Elimination of left Recursion. Example

- Consider the grammar
 $S \rightarrow 1 \mid S 0$ ($\beta = 1$ and $\alpha = 0$)

can be rewritten as

$$\begin{aligned} S &\rightarrow 1 S' \\ S' &\rightarrow 0 S' \mid \epsilon \end{aligned}$$

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More Elimination of Left Recursion

- In general

$$S \rightarrow S \alpha_1 \mid \dots \mid S \alpha_n \mid \beta_1 \mid \dots \mid \beta_m$$

- All strings derived from S start with one of β_1, \dots, β_m and continue with several instances of $\alpha_1, \dots, \alpha_n$

- Rewrite as

$$\begin{aligned} S &\rightarrow \beta_1 S' \mid \dots \mid \beta_m S' \\ S' &\rightarrow \alpha_1 S' \mid \dots \mid \alpha_n S' \mid \epsilon \end{aligned}$$

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General Left Recursion

- The grammar

$$\begin{aligned} S &\rightarrow A \alpha \mid \delta & (1) \\ A &\rightarrow S \beta & (2) \end{aligned}$$

is also left-recursive because

$$S \rightarrow^+ S \beta \alpha$$

- This left recursion can also be eliminated by first substituting (2) into (1)
- There is a general algorithm (e.g. Aho, Sethi, Ullman §4.3)
- But personally, I'd just do this by hand.

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An Alternative Approach

- Instead of reordering or rewriting grammar, can use *top-down breadth-first search*.

$$S \rightarrow S a \mid a \quad \text{String: } aaa$$

S
 $S a$ ~~a~~ (string not all matched)
 $S a a$ ~~$a a$~~
 $S a a a$ $a a a$

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Summary of Top-Down Parsing So Far

- Simple and general parsing strategy
 - Left recursion must be eliminated first
 - ... but that can be done automatically
 - Or can use breadth-first search
- But backtracking (depth-first) or maintaining list of possible sentential forms (breadth-first) can make it slow
- Often, though, we can avoid both ...

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Predictive Parsers

- Modification of depth-first parsing in which parser "predicts" which production to use
 - By looking at the next few tokens
 - No backtracking
- Predictive parsers accept LL(k) grammars
 - L means "left-to-right" scan of input
 - L means "leftmost derivation"
 - k means "predict based on k tokens of lookahead"
- In practice, LL(1) is used

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LL(1) Languages

- Previously, for each non-terminal and input token there may be a choice of production
- LL(k) means that for each non-terminal and k tokens, there is only one production that could lead to success

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Recursive Descent: Grammar as Program

- In recursive descent, we think of a grammar as a program.
- Each non-terminal is turned into a procedure
- Each right-hand side transliterated into part of the procedure body for its non-terminal
- First, define
 - `next()` current token of input
 - `scan(t)` check that `next()=t` (else ERROR), and then read new token.

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Recursive Descent: Example

$P \rightarrow S \$$ $S \rightarrow T S'$
 $S' \rightarrow + S \mid \epsilon$ $T \rightarrow \text{int} \mid (S)$ ($\$$ = end marker)

```
def P(): S(); scan('$')
def S(): T(); S'()
def S'():
    if next() == '+': scan('+'); S()
    elif next() in ['(', '$']: pass
    else: ERROR
def T():
    if next() == 'int': scan('int')
    elif next() == '(': scan('('); S(); scan('(')
    else: ERROR
```

*But where do tests
come from?*

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Predicting Right-hand Sides

- The if-tests are conditions by which parser *predicts* which right-hand side to use.
- In our example, used only next symbol (LL(1)); but could use more.
- Can be specified as a 2D table
 - One dimension for current non-terminal to expand
 - One dimension for next token
 - A table entry contains one production

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But First: Left Factoring

- With the grammar
$$E \rightarrow T + E \mid T$$
$$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$$
- Impossible to predict because
 - For T two productions start with `int`
 - For E it is not clear how to predict
- A grammar must be *left-factored* before use for predictive parsing

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Left-Factoring Example

- Starting with the grammar
$$E \rightarrow T + E \mid T$$
$$T \rightarrow \text{int} \mid \text{int} * T \mid (E)$$
- Factor out common prefixes of productions
$$E \rightarrow T X$$
$$X \rightarrow + E \mid \epsilon$$
$$T \rightarrow (E) \mid \text{int} Y$$
$$Y \rightarrow * T \mid \epsilon$$

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LL(1) Parsing Table Example

- Left-factored grammar

$$E \rightarrow TX \quad X \rightarrow + E \mid \epsilon$$

$$T \rightarrow (E) \mid int Y \quad Y \rightarrow * T \mid \epsilon$$

- The LL(1) parsing table (\$ is a special end marker):

	int	*	+	()	\$
T	int Y			(E)		
E	TX			TX		
X			+ E			ϵ
Y		* T	ϵ			ϵ

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LL(1) Parsing Table Example (Cont.)

- Consider the [E, int] entry
 - "When current non-terminal is E and next input is int, use production $E \rightarrow TX$ "
 - This production can generate an int in the first place
- Consider the [Y, +] entry
 - "When current non-terminal is Y and current token is +, get rid of Y"
 - We'll see later why this is so

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LL(1) Parsing Tables. Errors

- Blank entries indicate error situations
 - Consider the [E,*] entry
 - "There is no way to derive a string starting with * from non-terminal E"

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Using Parsing Tables

- Method similar to recursive descent, except
 - For first non-terminal S
 - We look at the next token a
 - And choose the production shown at [S,a]
- We use a stack to keep track of pending non-terminals
- We reject when we encounter an error state
- We accept when we encounter end-of-input

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LL(1) Parsing Algorithm

initialize stack = <S,\$>

repeat

 case stack of

 <X, rest> : if $T[X, \text{next}()] = Y_1 \dots Y_n$;
 stack \leftarrow <Y₁... Y_n rest>;
 else: error ();

 <t, rest> : scan (t); stack \leftarrow <rest>;

until stack == < >

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LL(1) Parsing Example

Stack	Input	Action
E \$	int * int \$	TX
TX \$	int * int \$	int Y
int Y X \$	int * int \$	terminal
Y X \$	* int \$	* T
* TX \$	* int \$	terminal
TX \$	int \$	int Y
int Y X \$	int \$	terminal
Y X \$	\$	ϵ
X \$	\$	ϵ
\$	\$	ACCEPT

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Constructing Parsing Tables

- LL(1) languages are those definable by a parsing table for the LL(1) algorithm
- No table entry can be multiply defined
- Once we have the table
 - Can create table-driver or recursive-descent parser
 - The parsing algorithms are simple and fast
 - No backtracking is necessary
- We want to generate parsing tables from CFG

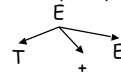
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Top-Down Parsing. Review

- Top-down parsing expands a parse tree from the start symbol to the leaves
 - Always expand the leftmost non-terminal



int * int + int

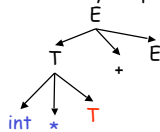
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int * int + int

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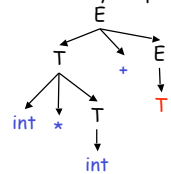
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- The leaves at any point form a string $\beta A \gamma$
 - β contains only terminals
 - The input string is $\beta b \delta$
 - The prefix β matches
 - The next token is b

Top-Down Parsing. Review

- Top-down parsing expands a parse tree from the start symbol to the leaves
 - Always expand the leftmost non-terminal



int * int + int

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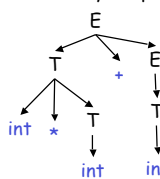
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- The leaves at any point form a string $\beta A \gamma$
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Top-Down Parsing. Review

- Top-down parsing expands a parse tree from the start symbol to the leaves
 - Always expand the leftmost non-terminal



int * int + int

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- The leaves at any point form a string $\beta A \gamma$
 - β contains only terminals
 - The input string is $\beta b \delta$
 - The prefix β matches
 - The next token is b

Constructing Predictive Parsing Tables

- Consider the state $S \rightarrow * \beta A \gamma$
 - With b the next token
 - Trying to match $\beta b \delta$

There are two possibilities:

1. b belongs to an expansion of A
 - Any $A \rightarrow \alpha$ can be used if b can start a string derived from α
 - In this case we say that $b \in \text{First}(\alpha)$

Or...

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Constructing Predictive Parsing Tables (Cont.)

- b** does not belong to an expansion of **A**
 - The expansion of **A** is empty and **b** belongs to an expansion of γ (e.g., $b\omega$)
 - Means that **b** can appear after **A** in a derivation of the form $S \rightarrow^* \beta A b \omega$
 - We say that $b \in \text{Follow}(A)$ in this case
 - What productions can we use in this case?
 - Any $A \rightarrow \alpha$ can be used if α can expand to ϵ
 - We say that $\epsilon \in \text{First}(A)$ in this case

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Summary of Definitions

- For $b \in T$, the set of terminals; α a sequence of terminal & non-terminal symbols, S the start symbol, $A \in N$, the set of non-terminals:
 - $\text{FIRST}(\alpha) \subseteq T \cup \{\epsilon\}$
 - $b \in \text{FIRST}(\alpha)$ iff $\alpha \rightarrow^* b \dots$
 - $\epsilon \in \text{FIRST}(\alpha)$ iff $\alpha \rightarrow^* \epsilon$
 - $\text{FOLLOW}(A) \subseteq T$
 - $b \in \text{FOLLOW}(A)$ iff $S \rightarrow^* \dots A b \dots$

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Computing First Sets

Definition $\text{First}(X) = \{ b \mid X \rightarrow^* b\alpha \} \cup \{ \epsilon \mid X \rightarrow^* \epsilon \}$,
 X any grammar symbol.

- $\text{First}(b) = \{ b \}$
- For all productions $X \rightarrow A_1 \dots A_n$
 - Add $\text{First}(A_1) - \{\epsilon\}$ to $\text{First}(X)$. Stop if $\epsilon \notin \text{First}(A_1)$
 - Add $\text{First}(A_2) - \{\epsilon\}$ to $\text{First}(X)$. Stop if $\epsilon \notin \text{First}(A_2)$
 - ...
 - Add $\text{First}(A_n) - \{\epsilon\}$ to $\text{First}(X)$. Stop if $\epsilon \notin \text{First}(A_n)$
 - Add ϵ to $\text{First}(X)$

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Computing First Sets, Contd.

- That takes care of single-symbol case.
- In general:

$$\begin{aligned} \text{FIRST}(X_1 X_2 \dots X_k) = & \text{FIRST}(X_1) \\ & \cup \text{FIRST}(X_2) \text{ if } \epsilon \in \text{FIRST}(X_1) \\ & \cup \dots \\ & \cup \text{FIRST}(X_k) \text{ if } \epsilon \in \text{FIRST}(X_1 X_2 \dots X_{k-1}) \\ & - \{ \epsilon \} \text{ unless } \epsilon \in \text{FIRST}(X_i) \quad \forall i \end{aligned}$$

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First Sets. Example

- For the grammar

$E \rightarrow TX$	$X \rightarrow +E \mid \epsilon$
$T \rightarrow (E) \mid \text{int } Y$	$Y \rightarrow *T \mid \epsilon$
- First sets

$\text{First}(() = \{ (\}$	$\text{First}(T) = \{ \text{int}, (\}$
$\text{First}() = \{ \}$	$\text{First}(E) = \{ \text{int}, (\}$
$\text{First}(\text{int}) = \{ \text{int} \}$	$\text{First}(X) = \{ +, \epsilon \}$
$\text{First}(+) = \{ + \}$	$\text{First}(Y) = \{ *, \epsilon \}$
$\text{First}(*) = \{ * \}$	

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Computing Follow Sets

Definition $\text{Follow}(X) = \{ b \mid S \rightarrow^* \beta X b \omega \}$

- Compute the **First** sets for all non-terminals first
- Add $\$$ to $\text{Follow}(S)$ (if S is the start non-terminal)
- For all productions $Y \rightarrow \dots X A_1 \dots A_n$
 - Add $\text{First}(A_1) - \{\epsilon\}$ to $\text{Follow}(X)$. Stop if $\epsilon \notin \text{First}(A_1)$
 - Add $\text{First}(A_2) - \{\epsilon\}$ to $\text{Follow}(X)$. Stop if $\epsilon \notin \text{First}(A_2)$
 - ...
 - Add $\text{First}(A_n) - \{\epsilon\}$ to $\text{Follow}(X)$. Stop if $\epsilon \notin \text{First}(A_n)$
 - Add $\text{Follow}(Y)$ to $\text{Follow}(X)$

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Follow Sets. Example

- For the grammar
 $E \rightarrow TX$ $X \rightarrow +E \mid \epsilon$
 $T \rightarrow (E) \mid \text{int } Y$ $Y \rightarrow *T \mid \epsilon$
- Follow sets
Follow(E) = { }, \$}
Follow(X) = { \$,) }
Follow(Y) = { +, , , \$ }
Follow(T) = { +, , , \$ }

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Constructing LL(1) Parsing Tables

- Construct a parsing table T for CFG G
- For each production $A \rightarrow \alpha$ in G do:
 - For each terminal $b \in \text{First}(\alpha)$ do
 - $T[A, b] = \alpha$
 - If $\alpha \rightarrow^* \epsilon$, for each $b \in \text{Follow}(A)$ do
 - $T[A, b] = \alpha$

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Constructing LL(1) Tables. Example

- For the grammar
 $E \rightarrow TX$ $X \rightarrow +E \mid \epsilon$
 $T \rightarrow (E) \mid \text{int } Y$ $Y \rightarrow *T \mid \epsilon$
- Where in the line of Y do we put $Y \rightarrow *T$?
 - In the lines of $\text{First}(*T) = \{ * \}$
- Where in the line of Y do we put $Y \rightarrow \epsilon$?
 - In the lines of $\text{Follow}(Y) = \{ \$, +, , \}$

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Notes on LL(1) Parsing Tables

- If any entry is multiply defined then G is not LL(1)
 - If G is ambiguous
 - If G is left recursive
 - If G is not left-factored
 - And in other cases as well
- Most programming language grammars are not LL(1)
- There are tools that build LL(1) tables

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Recursive Descent for Real

- So far, have presented a purist view.
- In fact, use of recursive descent makes life simpler in many ways if we "cheat" a bit.
- Here's how you *really* handle left recursion in recursive descent, for $S \rightarrow SA \mid R$:

```
def S():
    R()
    while next() ∈ FIRST(A):
        A()
```
- It's a program: all kinds of shortcuts possible.

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Review

- For some grammars there is a simple parsing strategy
 - Predictive parsing (LL(1))
 - Once you build the LL(1) table, you can write the parser by hand
- Next: a more powerful parsing strategy for grammars that are not LL(1)

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