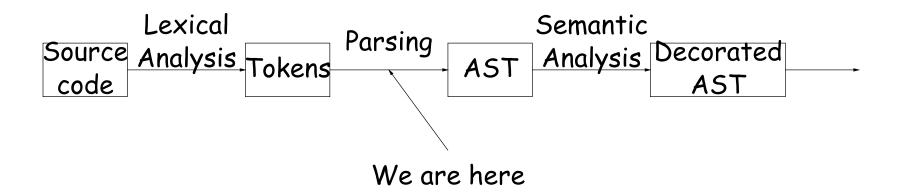
# Lecture 4: Parsing

#### Administrivia

- If you do not have a group, please post a request on Piazzza (see the "Form project teams..." item. Be sure to update your post if you find one.
- We will assign orphans to groups randomly in a few days.
- Programming Contest coming up: 29 Sept. Watch for details.

# A Glance at the Map



#### Review: BNF

- BNF is another pattern-matching language;
- Alphabet typically set of tokens, such as from lexical analysis, referred to as terminal symbols or terminals.
- Matching rules have form:

$$X: \alpha_1\alpha_2\cdots\alpha_n,$$

where X is from a set of nonterminal symbols (or nonterminals or meta-variables),  $n \geq 0$ , and each  $\alpha_i$  is a terminal or nonterminal symbol.

- ullet For emphasis, may write  $X:\ \epsilon$  when n=0.
- Read  $X: \alpha_1\alpha_2\cdots\alpha_n$ , as

"An X may be formed from the concatenation of an  $lpha_1$  ,  $lpha_2$  ,  $\ldots$  ,  $\alpha_n$ ."

- Designate one nonterminal as the start symbol.
- Set of all matching rules is a context-free grammar.

#### Review: Derivations

- String (of terminals) T is in the language described by grammar G,  $(T \in L(G))$  if there is a derivation of T from the start symbol of G.
- Derivation of  $T = \tau_1 \cdots \tau_k$  from nonterminal A is sequence of sentential forms:

$$A \Rightarrow \alpha_{11}\alpha_{12} \dots \Rightarrow \alpha_{21}\alpha_{22} \dots \Rightarrow \dots \Rightarrow \tau_1 \dots \tau_k$$

where each  $\alpha_{ij}$  is a terminal or nonterminal symbol.

• We say that

$$\alpha_1 \cdots \alpha_{m-1} B \alpha_{m+1} \cdots \alpha_n \Rightarrow \alpha_1 \cdots \alpha_{m-1} \beta_1 \cdots \beta_p \alpha_{m+1} \cdots \alpha_n$$

if  $B: \beta_1 \cdots \beta_p$  is a production. ( $1 \le m \le n$ ).

- If  $\Phi$  and  $\Phi'$  are sentential forms, then  $\Phi_1 \stackrel{*}{\Longrightarrow} \Phi_2$  means that 0 or more  $\Rightarrow$  steps turns  $\Phi_1$  into  $\Phi_2$ .  $\Phi_1 \stackrel{+}{\Longrightarrow} \Phi_2$  means 1 or more  $\Rightarrow$  steps does it.
- So if S is start symbol of G, then  $T \in L(G)$  iff  $S \stackrel{+}{\Longrightarrow} T$ .

# Example of Derivation

1. e : s ID

Alternative Notation

2. e : s '(' e ')'

3. e : e '/' e

4. s :

5. s : '+'

6. s : '-'

e : s ID

| s '(' e ')'

| e '/' e

 $s:\epsilon\mid '+'\mid '-'$ 

Problem: Derive - ID / ( ID / ID )

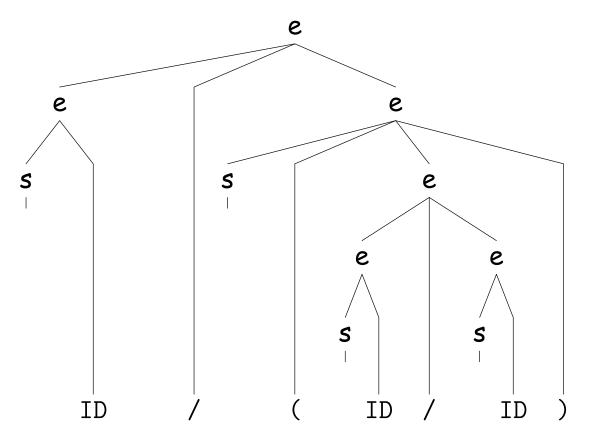
e 
$$\stackrel{3}{\Longrightarrow}$$
 e / e  $\stackrel{1}{\Longrightarrow}$  s ID / e  $\stackrel{6}{\Longrightarrow}$  - ID / e  $\stackrel{2}{\Longrightarrow}$  - ID / s ( e )  $\stackrel{4}{\Longrightarrow}$  - ID / ( e )  $\stackrel{3}{\Longrightarrow}$  - ID / ( e / e )  $\stackrel{1}{\Longrightarrow}$  - ID / ( s ID / e )  $\stackrel{4}{\Longrightarrow}$  - ID / ( ID / e )  $\stackrel{1}{\Longrightarrow}$  - ID / ( ID / ID )

# Types of Derivation

- Context free means can replace nonterminals in any order (i.e., regardless of context) to get same result (as long as you use same productions).
- So, if we use a particular rule for selecting nonterminal to "produce" from, can characterize derivation by just listing productions.
- Previous example was *leftmost derivation*: always choose leftmost nonterminals. Completely characterized by list of productions: 3, 1, 6, 2, 4, 3, 1, 4, 1, 4.

### Derivations and Parse Trees

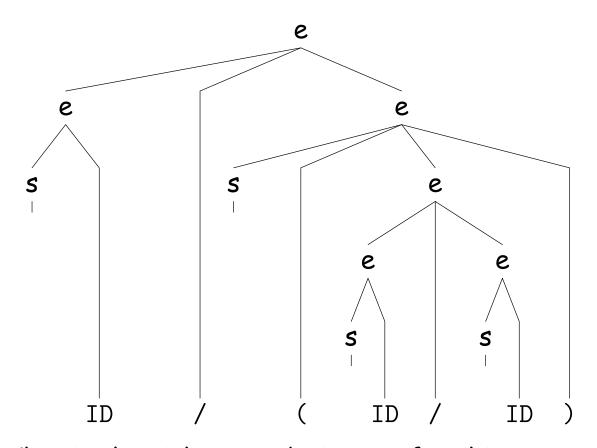
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$$\begin{array}{c} e \stackrel{3}{\Longrightarrow} e \ / \ e \stackrel{2}{\Longrightarrow} e \ / \ s \ (e) \stackrel{3}{\Longrightarrow} e \ / \ s \ (e \ / \ e) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e \ / \ s) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e \ / \ s) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e \ / \ s) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e \ / \ s) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e \ / \ e) \\ \stackrel{1}{\Longrightarrow} e \ / \ s \ (e$$

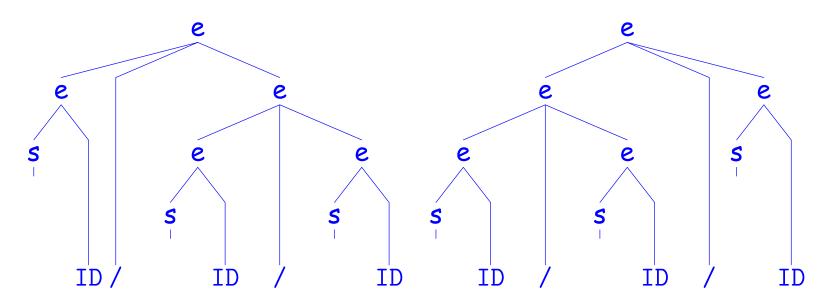
# **Ambiguity**

- Only one derivation for previous example.
- What about 'ID / ID / ID'?
- Claim there are two parse trees, corresponding to two leftmost derivations. What are they?

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# Review: Syntax-Directed Translation

- Want the structure of sentences, not just whether they are in the language, because this drives translation.
- Associate translation rules to each production, just as Flex associated actions with matching patterns.
- Bison notation:

```
e:e'/'e
                     \{ \$\$ = doDivide(\$1, \$3); \}
```

provides way to refer to and set *semantic values* on each node of a parse tree.

- Compute these semantic values from leaves up the parse tree.
- Same as the order of a rightmost derivation in reverse (a.k.a a canonical derivation).
- Alternatively, just perform arbitrary actions in the same order.

# Example: Conditional statement

**Problem:** if-else or if-elif-else statements in Python (else optional). Assume that only (indented) suites may be used for then and else clauses, that nonterminal stmt defines an individual statement (one per line), and that nonterminal expr defines an expression. Lexer supplies INDENTs and DEDENTs. A cond is a kind of stmt.

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```
expr: ...
stmt : ... | cond | ...
cond : "if" '(' expr ')' stmt else
else : \epsilon | "else" stmt
```

But this doesn't quite work: recognizes correct statements and rejects incorrect ones, but is ambiguous. E.g.,

```
if (foo) if (bar) walk(); else chewGum();
```

Do we chew gum if foo is false? That is, is this equivalent to

```
if (foo) { if (bar) walk(); } else chewGum();
/*or*/ if (foo) { if (bar) walk(); else chewGum(); } ?
```

# Example resolved: Conditional statement in Java

The rule is supposed to be "each 'else' attaches to the nearest open 'if' on the left," which is captured by:

#### This does not allow us to interpret

```
if (foo) if (bar) walk(); else chewGum();

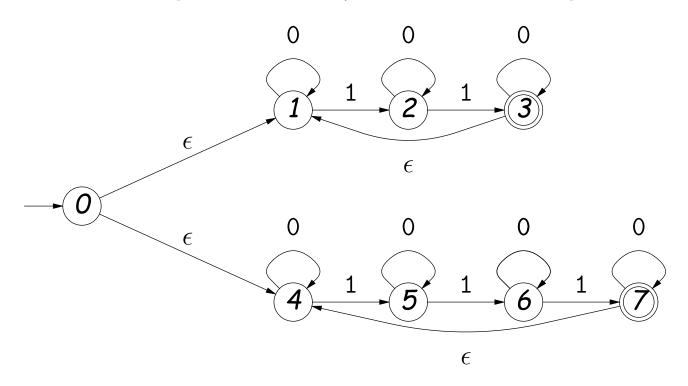
as

if (foo) { if (bar) walk(); } else chewGum();
```

But it's not exactly clear, is it?

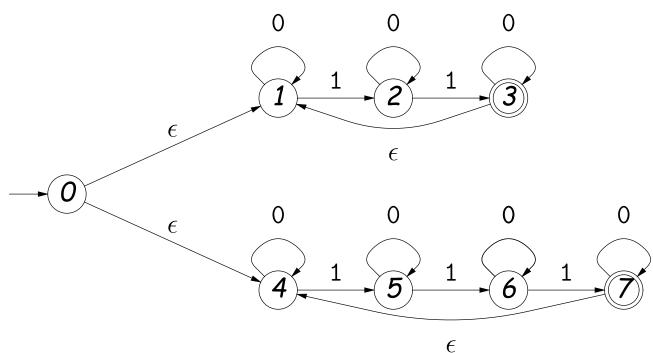
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#### A conventional answer (from class):

S: S2s Z | S3s Z

Z: '0' Z |  $\epsilon$ 

S2s: S2 | S2 S2s

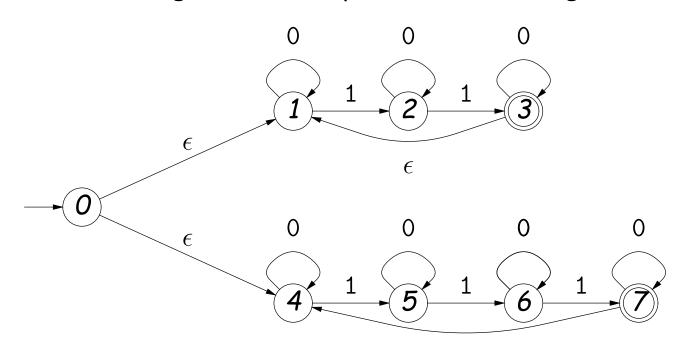
S3s: S3 | S3 S3s

S2: Z '1' Z '1'

S3: Z '1' Z '1' Z '1'

#### Puzzle: NFA to BNF

What BNF grammar accepts the same string as this NFA? Problem:



General answer (adaptable to any NFA), with one nonterminal per state:

S0: S1   S4	S4: '1' S5   '0' S4
S1: '1' S2   '0' S1	S5: '1' S6   '0' S5
S2: '1' S3   '0' S2	S6: '1' S7   '0' S6
S3: S1   '0' S3   $\epsilon$	S7: S4   '0' S7   $\epsilon$

Nonterminal Sk is "the set of strings that will get me from Sk in the NFA to a final state in the NFA."