

- Project involves generating an AST for Python dialect.
- Our tools provide extended BNF (BNF + regular-expression notations like '*', '+', and '?') both for context-free and lexical definitions.
- Tools also provide largely automatic AST building:
 - Tokens double as AST operators.
 - By default, each rule computes the list of all trees built by its right-hand side.
 - The '^' notation allows you to build a tree designating the operator.
 - Or, in an action, you can use '\$^(...)' to build an AST node, and '\$*' to denote the list of children's ASTs.
- We've also provided methods to print nodes.

Project #1 Notes (II)

- In my solution, a majority of grammar rules look like this:

```
attributeref: primary "."! identifier
             { $$ = $^(ATTRIBUTEREF, $*); }
;
```

and all the printing, etc. is taken care of.

- Dummy tokens like ATTRIBUTEREF are first defined with

```
%token ATTRIBUTEREF "@attributeref"
```

- In a few cases, I can just write

```
expr1 : expr1 "or"~ expr1
```

and the action is generated automatically.

A Little Notation

Here and in lectures to follow, we'll often have to refer to general productions or derivations. In these, we'll use various alphabets to mean various things:

- Capital roman letters are nonterminals (A, B, \dots).
- Lower-case roman letters are terminals (or tokens, characters, etc.).
- Lower-case greek letters are sequences of zero or more terminal and nonterminal symbols, such as appear in sentential forms or on the right sides of productions (α, β, \dots).
- Subscripts on lower-case greek letters indicate individual symbols within them, so $\alpha = \alpha_1 \alpha_2 \dots \alpha_n$ and each α_i is a single terminal or nonterminal.

For example,

- $A: \alpha$ might describe the production $e: e '+' t$,
- $B \Rightarrow \alpha A \gamma \Rightarrow \alpha \beta \gamma$ might describe the derivation steps $e \Rightarrow e '+' t \Rightarrow e '+' ID$ (α is $e '+'$; A is t ; B is e ; and γ is empty.)

Fixing Recursive Descent

- First, let's define an impractical but simple implementation of a top-down parsing routine.
- For nonterminal A and string $S=c_1c_2\dots c_n$, we'll define $\text{parse}(A, S)$ to return the length of a valid substring derivable from A .
- That is, $\text{parse}(A, c_1c_2\dots c_n) = k$, where

$$\frac{c_1c_2\dots c_k}{A \xrightarrow{*}}$$

Abstract body of parse(A, S)

- Can formulate top-down parsing analogously to NFAs.

```

parse (A, S):
    ""Assuming A is a nonterminal and S = c_1c_2...c_n is a string, return
    integer k such that A can derive the prefix string c_1...c_k of S.""
    Choose production 'A: alpha_1alpha_2...alpha_m' for A (nondeterministically)
    k = 0
    for x in alpha_1, alpha_2, ..., alpha_m:
        if x is a terminal:
            if x == c_{k+1}:
                k += 1
            else:
                GIVE UP
        else:
            k += parse (x, c_{k+1}...c_n)
    return k
    
```

- Assume that the grammar contains one production for the start symbol: $p: \gamma \rightarrow$.
- We'll say that a call to parse returns a value if *some* set of choices for productions (the blue step) would return a value (just like NFA).
- Then if $\text{parse}(p, S)$ returns a value, S must be in the language.

Example

Consider parsing $S="ID*ID-"$ with a grammar from last time:

```

p : e '-'
e : t
  | e '/' t
  | e '*' t
t : ID
    
```

A successful path through the program:

```

parse(p, S):
  Choose p : e '-':
    parse(e, S):
      Choose e : e '*':
        parse(e, S):
          Choose e : t:
            parse(t, S):
              Choose t : ID:
                check S[k_1] == ID; OK, so k_1 += 1;
                return 1 (and add to k_2)
          Check S[k_2] == '*'; OK, k_2 += 1
        parse(t, S_3): # S_3 == "ID -"
          Choose t : ID:
            check S_3[k_3+1] == S_3[1] == ID; OK
            k_3 += 1; return 1 (so k_2 += 1)
          return 3
        Check S[k_1+1] == S[4] == '-': OK
        k_1 += 1; return 4
    
```

k_i means "the variable k in the call to parse that is nested i deep." Outermost k is k_1 . Likewise for S .

Making a Deterministic Algorithm

- If we had an infinite supply of processors, could just spawn new ones at each "Choose" line.
- Some would give up, some loop forever, but on correct programs, at least one processor would get through.
- To do this for real (say with one processor), need to keep track of all possibilities systematically.
- This is the idea behind Earley's algorithm:
 - Handles any context-free grammar.
 - Finds all parses of any string.
 - Can recognize or reject strings in $O(N^3)$ time for ambiguous grammars, $O(N^2)$ time for "nondeterministic grammars", or $O(N)$ time for deterministic grammars (such as accepted by Bison).

Example, completed

- Last slide showed only those items that survive and get used. Algorithm actually computes dead ends as well (unlettered, in red).

0	-	1	I	2	+	3	I
a.p: ● e '→', 0	e.s: '→'●, 0	g.e: s I●, 0		i.e: e '→' ● e, 0			
b.e: ● e '→' e, 0	f.e: s● I, 0	h.e: e ● '→' e, 0		j.e: ● s I, 3			
c.e: ● s I, 0		p: e ● '→', 0		k.s: ●, 3			
d.s: ● '→', 0				l.e: s ● I, 3			
s: ●, 0				s: ● '→', 3			
e: s ● I, 0				e: ● e '→' e, 3			
4	-	5					
m.e: s I●, 3		p.p: e '→' ●, 0					
n.e: e '→' e●, 0							
a.p: e● '→', 0							
e: e ● '→' e, 3							

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Adding Semantic Actions

- Pretty much like recursive descent. The call $\text{parse}(A: \alpha \bullet \beta, s, k)$ can return, in addition to j , the semantic value of the A that matches characters $c_{s+1} \dots c_j$.
- This value is actually computed during calls of the form $\text{parse}(A: \alpha' \bullet, s, k)$ (i.e., where the β part is empty).
- Assume that we have attached these values to the nonterminals in α , so that they are available when computing the value for A .

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Ambiguity

- Ambiguity only important here when computing semantic actions.
- Rather than being satisfied with a single path through the chart, we look at *all* paths.
- And we attach the *set* of possible results of $\text{parse}(Y: \bullet \kappa, s, k)$ to the nonterminal Y in the algorithm.

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