Lecture 23: Code Optimization

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Introduction to Code Optimization

dapted from notes by R. Bodik and G. Necula] blic Service Announcement . "Hackers@Berkeley is hosting BEARHACK is Saturday at 11AM in the Wozniak Lounge. It's a 24 hour hackathon here'll be tons of good food (Cheeseboard, sushi & boba!), activities cluding massages!), and prizes (including an Occulus Rift).	Code optimization is the usual term, but is grossly misnamed, since code produced by "optimizers" is not optimal in any reasonable sense. Pro- gram improvement would be more appropriate. Topics: Basic blocks Control-flow graphs (CFGs) Algebraic simplification Constant folding Static single-assignment form (SSA) Common-subexpression elimination (CSE) Copy propagation Dead-code elimination Peephole optimizations	
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Basic Blocks	Basic-Block Example	
 A basic block is a maximal sequence of instructions with: no labels (except at the first instruction), and no jumps (except in the last instruction) Idea: Cannot jump into a basic block, except at the beginning. Cannot jump within a basic block, except at end. Therefore, each instruction in a basic block is executed after all the preceding instructions have been executed 	 Consider the basic block L1: t := 2 * x w := t + x if w > 0 goto L2 No way for (3) to be executed without (2) having been executed right before We can change (3) to w := 3 * x Can we eliminate (2) as well? 	

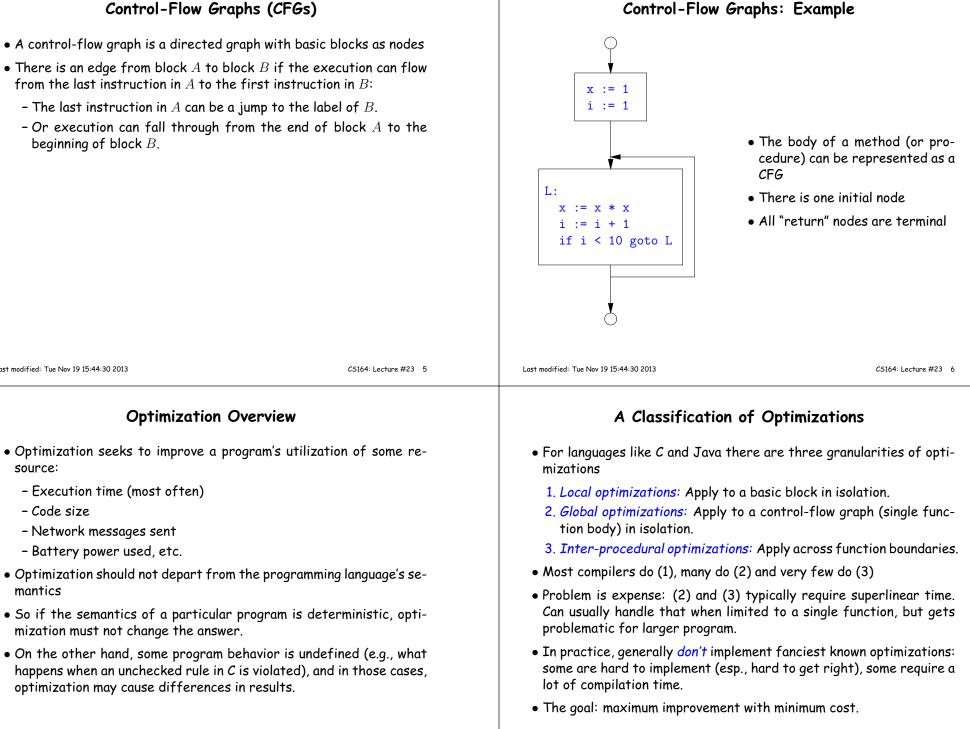
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Control-Flow Graphs (CFGs)

- A control-flow graph is a directed graph with basic blocks as nodes
- There is an edge from block A to block B if the execution can flow from the last instruction in A to the first instruction in B:
 - The last instruction in A can be a jump to the label of B.
 - Or execution can fall through from the end of block A to the beginning of block B.



mization must not change the answer.

- Execution time (most often)

- Network messages sent

- Battery power used, etc.

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source:

mantics

- Code size

Local Optimizations: Algebraic Simplification	Local Optimization: Constant Folding				
 Some statements can be deleted 	 Operations on constants can be computed at compile time. 				
x := x + 0 x := x * 1 • Some statements can be simplified or converted to use faster operations: $\begin{array}{c c} Original & Simplified \\ \hline x := x * 0 & x := 0 \\ y := y * * 2 & y := y * y \end{array}$	 Example: x := 2 + 2 becomes x := 4. Example: if 2 < 0 jump L becomes a no-op. When might constant folding be dangerous? 				
x := x * 8 $x := x * 15$ $t := x << 4; x := t - x$ (on some machines << is faster than *; but not on all!)					
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Global Optimization: Unreachable code elimination	Single Assignment Form				
 Basic blocks that are not reachable from the entry point of the CFG may be eliminated. 	 Some optimizations are simplified if each assignment is to a tempo- rary that has not appeared already in the basic block. 				
 Why would such basic blocks occur? 	• Intermediate code can be rewritten to be in (static) single assign-				
 Removing unreachable code makes the program smaller (sometimes also faster, due to instruction-cache effects, but this is probably not a terribly large effect.) 	ment (SSA) form: $x := a + y$ $x := a + y$ $a := x$ $a1 := x$ $x := a * x$ $x1 := a1 * x$ $b := x + a$ $b := x1 + a1$ where x1 and a1 are fresh temporaries.				

Common SubExpression (CSE) Elimination in Basic Blocks

- A common subexpression is an expression that appears multiple times on a right-hand side in contexts where the operands have the same values in each case (so that the expression will yield the same value).
- Assume that the basic block on the left is in single assignment form.

x := y + z	x := y + z
w := y + z	w := x

• That is, if two assignments have the same right-hand side, we can replace the second instance of that right-hand side with the variable that was assigned the first instance.

Another Example of Copy Propagation and Constant

Folding

a := 5

x := 10

a := 5

x := 2 * 5

y := x + 6

t := x * y

• How did we use the assumption of single assignment here?

Copy Propagation

- If w := x appears in a block, can replace all subsequent uses of w with uses of x.
- Example:

b:=z+y	b:=z+y
a := b	a := b
x:=2*a	x:=2*b

- This does not make the program smaller or faster but might enable other optimizations. For example, if a is not used after this statement, we need not assign to it.
- Or consider:

b:=13	b:=13
x:=2*b	x:=2*13

which immediately enables constant folding.

• Again, the optimization, as described, won't work unless the block is in single assignment form.

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Dead Code Elimination

- If that statement w := rhs appears in a basic block and w does not appear anywhere else in the program, we say that the statement is *dead* and can be eliminated; it does not contribute to the program's result.
- Example: (a is not used anywhere else)

b	:= z	+	У	b	:=	z	+	У	b	:=	z	+	У
a	:= b			a	:=	b							
x	:= 2	*	a	х	:=	2	*	b	x	:=	2	*	b

• How have I used SSA here?

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2 * a

y := x + 6

t := x * v

a := 5

x :=

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a := 5

x := 10

y := 16

t := 160

a := 5

x := 10

y := 10 + 6 y := 16

t := 10 * y t := 10 * 16

Applying Local Optimizations An Example: Initial Code • As the examples show, each local optimization does very little by a := x ** 2 itself. b := 3 c := x • Typically, optimizations interact: performing one optimization end := c * c ables others. e := b * 2 • So typical optimizing compilers repeatedly perform optimizations f := a + d until no improvement is possible, or it is no longer cost effective. g := e * f Last modified: Tue Nov 19 15:44:30 2013 CS164: Lecture #23 17 Last modified: Tue Nov 19 15:44:30 2013 CS164: Lecture #23 18 An Example II: Algebraic simplification An Example: Copy propagation a := x * x a := x * x b := 3 b := 3 c := x c := x d := c * c d := x * x e := b + b e := 3 + 3 f := a + d f := a + d g := e * f g := e * f

An Example: Constant folding		An Example: Common Subexpression El	imination
a := x * x b := 3 c := x d := x * x e := 6 f := a + d g := e * f		<pre>a := x * x b := 3 c := x d := a e := 6 f := a + d g := e * f</pre>	
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An Example: Copy propagation		An Example: Dead code eliminati	on
a := x * x b := 3 c := x d := a e := 6 f := a + a g := 6 * f		a := x * x f := a + a g := 6 * f This is the final form.	

Peephole Optimizations on Assembly Code

- The optimizations presented before work on intermediate code.
- *Peephole optimization* is a technique for improving assembly code directly
 - The "*peephole*" is a short subsequence of (usually contiguous) instructions, either continguous, or linked together by the fact that they operate on certain registers that no intervening instructions modify.
 - The optimizer replaces the sequence with another equivalent, but (one hopes) better one.
 - Write peephole optimizations as replacement rules

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i1; ...; in \Rightarrow j1; ...; jm
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possibly plus additional constraints. The $j^\prime s$ are the improved version of the $i^\prime s.$

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Problems:

- Serious problem: what to do with pointers? Problem is *aliasing:* two names for the same variable:
 - As a result, *t may change even if local variable t does not and we never assign to *t.
 - Affects language design: rules about overlapping parameters in Fortran, and the **restrict** keyword in C.
 - Arrays are a special case (address calculation): is A[i] the same as A[j]? Sometimes the compiler can tell, depending on what it knows about i and j.
- What about globals variables and calls?
 - Calls are not exactly jumps, because they (almost) always return.
 - Can modify global variables used by caller

Peephole optimization examples:

- \bullet We'll use the notation '@A' for pattern variables.
- Example:

movl %@a %@b; L: movl %@b %@a \Rightarrow movl %@a %@b

assuming ${\tt L}$ is not the target of a jump.

• Example:

addl \$@k1, %@a; movl @k2(%@a), %@b ⇒ movl @k1+@k2(%@a), %@b

assuming %@a is "dead".

• Example (PDP11):

mov #@I, @I(@ra) \Rightarrow mov (r7), @I(@ra)

This is a real hack: we reuse the value I as both the immediate value and the offset from ra. On the PDP11, the program counter is r7.

• As for local optimizations, peephole optimizations need to be applied repeatedly to get maximum effect.

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Global Optimization

- *Global optimization* refers to program optimizations that encompass multiple basic blocks in a function.
- (I have used the term *galactic optimization* to refer to going beyond function boundaries, but it hasn't caught on; we call it just *interprocedural optimization*.)
- Since we can't use the usual assumptions about basic blocks, global optimization requires *global flow analysis* to see where values can come from and get used.
- The overall question is: When can local optimizations (from the last lecture) be applied across multiple basic blocks?

A Simple Example: Copy Propagation	Issues					
	 This correctness condition is not trivial to check 					
$\begin{array}{c} X & := 3 \\ B > 0 \end{array}$	 "All paths" includes paths around loops and through branches of con- ditionals 					
$Y := Z + W \qquad Y := 0$	 Checking the condition requires global analysis: an analysis of the entire control-flow graph for one method body. 					
X := 4	 This is typical for optimizations that depend on some property P at a particular point in program execution. 					
A := 2 * X	• Indeed, property <i>P</i> is typically undecidable, so program op is all about making <i>conservative</i> (but not cowardly) approvof <i>P</i> .					
 Without other assignments to X, it is valid to treat the red parts as if they were in the same basic block. 						
 But as soon as one other block on the path to the bottom block assigns to X, we can no longer do so. 						
• It is correct to apply copy propagation to a variable x from an as- signment statement A: x := to a given use of x in statement B only if the last assignment to x in every path from to B is A.						
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Undecidability of Program Properties	Conservative Program Analyses					
• Rice's "theorem:" Most interesting dynamic properties of a program	ullet If a certain optimization requires P to be true, then					
are undecidable. E.g.,	– If we know that P is definitely true, we can apply the optimiza-					
- Does the program halt on all (some) inputs? (Halting Problem)	tion					
- Is the result of a function F always positive? (Consider	- If we don't know whether P is true, we simply don't a					
def F(x): H(x)	timization. Since optimizations are not supposed to c meaning of a program, this is safe.	nunge me				
return 1	 In other words, in analyzing a program for properties lil 	ko P it ic				
Result is positive iff H halts.)	<i>always correct</i> (albeit non-optimal) to say "don't know."	ne 1 , 11 13				

- Syntactic properties are typically decidable (e.g., "How many occurrences of x are there?").
- Theorem does not apply in absence of loops

• The trick is to say it as seldom as possible.

with these characteristics.

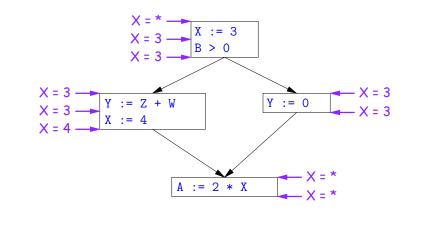
• Global dataflow analysis is a standard technique for solving problems

Example: Global Constant Propagation

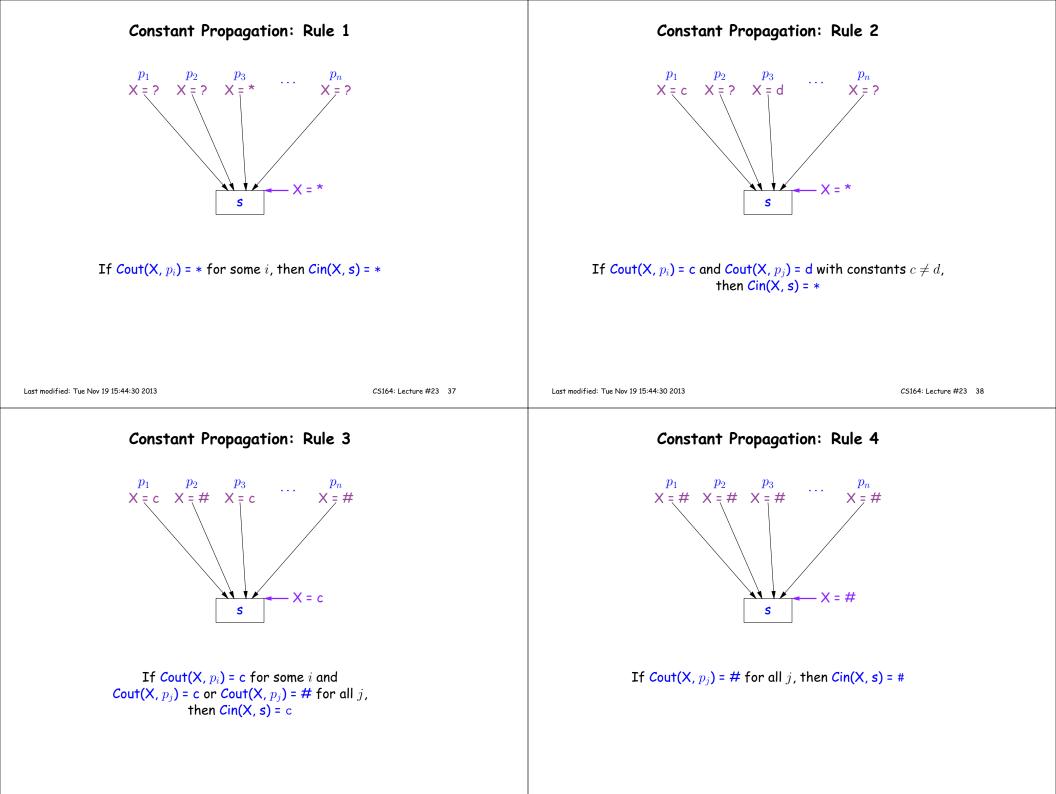
- *Global constant propagation* is just the restriction of copy propagation to constants.
- In this example, we'll consider doing it for a single variable (X).
- \bullet At every program point (i.e., before or after any instruction), we associate one of the following values with ${\tt X}$

Value	Interpretation
#	(aka bottom) No value has reached here (yet)
с	(For c a constant) X definitely has the value c .
*	(aka <i>top</i>) Don't know what, if any, constant value X has.

Example of Result of Constant Propagation



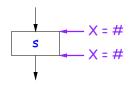
Last modified: Tue Nov 19 15:44:30 2013 Using Analysis Re	C5164: Lecture #23 33	Last modified: Tue Nov 19 15:44:30 2013 Transfer Fun	C5164: Lecture #23 34
 Given global constant information, it is mization: Tf the point immediately before a str 		 Basic Idea: Express the analysis of a bination of simple rules relating the adjacent statements 	
 If the point immediately before a statement using x tells us that x = c, then replace x with c. Otherwise, leave it alone (the conservative option). But how do we compute these properties x =? 		 That is, we "push" or transfer infor the next. 	mation from one statement to
		 For each statement s, we end up wird of x immediately before and after s: 	
		Cin(X,s) = value of x before s Cout(X,s) = value of x after s	
		 Here, the "values of x" we use come taining the values we care about—#, by our analysis. 	
		 For the constant propagation problem and we'll get Cin from the Couts of pr p₁),,Cout(X,p_n). 	•



Constant Propagation: Computing Cout

- Rules 1-4 relate the *out* of one statement to the *in* of the successor statements, thus propagating information *forward* across CFG edges.
- Now we need *local* rules relating the *in* and *out* of a single statement to propagate information across statements.

Constant Propagation: Rule 5



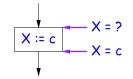
Cout(X, s) = # if Cin(X, s) =

The value '#' means "so far, no value of X gets here, because the we don't (yet) know that this statement ever gets executed."

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Constant Propagation: Rule 6

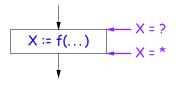


Cout(X, X := c) = c if c is a constant and ? is not #.

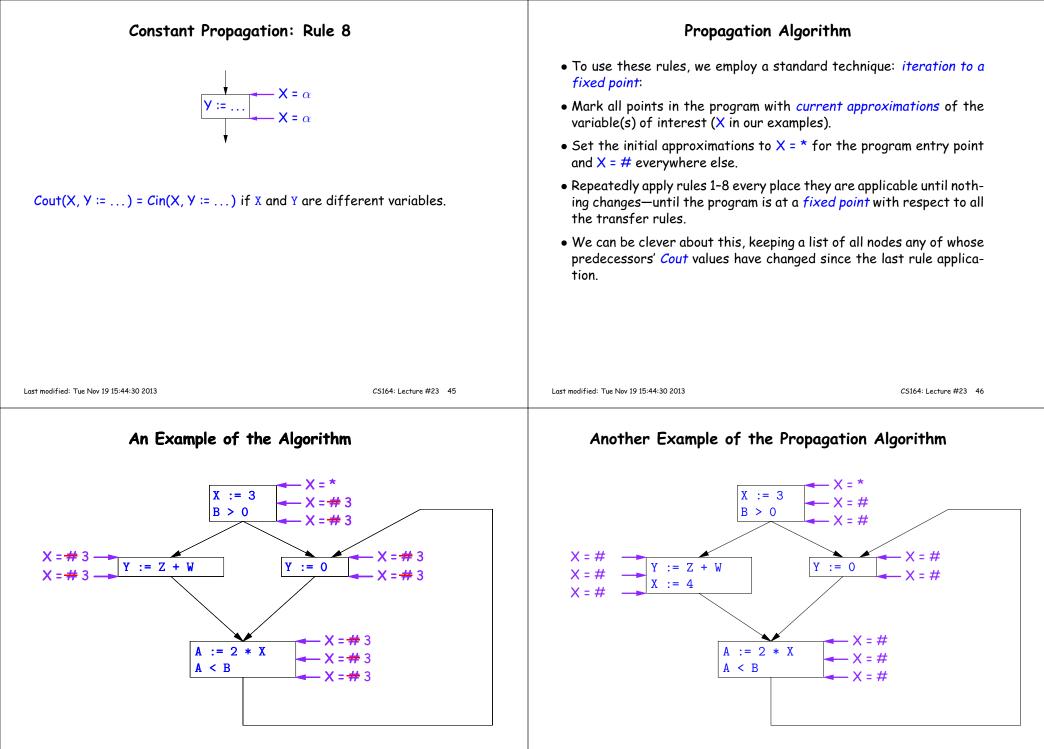
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Constant Propagation: Rule 7

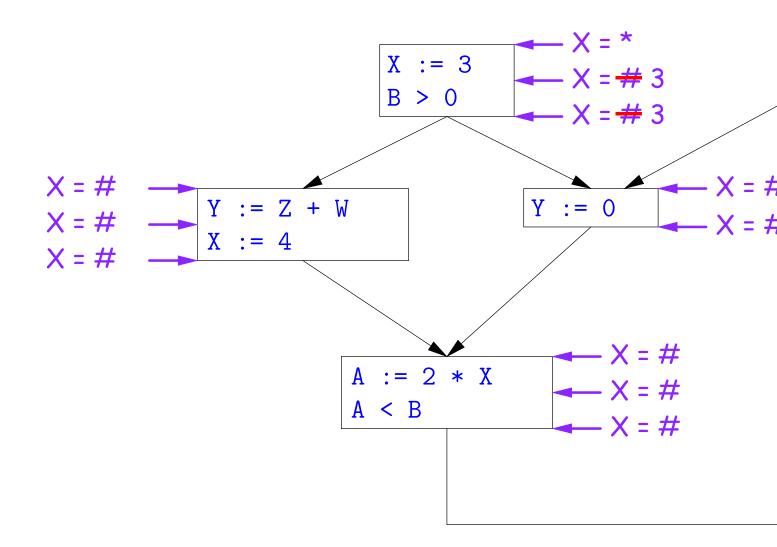


Cout(X, X := f(...)) = * for any function call, if ? is not #.

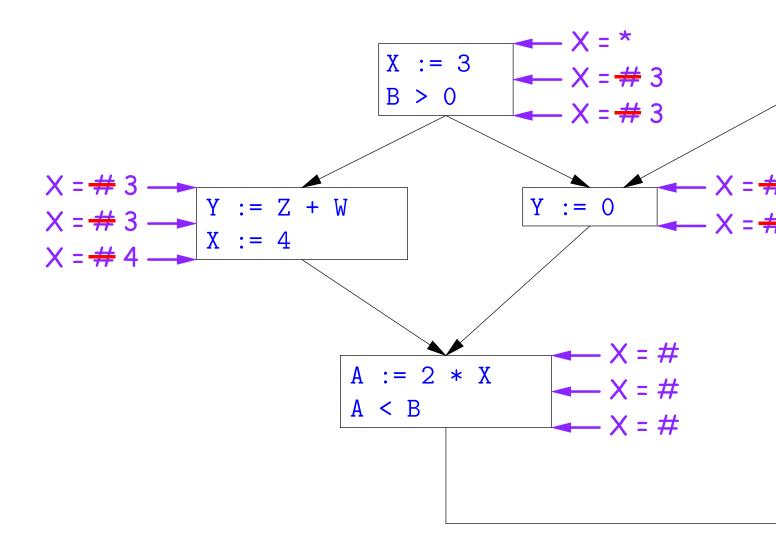


So we can replace X with 3 in the bottom block.

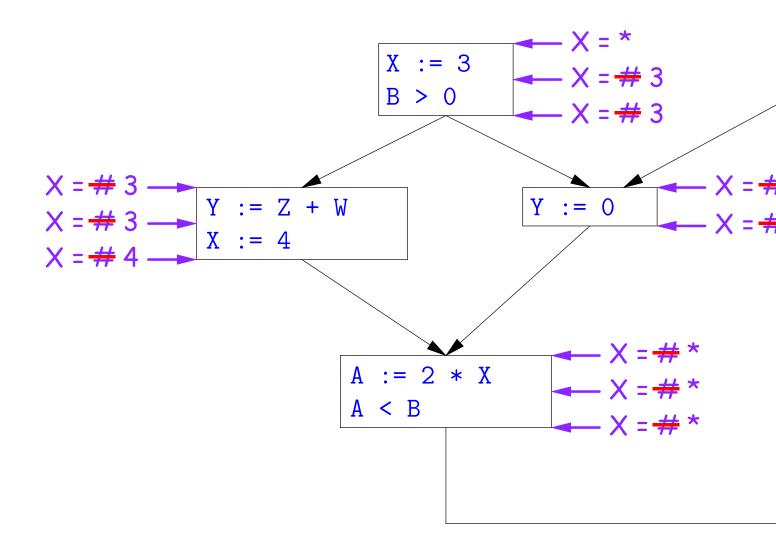




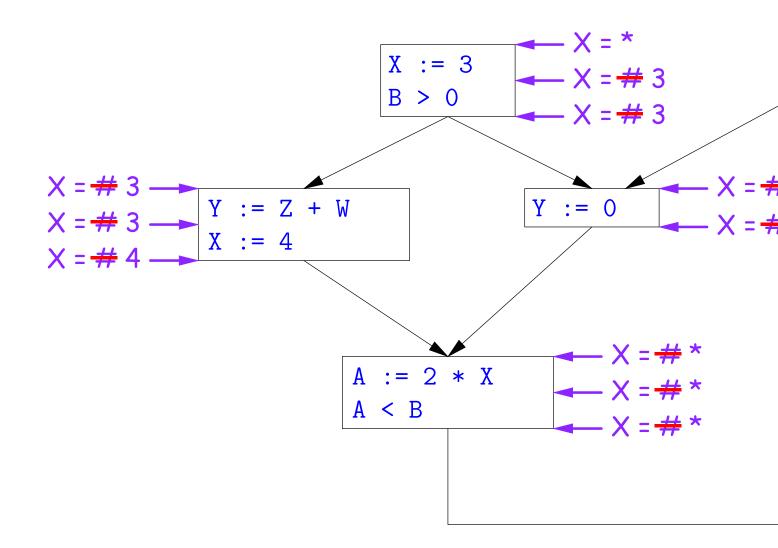
Another Example of the Propagation Algorithm



Another Example of the Propagation Algorithm

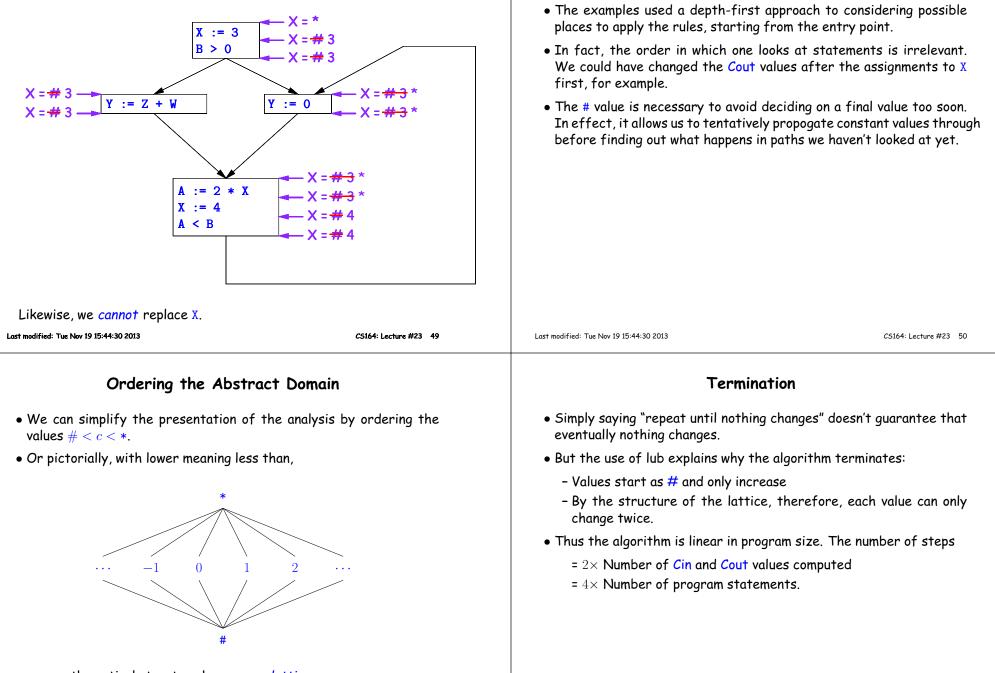


Another Example of the Propagation Algorithm



Here, we cannot replace X in two of the basic blocks.

A Third Example

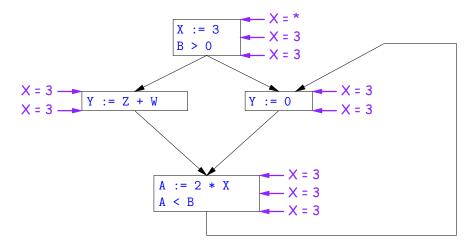


- ... a mathematical structure known as a *lattice*.
- With this, our rule for computing Cin is simply a least upper bound:
 Cin(x, s) = lub { Cout(x, p) such that p is a predecessor of s }.

Comments

Liveness Analysis

Once constants have been globally propagated, we would like to eliminate dead code



After constant propagation, X	:= 3 is dead code (assuming this is the	
entire CFG)		
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Computing Liveness

- We can express liveness as a function of information transferred between adjacent statements, just as in copy propagation
- Liveness is simpler than constant propagation, since it is a boolean property (true or false).
- That is, the lattice has two values, with false<true.
- It also differs in that liveness depends on what comes after a statement, not before—we propagate information backwards through the flow graph, from Lout (liveness information at the end of a statment) to Lin.

Terminology: Live and Dead

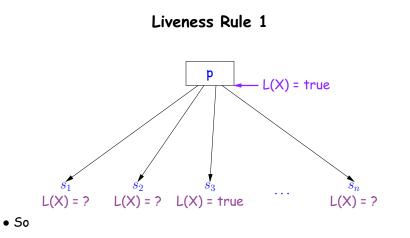
• In the program

X := 3; /*(1)*/ X = 4; /*(2)*/ Y := X /*(3)*/

- the variable X is *dead* (never used) at point (1), *live* at point (2), and may or may not be live at point (3), depending on the rest of the program.
- More generally, a variable x is live at statement s if
 - There exists a statement s' that uses x;
 - There is a path from s to s'; and
 - That path has no intervening assignment to ${\boldsymbol{x}}$
- A statement x := ... is dead code (and may be deleted) if x is dead after the assignment.

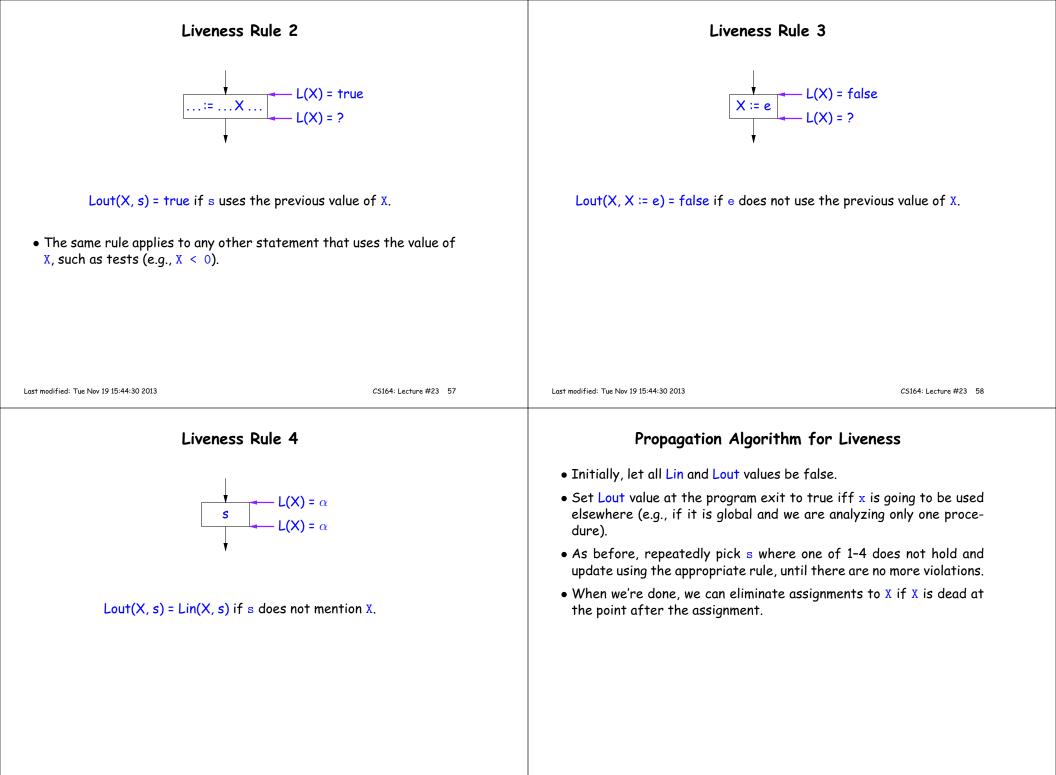
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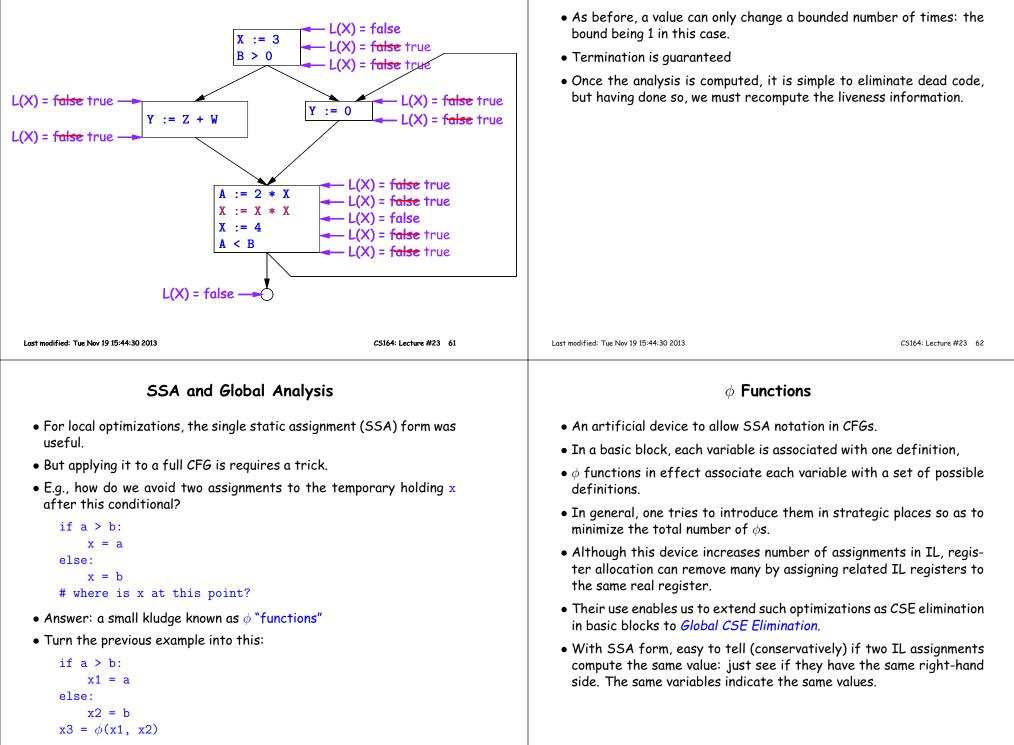


Lout(x, p) = lub { Lin(x, s) such that s is a predecessor of p }.

• Here, least upper bound (lub) is the same as "or".



Example of Liveness Computation



Termination

Summary

- We've seen two kinds of analysis:
 - Constant propagation is a *forward analysis*: information is pushed from inputs to outputs.
 - Liveness is a *backwards analysis*: information is pushed from outputs back towards inputs.
- But both make use of essentially the same algorithm.
- Numerous other analyses fall into these categories, and allow us to use a similar formulation:
 - An abstract domain (abstract relative to actual values);
 - Local rules relating information between consecutive program points around a single statement; and
 - Lattice operations like least upper bound (or *join*) or greatest lower bound (or *meet*) to relate inputs and outputs of adjoining statements.

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