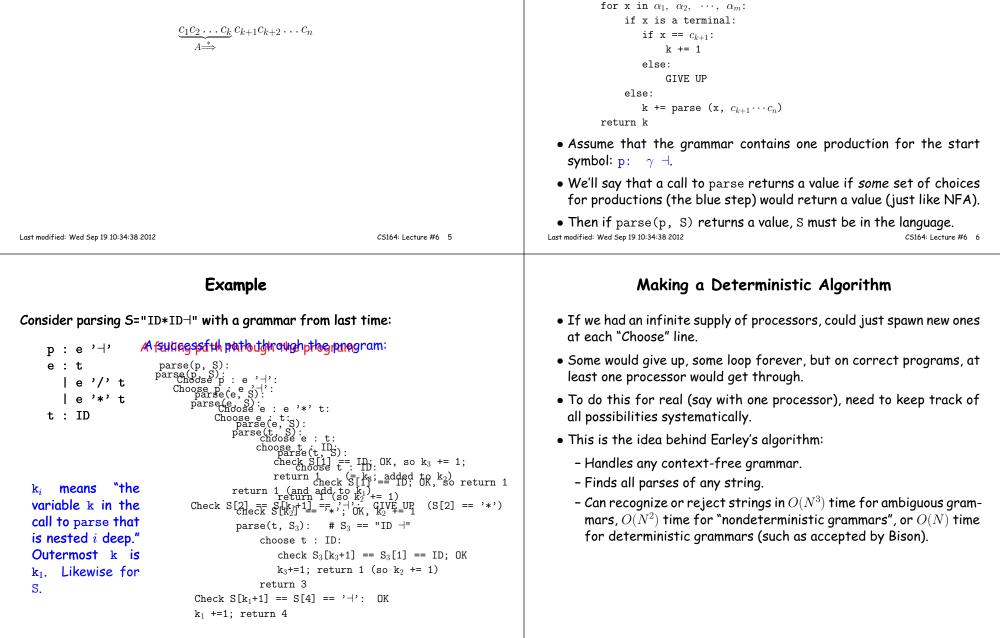
Lecture 6: General and Bottom-Up Parsing	Project #1 Notes				
	<ul> <li>Project involves generating an AST for Python dialect.</li> </ul>				
	• Our tools provide extended BNF (BNF + regular-expression nota- tions like '*', '+', and '?') both for context-free and lexical defini- tions.				
	<ul> <li>Tools also provide largely automatic AST building:</li> </ul>				
	– Tokens double as AST operators.				
	<ul> <li>By default, each rule computes the list of all trees built by its right-hand side.</li> </ul>				
	<ul> <li>The '^' notation allows you to build a tree designating the opera- tor.</li> </ul>				
	<ul> <li>Or, in an action, you can use '\$^()' to build an AST node, and</li> <li>'\$*' to denote the list of children's ASTs.</li> </ul>				
	<ul> <li>We've also provided methods to print nodes.</li> </ul>				
Last modified: Wed Sep 19 10:34:38 2012 C5164: Lecture #6 1 Project #1 Notes (II)	Last modified: Wed Sep 19 10:34:38 2012 CS164: Lecture #6 2 A Little Notation				
• In my solution, a majority of grammar rules look like this: attributeref: primary "."! identifier	Here and in lectures to follow, we'll often have to refer to general productions or derivations. In these, we'll use various alphabets to mean various things:				
{ \$\$ = \$^(ATTRIBUTEREF, \$*); };	<ul> <li>Capital roman letters are nonterminals (A, B,).</li> </ul>				
and all the printing, etc. is taken care of.	• Lower-case roman letters are terminals (or tokens, characters, etc.)				
• Dummy tokens like ATTRIBUTEREF are first defined with %token ATTRIBUTEREF "@attributeref"	• Lower-case greek letters are sequences of zero or more terminal and nonterminal symbols, such as appear in sentential forms or on the right sides of productions $(\alpha, \beta,)$ .				
<ul> <li>In a few cases, I can just write</li> <li>expr1 : expr1 "or"<sup>^</sup> expr1</li> <li>and the action is generated automatically.</li> </ul>	• Subscripts on lower-case greek letters indicate individual symbols within them, so $\alpha = \alpha_1 \alpha_n \dots \alpha_n$ and each $\alpha_i$ is a single terminal or nonterminal.				
and the denot to generated datomatically.	For example,				
	• $A: \alpha$ might describe the production e: e '+' t,				
	• $B \Rightarrow \alpha A \gamma \Rightarrow \alpha \beta \gamma$ might describe the derivation steps $e \Rightarrow e' + t'$ $\Rightarrow e' + TD (\alpha \text{ is } e' + t'; A \text{ is } t; B \text{ is } e; \text{ and } \gamma \text{ is empty.})$				

### **Fixing Recursive Descent**

- First, let's define an impractical but simple implementation of a topdown parsing routine.
- For nonterminal A and string  $S=c_1c_2...c_n$ , we'll define parse(A, S) to return the length of a valid substring derivable from A.
- That is,  $parse(A, c_1c_2...c_n) = k$ , where



Abstract body of parse(A,S)

"""Assuming A is a nonterminal and S =  $c_1c_2...c_n$  is a string, return

Choose production 'A:  $\alpha_1 \alpha_2 \cdots \alpha_m$ ' for A (nondeterministically)

integer k such that A can derive the prefix string  $c_1 \dots c_k$  of S."""

Can formulate top-down parsing analogously to NFAs.

parse (A, S):

k = 0

## Earley's Algorithm: I

- First, reformulate to use recursion instead of looping. Assume the string  $S = c_1 \cdots c_n$  is fixed.
- Redefine parse:
  - parse (A:  $\alpha \bullet \beta$ , s, k): """Assumes A:  $\alpha\beta$  is a production in the grammar, 0 <= s <= k <= n, and  $\alpha$  can produce the string  $c_{s+1} \cdots c_k$ . Returns integer j such that  $\beta$  can produce  $c_{k+1} \cdots c_j$ ."""
- Or diagrammatically, parse returns an integer j such that:

# $c_1 \cdots c_s \underbrace{c_{s+1} \cdots c_k}_{\alpha \xrightarrow{*}} \underbrace{c_{k+1} \cdots c_j}_{\beta \xrightarrow{*}} c_{j+1} \cdots c_n$

# Earley's Algorithm: II

```
parse (A: \alpha \bullet \beta, s, k):
   """Assumes A: \alpha\beta is a production in the grammar,
       0 <= s <= k <= n, and \alpha can produce the string c_{s+1} \cdots c_k.
       Returns integer j such that \beta can produce c_{k+1} \cdots c_i."""
   if \beta is empty:
       return k
   Assume \beta has the form x\delta
   if x is a terminal:
       if x == c_{k+1}:
            return parse(A: \alpha x \bullet \delta, s, k+1)
       else:
             GIVE UP
   else:
       Choose production 'x: \kappa' for x (nondeterministically)
       j = parse(x: \bullet \kappa, k, k)
       return parse (A: \alpha x \bullet \delta, s, j)
```

• Now do all possible choices that result in such a way as to avoid redundant work ("nondeterministic memoization").

Last modified: Wed Sep 19 10:34:38 2012	C5164: Lecture #6 9	Last modified: Wed Sep 19 10:34:38 2012	CS164: Lecture #6 10

# **Chart Parsing**

- Idea is to build up a table (known as a *chart*) of all calls to parse that have been made.
- Only one entry in chart for each distinct triple of arguments (A:  $\alpha \bullet \beta$ , s, k).
- We'll organize table in columns numbered by the k parameter, so that column k represents all calls that are looking at  $c_{k+1}$  in the input.
- Each column contains entries with the other two parameters: [A:  $\alpha \bullet \beta$ , s], which are called *items*.
- The columns, therefore, are *item sets*.

## Example

Grammar	Input String
p : e '⊢'	- I + I ⊣
e : s I   e '+' e	
s : '-'	

Chart.	Headings are values of $k$ and $c_{k+1}$ (raised symbols)	).
--------	---	----

0	-	1 <sup>I</sup>		2	+	3	I
a.p: ●e '⊢', 0	e. S :	'-'●, 0	g.e: s	I•, 0	i. e:	e '+' ●	e, 0
b.e: ●e '+' e,	0 f.e:	s•I, 0	h.e: e	•'+' e,	0 j.e:	•s I, 3	
<i>c</i> .e: ●s I, O						•, 3	
d.s: •'−', 0					<i>I.</i> e:	s •I, 3	
4	4	5					
m.e: s I•, 3	<i>p.</i> p:	e '⊣'•	, 0				
n.e: e '+' e●,	0						
<i>o</i> .p: e●'⊣', 0							

#### Example, completed

• Last slide showed only those items that survive and get used. Algorithm actually computes dead ends as well (unlettered, in red).

p:  $e \bullet ' \dashv ', 0 k s: \bullet, 3$ 

*l*.e: s • I, 3

s: • '-', 3

e: • e '+' e, 3

b.e: • e '+' e, 0 f.e: s• I, 0 h.e: e • '+' e, 0 j.e: • s I, 3

c.e: ● s I, 0

4 <sup>→</sup> 5 m.e: s I•, 3 p.p: e '→' •, 0

d.s: • '−', 0

e: s • I, 0

*n*.e: e '+' e●, 0 o.p: e● '⊢', 0 e: e • '+' e, 3

s: •, 0

# Adding Semantic Actions

- Pretty much like recursive descent. The call parse (A:  $\alpha \bullet \beta$ , s, k) can return, in addition to j, the semantic value of the A that matches characters  $c_{s+1} \cdots c_i$ .
- This value is actually computed during calls of the form parse(A:  $\alpha' \bullet$ , s, k) (i.e., where the  $\beta$  part is empty).
- Assume that we have attached these values to the nonterminals in  $\alpha$ , so that they are available when computing the value for A.

Last modified: Wed Sep 19 10:34:38 2012 CS164: Lectu	ure #6 13 Last modified: Wed Sep 19 10:34:38 20	12 CS164: Lecture #6 14
--	---	-------------------------

Ι

#### Ambiguity

- Ambiguity only important here when computing semantic actions.
- Rather than being satisfied with a single path through the chart, we look at all paths.
- And we attach the set of possible results of parse(Y: • $\kappa$ , s, k) to the nonterminal Y in the algorithm.