Lecture 7: General and Bottom-Up Parsing

Administrivia

- Project #1 posted. Due 27 Feb.
- HW #3 posted, due next Monday. HW #4 goes back to Friday schedule.
- Test #1: March 10 (in class).

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Making a Deterministic Algorithm

- If we had an infinite supply of processors, could just spawn new ones at each "Choose" line.
- Some would give up, some loop forever, but on correct programs, at least one process would get through.
- To do this for real (say with one processor), need to keep track of all possibilities systematically.
- This is the idea behind Earley's algorithm:
 - Handles any context-free grammar.
 - Finds all parses of any string.
 - Runs in $O(N^3)$ time for ambiguous grammars, $O(N^2)$ time for "non-deterministic grammars", or O(N) time for deterministic grammars (such as accepted by Bison).

Fixing Recursive Descent

Can formulate top-down parsing analogously to NFAs.

```
parse (A, S): 
"""Assuming A is a nonterminal and S = c_1c_2 \dots c_n is a string, 
return integer k such that A can derive the string c_1 \dots c_k."""

Choose production 'A: \alpha_1\alpha_2 \cdots \alpha_m' for A (nondeterministically) 
k = 0 
for x in \alpha_1, \alpha_2, \cdots, \alpha_m: 
if x is a terminal: 
if x == c_{k+1}: 
k += 1 
else: 
GIVE UP 
else: 
k += parse (x, c_{k+1} \cdots c_n) 
return k
```

- Assume that the grammar contains one production for the start symbol: p: $\gamma\dashv$.
- We'll say that a call to parse returns a value if some set of choices for productions (the blue step) would return a value (just like NFA).
- Then if parse(p, S) returns a value, S must be in the language.

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Earley's Algorithm: I

ullet First, reformulate to ditch the loop. Assume the string $S=c_1\cdots c_n$ is fixed.

```
parse (A: \alpha \bullet \beta, s, k):
   """Assumes A: \alpha\beta is a production in the
        grammar, 0 <= s <= k <= n, and \alpha can produce the string
       c_{s+1}\cdots c_k. Returns integer j such that \beta can
       produce c_{k+1} \cdots c_i."""
   if \beta is empty:
       return k
   Assume \beta has the form y\delta
   if y is a terminal:
       if y == c_{k+1}:
            return parse(A: \alpha y \bullet \delta, s, k+1)
       else
            GIVE UP
   else:
       Choose production 'y: \kappa' for y (nondeterministically)
       j = parse(y: \bullet \kappa, k, k)
       return parse (A: \alpha y \bullet \delta, s, j)
```

• Now do all possible choices that result in such a way as to avoid redundant work ("nondeterministic memoization").

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Chart Parsing

- Idea is to build up a table (known as a *chart* of all calls to parse that have been made.
- Only one entry in chart for each distinct triple of arguments (A: $\alpha \bullet \beta$, s, k).
- ullet We'll organize table in columns numbered by the k parameter, so that column k represents all calls that are looking at c_{k+1} in the input.
- Each column contains entries with the other two parameters: [A: $\alpha \bullet \beta$, s], which is called an *item*.
- The columns, therefore, are item sets.

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Example, completed

• Last slide showed only those items that survive and get used. Algorithm actually computes dead ends as well (unlettered, in red).

Example

Grammar

Input String

- I + I ⊢

Chart. Headings are values of k and c_{k+1} (raised symbols).

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Adding Semantic Actions

- Pretty much like recursive descent. The call parse (A: $\alpha \bullet \beta$, s, k) can return, in addition to j, the semantic value of the A that matches characters $c_{s+1} \cdots c_j$.
- This value is actually computed during calls of the form parse(A: α' •, s, k) (i.e., where the β part is empty).
- ullet Assume that we have attached these values to the nonterminals in lpha, so that they are available when computing the value for A.

Ambiguity

- Ambiguity only important here when computing semantic actions.
- Rather than being satisfied with a single path through the chart, we look at *all* paths.
- And we attach the set of possible results of parse(Y: $\bullet \kappa$, s, k) to the nonterminal Y in the algorithm.

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