

Foundations of Computer Graphics (Spring 2010)

CS 184, Lecture 24: Animation
<http://inst.eecs.berkeley.edu/~cs184>

Many slides courtesy Adam Finkelstein, James O'Brien, others

To Do

- Submit HW 4 (today)
- Start working on HW 5 (can be simple add-on)

These Lectures

- 3 classical prongs in graphics pipeline: Modeling, Rendering, Animation
- We talk a little about animation or motion
- Limited time, hence fun lectures, not covered in detail on final
- Possibility for HW 5, but only if very motivated
- Will also show historical videos

History of Computer Animation

- [Video \(also shown first class\)](#)

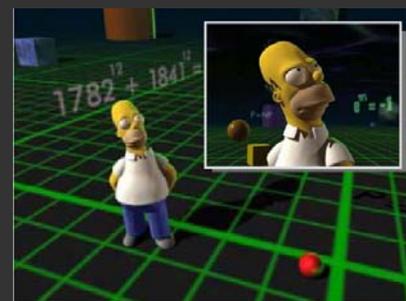
Computer Animation

- What is animation?
 - Motion of objects (change behavior with time)
 - Often scripted with spline curve
 - Trivial example animations for HW 3  Geri's game: Pixar
- What is simulation?
 - Predict how objects move according to laws of physics
 - Graphics animation often involves "directable" simulation
 - [Fracture video \(O'Brien\)](#)

2D and 3D Animation



Homer 2D



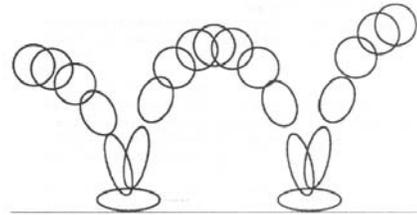
Homer 3D

Principles of Traditional Animation

- Squash and stretch
- Slow In and out
- Anticipation
- Exaggeration
- Follow through and overlapping action
- Timing
- Staging
- Straight ahead action and pose-to-pose action
- Arcs
- Secondary action
- Appeal

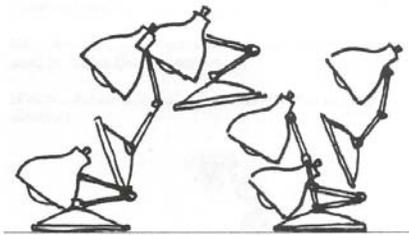
Disney

Squash and Stretch



Lasseter '87

Anticipation



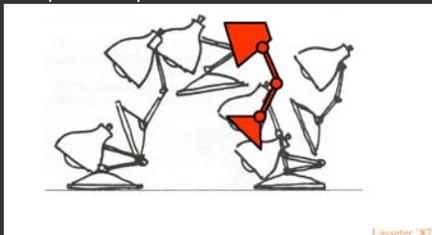
Lasseter '87

Outline

- Keyframes
- Articulated Figures
- Kinematics
- Dynamics

Computer Animation

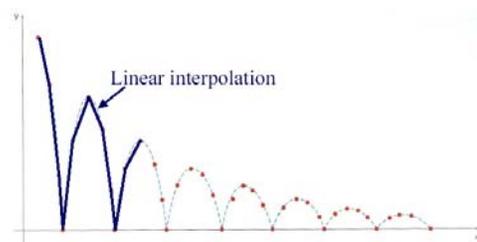
- Simplest idea: Keyframing or in-betweening
- Character poses at specific keyframes
 - Computer interpolates in-between frames



Lasseter '87

How to Interpolate?

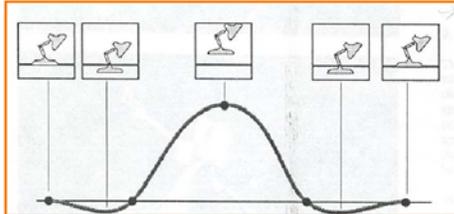
- Linear interpolation not usually good enough



H&B Figure 16.16

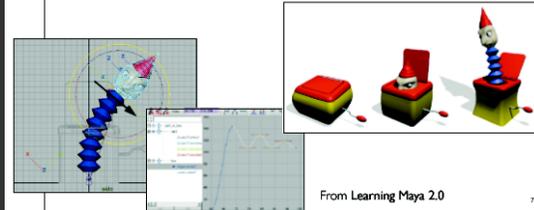
Keyframe Interpolation

- Inbetweening:
 - Cubic spline interpolation - maybe good enough
 - » May not follow physical laws



Keyframing

- Requires a highly skilled user
- Poorly suited for interactive applications
- High quality / high expense
- Limited applicability



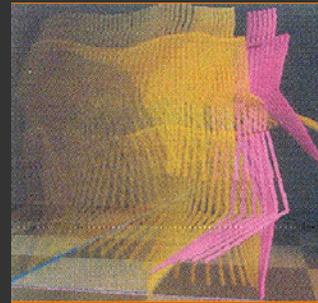
Motion Capture (recorded)

- Markers/sensors placed on subject
- Time-consuming clean-up
- Reasonable quality / reasonable price
- Manipulation algorithms an active research area



Inverse Kinematics

- Consider structure of articulated object

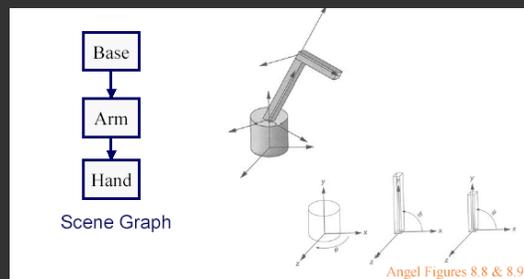


Outline

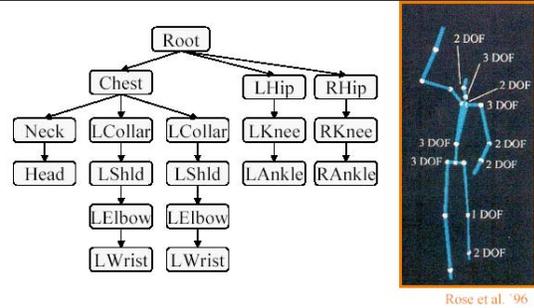
- Keyframes
- *Articulated Figures*
- Kinematics
- Dynamics

Articulated Figures

- Rigid objects connected by joints



Humanoid Characters



Outline

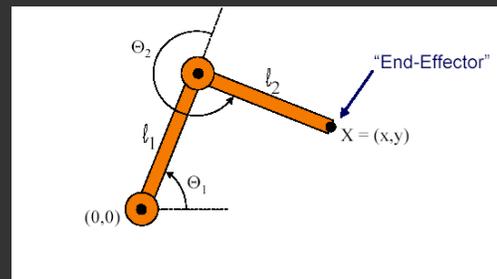
- Keyframes
- Articulated Figures
- Kinematics
- Dynamics

Kinematics and Dynamics

- Kinematics
 - Consider only motion. Positions, velocity, acceleration
- Dynamics
 - Considers underlying forces. Initial conditions+physics
- Articulated objects
 - Forward and inverse kinematics
 - Possibly forward and inverse dynamics
 - Many links to robotics, mechanics and other fields

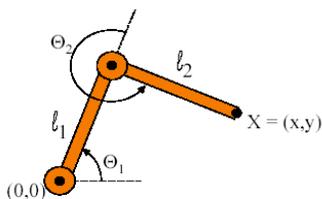
Simple 2 link arm

- 2 links connected by rotational joints



Forward Kinematics

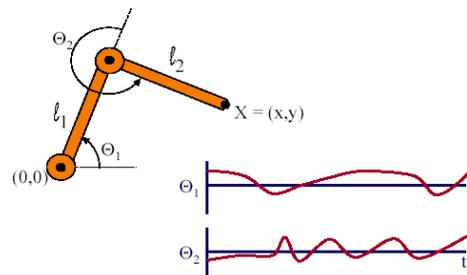
- Specify joint angles, computer finds end-effector



$$X = (l_1 \cos \theta_1 + l_2 \cos(\theta_1 + \theta_2), l_1 \sin \theta_1 + l_2 \sin(\theta_1 + \theta_2))$$

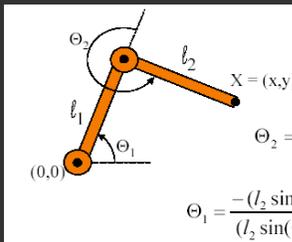
Forward Kinematics

- Then specify joint motions with spline curves



Inverse Kinematics

- Animator knows/specifies end-effector
 - System must compute joint angles
 - Harder, topic of next lecture, possible HW 5



$$\Theta_2 = \cos^{-1} \left(\frac{x^2 + y^2 - l_1^2 - l_2^2}{2l_1 l_2} \right)$$

$$\Theta_1 = \frac{-(l_2 \sin(\Theta_2)x + (l_1 + l_2 \cos(\Theta_2))y)}{(l_2 \sin(\Theta_2))y + (l_1 + l_2 \cos(\Theta_2))x}$$

Summary of Kinematics

- Forward kinematics
 - Specify joint angles, system computes end-effector
- Inverse kinematics
 - Easier to specify for most animations
 - Animator specifies end-effector
 - System computes joint angles (harder)
 - "Goal-Directed" motion (animator specifies end-goals)

Outline

- Keyframes
- Articulated Figures
- Kinematics
- Dynamics

Dynamics

- Consider underlying forces
- Motion from initial conditions, forces
- In graphics, include goals
 - Optimization to satisfy goals and physics

Dynamics

- Simulation to ensure physical realism
- Spacetime Constraints [Witkin and Kass '88]
 - Goals (e.g. jump from here to there)
 - Optimized motion (e.g. minimize energy or torque)
 - Character's physical structure (articulation)
 - Other constraints (foot contact, floor etc.)
 - Iterative optimization given constraint, objective

Spacetime Constraints

- Computer finds the "best" physical motion satisfying constraints
- Example: particle with jet propulsion
 - $\mathbf{x}(t)$ is position of particle at time t
 - $\mathbf{f}(t)$ is force of jet propulsion at time t
 - Particle's equation of motion is:

$$m\mathbf{x}'' - \mathbf{f} - m\mathbf{g} = 0$$
 - Suppose we want to move from a to b within t_0 to t_1 with minimum jet fuel:

$$\text{Minimize } \int_{t_0}^{t_1} f(t)^2 dt \quad \text{subject to } x(t_0) = a \text{ and } x(t_1) = b$$



Witkin & Kass '88

Spacetime Constraints

- Discretize time steps:

$$x'_i = \frac{x_i - x_{i-1}}{h}$$
$$x''_i = \frac{x_{i+1} - 2x_i + x_{i-1}}{h^2}$$

$$m \left(x''_i = \frac{x_{i+1} - 2x_i + x_{i-1}}{h^2} \right) - f_i - mg = 0$$

Minimize $h \sum_i |f_i|^2$ subject to $x_0 = a$ and $x_j = b$

Witkin & Kass '88

Spacetime Constraints

Advantages

- Directly specify goals, not low-level joint angles etc.
- Can easily edit and vary motions

Disadvantages

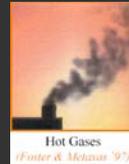
- Specifying constraints, objective functions
- Optimization, and avoiding local minima

Video



Dynamics: Physical Simulation

- Rigid Bodies
- Soft deformable objects
- Cloth
- Liquids (water)
- Gases (smoke, fluids)
- [Wrinkle Synthesis Video](#)



History of Computer Animation 2

- [Part 2 of video](#)