Foundations of Computer Graphics (Spring 2012)

CS 184, Lecture 5: Viewing http://inst.eecs.berkeley.edu/~cs184

To Do

- Questions/concerns about assignment 1?
- Remember it is due next Thu. Ask me or TAs re problems

Motivation

- We have seen transforms (between coord systems)
- But all that is in 3D
- We still need to make a 2D picture
- Project 3D to 2D. How do we do this?
- This lecture is about viewing transformations

Demo (Projection Tutorial)

- Nate Robbins OpenGL tutors
- Projection.exe
- Download others



What we've seen so far

- Transforms (translation, rotation, scale) as 4x4 homogeneous matrices
- Last row always 0 0 0 1. Last w component always 1
- For viewing (perspective), we will use that last row and w component no longer 1 (must divide by it)

Outline

- Orthographic projection (simpler)
- Perspective projection, basic idea
- Derivation of gluPerspective (handout: glFrustum)
 In new OpenGL, glm macro glm::lookAt glm::Perspective
- Brief discussion of nonlinear mapping in z

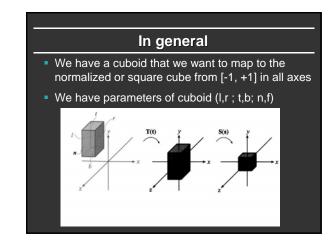
Not well covered in textbook chapter 7. We follow section 3.5 of real-time rendering most closely. Handouts on this will be given out.

Projections

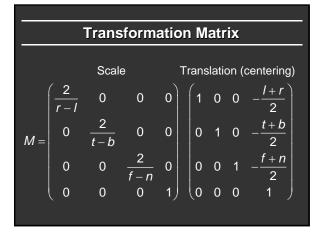
- To lower dimensional space (here 3D -> 2D)
- Preserve straight lines
- Trivial example: Drop one coordinate (Orthographic)

Orthographic Projection Characteristic: Parallel lines remain parallel Useful for technical drawings etc. Fig 7.1 in text Perspective

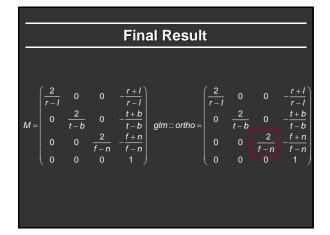
Example Simply project onto xy plane, drop z coordinate projection plane, z=0



Orthographic Matrix • First center cuboid by translating • Then scale into unit cube



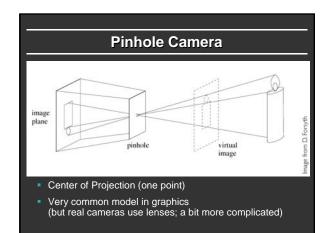
Caveats Looking down –z, f and n are negative (n > f) OpenGL convention: positive n, f, negate internally

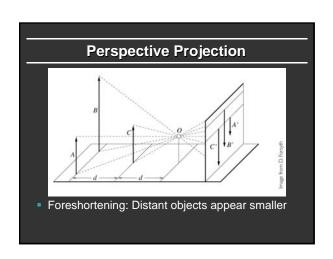


Outline

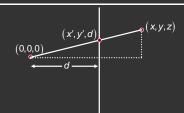
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- Perspective projection, basic idea
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 In modern OpenGL, glm::perspective
- Brief discussion of nonlinear mapping in z

Perspective Projection Most common computer graphics, art, visual system Further objects are smaller (size, inverse distance) Parallel lines not parallel; converge to single point Plane of Projection (camera/eye location)





Overhead View of Our Screen



Looks like we've got some nice similar triangles here?

$$\frac{x}{z} = \frac{x'}{d} \Rightarrow x' = \frac{d * x}{z} \qquad \frac{y}{z} = \frac{y'}{d} \Rightarrow y' = \frac{d * y}{z}$$

In Matrices

- Note negation of z coord (focal plane –d)
- (Only) last row affected (no longer 0 0 0 1)
- w coord will no longer = 1. Must divide at end

$$P = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{d} & 0 \end{pmatrix}$$

Verify

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{d} & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = ? \quad \begin{pmatrix} x \\ y \\ z \\ -\frac{z}{d} \end{pmatrix} = \begin{pmatrix} -\frac{d^*x}{z} \\ -\frac{d^*y}{z} \\ -d \\ 1 \end{pmatrix}$$

Vanishing Points

- Parallel lines "meet" at vanishing point
- (x,y) ~ (d_x, d_y) [directions]
- Every pixel vanishing pt for some dirn (lines parallel to image plane vanish infinity)
- Horizon





Perspective Distortions

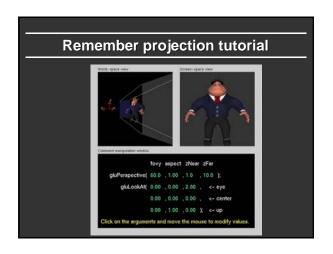
- Perspective can distort; artists often correct
- Computers can too (Zorin and Barr 95)

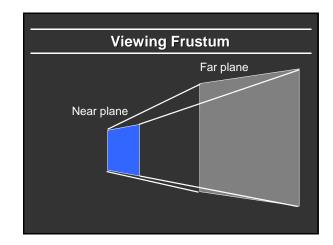


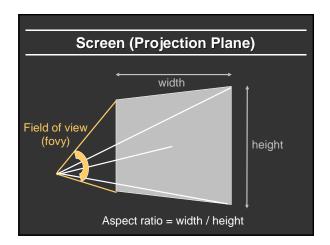


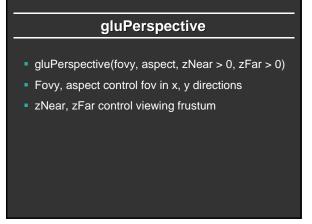
Outline

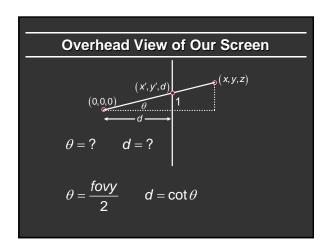
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in matrices						
Simplest form:	1 aspect		0	0		
P _	0 0	1	0	0		
, -	0	0				
	0	0	$-\frac{1}{d}$	0		
Aspect ratio taken into account						
Homogeneous, simpler to multiply through by d						
• Must map z vals based on near, far planes (not yet)						

In Matrices

$$P = \begin{pmatrix} \frac{1}{aspect} & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{d} & 0 \end{pmatrix} \rightarrow \begin{pmatrix} \frac{d}{aspect} & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & A & B \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

A and B selected to map n and f to -1, +1 respectively

Z mapping derivation

$$\begin{pmatrix} A & B \\ -1 & 0 \end{pmatrix} \begin{pmatrix} z \\ 1 \end{pmatrix} = ? \qquad \begin{pmatrix} Az + B \\ -z \end{pmatrix} = -A - \frac{B}{z}$$

Simultaneous equations?

$$-A + \frac{B}{n} = -1$$

$$-A + \frac{B}{f} = +1$$

$$A = -\frac{f + n}{f - n}$$

$$B = -\frac{2fn}{f - n}$$

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Mapping of Z is nonlinear

$$\begin{pmatrix} Az+B\\-z \end{pmatrix} = -A - \frac{B}{z}$$

- Many mappings proposed: all have nonlinearities
- Advantage: handles range of depths (10cm 100m)
- Disadvantage: depth resolution not uniform
- More close to near plane, less further away
- Common mistake: set near = 0, far = infty. Don't do this. Can't set near = 0; lose depth resolution.
- We discuss this more in review session

