Announcements

- **Project 0: Python Tutorial**
  - Due yesterday / Monday at 11:59pm (0 points in class, but pulse check to see you are in + get to know submission system)

- **Homework 0: Math self-diagnostic**
  - Optional, but important to check your preparedness for second half

- **Project 1: Search**
  - Will go out this week
  - Longer than most, and best way to test your programming preparedness

- **Sections**
  - Start this week, can go to any but priority in the one you signed up for on piazza

- **Instructional accounts: online (see our Welcome post on piazza)**

- **Pinned posts on piazza**

- **Reminder: We don’t use bCourses** [we use: class website, piazza, gradescope]
How about AI Research?

https://bair.berkeley.edu
CS 188: Artificial Intelligence

Search

Instructors: Pieter Abbeel & Dan Klein

University of California, Berkeley

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley (ai.berkeley.edu).]
Today

- Agents that Plan Ahead
- Search Problems
- Uninformed Search Methods
  - Depth-First Search
  - Breadth-First Search
  - Uniform-Cost Search
Agents that Plan
Reflex Agents

- Reflex agents:
  - Choose action based on current percept (and maybe memory)
  - May have memory or a model of the world’s current state
  - Do not consider the future consequences of their actions
  - Consider how the world IS

- Can a reflex agent be rational?
Video of Demo Reflex Optimal
Video of Demo Reflex Odd
Planning Agents

- **Planning agents:**
  - Ask “what if”
  - Decisions based on (hypothesized) consequences of actions
  - Must have a model of how the world evolves in response to actions
  - Must formulate a goal (test)
  - Consider how the world WOULD BE

- Optimal vs. complete planning

- Planning vs. replanning

[Demo: re-planning (L2D3)]
[Demo: mastermind (L2D4)]
Video of Demo Replanning
Video of Demo Mastermind
Search Problems
A search problem consists of:

- A state space
- A successor function (with actions, costs)
- A start state and a goal test

A solution is a sequence of actions (a plan) which transforms the start state to a goal state.
Search Problems Are Models
Example: Traveling in Romania

- **State space:**
  - Cities

- **Successor function:**
  - Roads: Go to adjacent city with cost = distance

- **Start state:**
  - Arad

- **Goal test:**
  - Is state == Bucharest?

- **Solution?**
What’s in a State Space?

The **world state** includes every last detail of the environment.

A **search state** keeps only the details needed for planning (abstraction).

### Problem: Pathing
- States: \((x,y)\) location
- Actions: NSEW
- Successor: update location only
- Goal test: is \((x,y)\)=END

### Problem: Eat-All-Dots
- States: \{(x,y), dot booleans\}
- Actions: NSEW
- Successor: update location and possibly a dot boolean
- Goal test: dots all false
State Space Sizes?

- World state:
  - Agent positions: 120
  - Food count: 30
  - Ghost positions: 12
  - Agent facing: NSEW

- How many
  - World states?
    \[ 120 \times (2^{30}) \times (12^2) \times 4 \]
  - States for pathing?
    120
  - States for eat-all-dots?
    \[ 120 \times (2^{30}) \]
Problem: eat all dots while keeping the ghosts perma-scared

What does the state space have to specify?
- (agent position, dot booleans, power pellet booleans, remaining scared time)
State Space Graphs and Search Trees
State Space Graphs

- State space graph: A mathematical representation of a search problem
  - Nodes are (abstracted) world configurations
  - Arcs represent successors (action results)
  - The goal test is a set of goal nodes (maybe only one)

- In a state space graph, each state occurs only once!

- We can rarely build this full graph in memory (it’s too big), but it’s a useful idea
State Space Graphs

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A search tree:

- A “what if” tree of plans and their outcomes
- The start state is the root node
- Children correspond to successors
- Nodes show states, but correspond to PLANS that achieve those states
- For most problems, we can never actually build the whole tree
We construct both on demand – and we construct as little as possible.

Each NODE in in the search tree is an entire PATH in the state space graph.
Quiz: State Space Graphs vs. Search Trees

Consider this 4-state graph:

How big is its search tree (from S)?
Quiz: State Space Graphs vs. Search Trees

Consider this 4-state graph:

How big is its search tree (from $S$)?

Important: Lots of repeated structure in the search tree!
Tree Search
Search Example: Romania
Searching with a Search Tree

- **Search:**
  - Expand out potential plans (tree nodes)
  - Maintain a *fringe* of partial plans under consideration
  - Try to expand as few tree nodes as possible
General Tree Search

function Tree-Search(problem, strategy) returns a solution, or failure
initialize the search tree using the initial state of problem
loop do
    if there are no candidates for expansion then return failure
    choose a leaf node for expansion according to strategy
    if the node contains a goal state then return the corresponding solution
    else expand the node and add the resulting nodes to the search tree
end

- Important ideas:
  - Fringe
  - Expansion
  - Exploration strategy

- Main question: which fringe nodes to explore?
Example: Tree Search
Example: Tree Search
Depth-First Search
Depth-First Search

Strategy: expand a deepest node first

Implementation:
Fringe is a LIFO stack
Search Algorithm Properties
Search Algorithm Properties

- **Complete:** Guaranteed to find a solution if one exists?
- **Optimal:** Guaranteed to find the least cost path?
- **Time complexity?**
- **Space complexity?**

**Cartoon of search tree:**
- $b$ is the branching factor
- $m$ is the maximum depth
- Solutions at various depths

**Number of nodes in entire tree?**
- $1 + b + b^2 + \ldots + b^m = O(b^m)$
Depth-First Search (DFS) Properties

- **What nodes DFS expand?**
  - Some left prefix of the tree.
  - Could process the whole tree!
  - If \( m \) is finite, takes time \( O(b^m) \)

- **How much space does the fringe take?**
  - Only has siblings on path to root, so \( O(bm) \)

- **Is it complete?**
  - \( m \) could be infinite, so only if we prevent cycles (more later)

- **Is it optimal?**
  - No, it finds the “leftmost” solution, regardless of depth or cost
Breadth-First Search
Breadth-First Search

Strategy: expand a shallowest node first

Implementation: Fringe is a FIFO queue
Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
  - Processes all nodes above shallowest solution
  - Let depth of shallowest solution be $s$
  - Search takes time $O(b^s)$

- How much space does the fringe take?
  - Has roughly the last tier, so $O(b^s)$

- Is it complete?
  - $s$ must be finite if a solution exists, so yes!

- Is it optimal?
  - Only if costs are all 1 (more on costs later)
Quiz: DFS vs BFS
Quiz: DFS vs BFS

- When will BFS outperform DFS?

- When will DFS outperform BFS?
Video of Demo Maze Water DFS/BFS (part 1)
Video of Demo Maze Water DFS/BFS (part 2)
Iterative Deepening

- Idea: get DFS’s space advantage with BFS’s time / shallow-solution advantages
  - Run a DFS with depth limit 1. If no solution...
  - Run a DFS with depth limit 2. If no solution...
  - Run a DFS with depth limit 3. ..... 

- Isn’t that wastefully redundant?
  - Generally most work happens in the lowest level searched, so not so bad!
BFS finds the shortest path in terms of number of actions. It does not find the least-cost path. We will now cover a similar algorithm which does find the least-cost path.
Uniform Cost Search
Uniform Cost Search

Strategy: expand the cheapest node first:

Fringe is a priority queue (priority: cumulative cost)

Cost contours
Uniform Cost Search (UCS) Properties

- What nodes does UCS expand?
  - Processes all nodes with cost less than cheapest solution!
  - If that solution costs $C^*$ and arcs cost at least $\varepsilon$, then the “effective depth” is roughly $C^*/\varepsilon$
  - Takes time $O(b^{C^*/\varepsilon})$ (exponential in effective depth)

- How much space does the fringe take?
  - Has roughly the last tier, so $O(b^{C^*/\varepsilon})$

- Is it complete?
  - Assuming best solution has a finite cost and minimum arc cost is positive, yes!

- Is it optimal?
  - Yes! (Proof next lecture via A*)
Uniform Cost Issues

- Remember: UCS explores increasing cost contours

- The good: UCS is complete and optimal!

- The bad:
  - Explores options in every “direction”
  - No information about goal location

- We’ll fix that soon!

[Demo: empty grid UCS (L2D5)]
[Demo: maze with deep/shallow water DFS/BFS/UCS (L2D7)]
Video of Demo Empty UCS
Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 1)
Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 2)
Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 3)
All these search algorithms are the same except for fringe strategies

- Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
- Practically, for DFS and BFS, you can avoid the log(n) overhead from an actual priority queue, by using stacks and queues
- Can even code one implementation that takes a variable queuing object
Search and Models

Search operates over models of the world

- The agent doesn’t actually try all the plans out in the real world!
- Planning is all “in simulation”
- Your search is only as good as your models...
Search Gone Wrong?