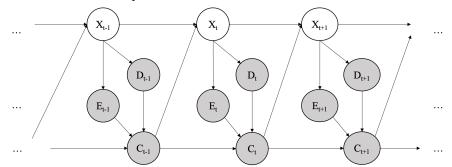
Introduction to Artificial Intelligence

Exam Prep 9

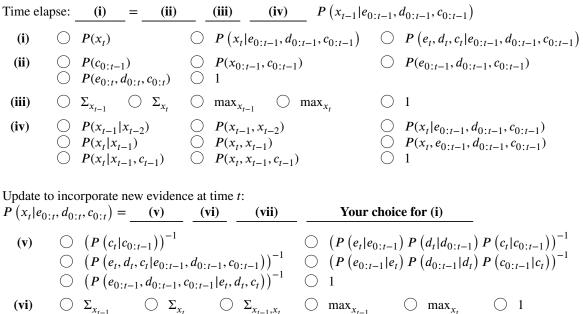
 $\bigcirc 1$

Q1. We Are Getting Close...

Mesut is trying to remotely control a car, which has gone out of his view. The unknown state of the car is represented by the random variable X. While Mesut can't see the car itself, his high-tech sensors on the car provides two useful readings: an estimate (E) of the distance to the car in front, and a detection model (D) that detects if the car is headed into a wall. Using these two readings, Mesut applies the controls (C), which determine the velocity of the car by changing the acceleration. The Dynamic Bayes Net below describes the setup.



(a) For the above DBN, complete the equations for performing updates. (Hint: think about the prediction update and observation update equations in the forward algorithm for HMMs.)



(vii)

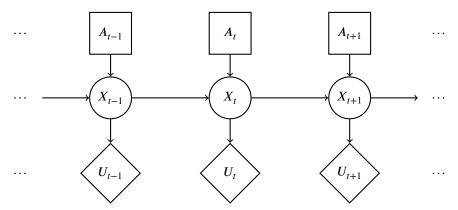
 $\bigcirc \Sigma_{x_{t-1}} \bigcirc \Sigma_{x_t} \bigcirc \Sigma_{x_{t-1},x_t}$ $\square P(x_t, e_t, d_t, c_t)$ $\square P(x_t, e_t, d_t, c_t, c_{t-1})$ $\square P(e_t, d_t, c_t | x_t)$ $\square P(x_t | e_t, d_t, c_t)$ $P(x_t|e_t, d_t, c_t, c_{t-1})$ $P(e_t, d_t|x_t)P(c_t|e_t, d_t, c_{t-1})$

(viii) Suppose we want to do the above updates in one step and use normalization to reduce computation. Select all the terms that are not explicitly calculated in this implementation. DO NOT include the choices if their values are 1.

(ii) (iv) (\mathbf{v}) (vi) (vii) None of the above

Q2. Planning ahead with HMMs

Pacman is tired of using HMMs to estimate the location of ghosts. He wants to use HMMs to plan what actions to take in order to maximize his utility. Pacman uses the HMM (drawn to the right) of length *T* to model the planning problem. In the HMM, $X_{1:T}$ is the sequence of hidden states of Pacman's world, $A_{1:T}$ are actions Pacman can take, and U_t is the utility Pacman receives at the particular hidden state X_t . Notice that there are no evidence variables, and utilities are not discounted.



(a) The belief at time t is defined as $B_t(X_t) = p(X_t|a_{1:t})$. The forward algorithm update has the following form:

$$B_t(X_t) =$$
 (i) (ii) $B_{t-1}(x_{t-1})$.

Complete the expression by choosing the option that fills in each blank.

(i)	$\bigcirc \max_{x_{t-1}}$	$\bigcirc \sum_{x_{t-1}}$	$\bigcirc \max_{x_t}$	$\bigcirc \Sigma_{x_t}$	\bigcirc 1
(ii)	$\bigcirc p(X_t x_{t-1})$	$\bigcirc p(X_t x_{t-1})p(X_t a_t)$	$\bigcirc p(X_t)$	$\bigcirc p(X_t x_{t-1},a_t)$	\bigcirc 1

 \bigcirc None of the above combinations is correct

(b) Pacman would like to take actions $A_{1:T}$ that maximizes the expected sum of utilities, which has the following form:

$$MEU_{1:T} = (i) (ii) (iii) (iv) (v)$$

Complete the expression by choosing the option that fills in each blank.

(i)	$\bigcirc \max_{a_{1:T}}$	$\bigcirc \max_{a_T}$	$\bigcirc \sum_{a_{1:T}}$	$\bigcirc \sum_{a_T}$	\bigcirc 1
(ii)	$\bigcirc \max_t$	$\bigcirc \prod_{t=1}^{T}$	$\bigcirc \sum_{t=1}^{T}$	$\bigcirc \min_t$	\bigcirc 1
(iii)	$\bigcirc \sum_{x_t,a_t}$	$\bigcirc \sum_{x_t}$	$\bigcirc \Sigma_{a_t}$	$\bigcirc \Sigma_{x_T}$	\bigcirc 1
(iv)	$\bigcirc p(x_t x_{t-1},a_t)$	$\bigcirc p(x_t)$	$\bigcirc B_t(x_t)$	$\bigcirc B_T(x_T)$	\bigcirc 1
(v)	$\bigcirc U_T$	$\bigcirc \frac{1}{U_t}$	$\bigcirc \frac{1}{U_T}$	$\bigcirc U_t$	\bigcirc 1

 \bigcirc None of the above combinations is correct

(c) A greedy ghost now offers to tell Pacman the values of some of the hidden states. Pacman needs your help to figure out if the ghost's information is useful. Assume that the transition function $p(x_t|x_{t-1}, a_t)$ is not deterministic. With respect to the utility U_t , mark all that can be True:

$$\bigcup_{\text{None of the above}} \text{VPI}(X_{t-1}|X_{t-2}) > 0 \qquad \bigcup_{\text{VPI}(X_{t-2}|X_{t-1})} > 0 \qquad \bigcup_{\text{VPI}(X_{t-1}|X_{t-2})} = 0 \qquad \bigcup_{\text{VPI}(X_{t-2}|X_{t-1})} = 0 \qquad \bigcup_{\text{None of the above}} \text{VPI}(X_{t-1}|X_{t-2}) = 0 \qquad \bigcup_{\text{VPI}(X_{t-1}|X_{t-1})} \text{VPI}(X_{t-1}|X_{t-1}) = 0 \qquad \bigcup_{\text{None of the above}} \text{VPI}(X_{t-1}|X_{t-1}) = 0 \qquad \bigcup_{\text{None of$$

(d) Pacman notices that calculating the beliefs under this model is very slow using exact inference. He therefore decides to try out various particle filter methods to speed up inference. Order the following methods by how accurate their estimate of $B_T(X_T)$ is? If different methods give an equivalently accurate estimate, mark them as the same number.

	Most			Least
	accurate			accurate
Exact inference	\bigcirc 1	\bigcirc 2	\bigcirc 3	0 4
Particle filtering with no resampling	\bigcirc 1	\bigcirc 2	\bigcirc 3	0 4
Particle filtering with resampling before every time elapse	\bigcirc 1	\bigcirc 2	\bigcirc 3	0 4
Particle filtering with resampling before every other time elapse	\bigcirc 1	\bigcirc 2	○ 3	0 4