## 188 Introduction to 2021 Artificial Intelligence Exam Prep 11 Solutions

## Q1. Machine Learning: Potpourri

- (a) What it the **minimum** number of parameters needed to fully model a joint distribution  $P(Y, F_1, F_2, ..., F_n)$  over label Y and *n* features  $F_i$ ? Assume binary class where each feature can possibly take on *k* distinct values.  $2k^n 1$
- (b) Under the Naive Bayes assumption, what is the minimum number of parameters needed to model a joint distribution  $P(Y, F_1, F_2, ..., F_n)$  over label Y and n features  $F_i$ ? Assume binary class where each feature can take on k distinct values. 2n(k-1) + 1
- (c) You suspect that you are overfitting with your Naive Bayes with Laplace Smoothing. How would you adjust the strength *k* in Laplace Smoothing?

While using Naive Bayes with Laplace Smoothing, increasing the strength $k$ in Laplace Smoothing can:	
Increase training error Decrease training error	
Increase validation error Decrease validation error	
It is possible for the perceptron algorithm to never terminate on a dataset that is linearly separable in its feature s	pace.
<ul> <li>True</li> <li>False</li> </ul>	
If the perceptron algorithm terminates, then it is guaranteed to find a max-margin separating decision boundary.	
○ True  False	

- (g) In binary perceptron where the initial weight vector is  $\vec{0}$ , the final weight vector can be written as a linear combination of the training data feature vectors.
  - True
     True
     True
- (h) For binary class classification, logistic regression produces a linear decision boundary.
  - True

(**d**)

**(e)** 

(**f**)

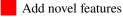
(i) In the binary classification case, logistic regression is exactly equivalent to a single-layer neural network with a sigmoid activation and the cross-entropy loss function.

True

○ False

○ False

(j) You train a linear classifier on 1,000 training points and discover that the training accuracy is only 50%. Which of the following, if done in isolation, has a good chance of improving your training accuracy?



Train on more data

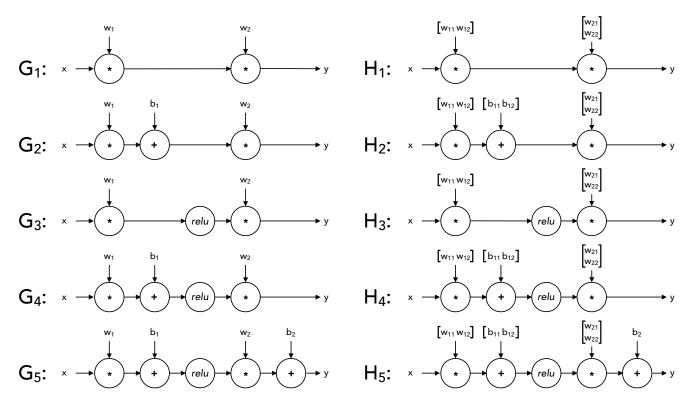
(k) You now try training a neural network but you find that the training accuracy is still very low. Which of the following, if done in isolation, has a good chance of improving your training accuracy?



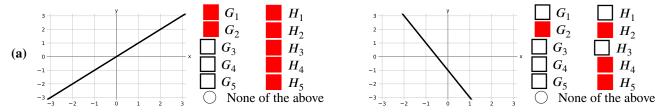
Add more hidden layers

Add more units to the hidden layers

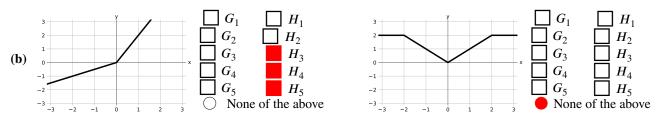
## Q2. Neural Networks: Representation



For each of the piecewise-linear functions below, mark all networks from the list above that can represent the function **exactly** on the range  $x \in (-\infty, \infty)$ . In the networks above, *relu* denotes the element-wise ReLU nonlinearity: relu(z) = max(0, z). The networks  $G_i$  use 1-dimensional layers, while the networks  $H_i$  have some 2-dimensional intermediate layers.



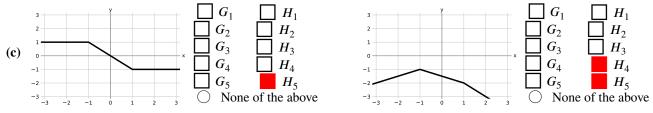
The networks  $G_3$ ,  $G_4$ ,  $G_5$  include a ReLU nonlinearity on a scalar quantity, so it is impossible for their output to represent a non-horizontal straight line. On the other hand,  $H_3$ ,  $H_4$ ,  $H_5$  have a 2-dimensional hidden layer, which allows two ReLU elements facing in opposite directions to be added together to form a straight line. The second subpart requires a bias term because the line does not pass through the origin.



These functions include multiple non-horizontal linear regions, so they cannot be represented by any of the networks  $G_i$  which apply ReLU no more than once to a scalar quantity.

The first subpart can be represented by any of the networks with 2-dimensional ReLU nodes. The point of nonlinearity occurs at the origin, so nonzero bias terms are not required.

The second subpart has 3 points where the slope changes, but the networks  $H_i$  only have a single 2-dimensional ReLU node. Each application of ReLU to one element can only introduce a change of slope for a single value of x.



Both functions have two points where the slope changes, so none of the networks  $G_i$ ;  $H_1$ ,  $H_2$  can represent them.

An output bias term is required for the first subpart because one of the flat regions must be generated by the flat part of a ReLU function, but neither one of them is at y = 0.

The second subpart doesn't require a bias term at the output: it can be represented as  $-relu(\frac{-x+1}{2}) - relu(x + 1)$ . Note how if the segment at x > 2 were to be extended to cross the x axis, it would cross exactly at x = -1, the location of the other slope change. A similar statement is true for the segment at x < -1.